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title: "homework3"
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output: word_document
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```{r setup, include=FALSE}
knitr::opts_chunk$set(echo = TRUE)
library(readxl)
mane6313_homework3 <- read_excel("mane6313_homework3.xlsx")
```

## Problem 2.28

### part a

```{r echo=TRUE}
var.test(mane6313_homework3$p2_28_type1, mane6313_homework3$p2_28_type2, alternative = "two.sided", conf.level = 0.95)
```

The p-value for the F-test is 0.9744. Using  $\alpha = 0.05$ , the conclusion of the hypothesis test  $H_0: \frac{\sigma^2_1}{\sigma^2_2} = 1$  versus  $H_1: \frac{\sigma^2_1}{\sigma^2_2} \neq 1$  is fail to reject  $H_0$ . Thus, it can be assumed that the variances are equal.

### Part b

Conduct a two-sample t-test to determine if the means are equal. Use  $\alpha = 0.05$ .

```{r}
t.test(mane6313_homework3$p2_28_type1, mane6313_homework3$p2_28_type2, alternative = "two.sided", mu = 0, paired = FALSE, var.equal = TRUE, conf.level = 0.95)
```

The p-value for the t-test is 0.9622. Using  $\alpha = 0.05$ , the conclusion of the hypothesis test  $H_0: \mu_1 = \mu_2 = 0$  versus  $H_1: \mu_1 \neq \mu_2$  is fail to reject  $H_0$ . Thus, it can be assumed that the means are equal.

### Part c

Test for normality.

```{r}
library(car)

```

```
qqPlot(mane6313_homework3$p2_28_type1)
qqPlot(mane6313_homework3$p2_28_type2)
```

```

Observing both normal probability plots (qqPlots), all points for both plots lie within the confidence bands. Therefore, it can be assume that both samples are from a normal distribution.

Problem 2.33

Part a

Construct a 95% confidence interval for σ^2 .

```
```{r}
library(EnvStats) # import library
varTest(mane6313_homework3$p2_33, alternative = "two.sided",
conf.level = 0.95, sigma.squared=1.0)
```
```

From the output, the 95% confidence interval for σ^2 is (0.4571524, 1.6862395)

Part b

Perform a hypothesis test of $H_0: \sigma^2=1$ versus $H_1: \sigma^2 \neq 1$. Use $\alpha=0.05$.

```
```{r}
library(EnvStats) # import library
varTest(mane6313_homework3$p2_33, alternative = "two.sided",
conf.level = 0.95, sigma.squared=1.0)
```
```

From the varTest output, the p-value is 0.5572. Since p-value is greater than α , the conclusion is fail to reject H_0 and accept the null hypothesis that σ^2 is equal to one.

Part c

Check the assumption of normality.

```
```{r}
library(car)
car::qqPlot(mane6313_homework3$p2_33)
```
```

Notice that a point is beyond the confidence bands. Therefore, the data is not from a normal distribution and it is not appropriate to use the t-test. A non-parametric test such as Kruskal-Wallis test should be used.

Problem 2.34

Part a

Conduct a test of hypothesis using $\alpha=0.05$ to determine if $H_0: \mu_d=0$ versus $H_1: \mu_d \neq 0$.

```
```{r}
t.test(mane6313_homework3$p2_34_caliper1, mane6313_homework3$p2_34_caliper2, alternative = "two.sided", mu=0, paired=TRUE, conf.level = 0.95)
```

```

The critical value for the rejection region is given below.

```
```{r}
qt(.975,11)
```

Since the absolute value of the test statistics is not greater than the critical value, 2.200985. The conclusion is to fail to reject  $H_0$  and accept the null hypothesis that the means are equal.

### Part b

The p-value, observed from the part a output, is 0.6742.

### Part c

The value of the two-sided 95% confidence interval, found in the part a output, is (-0.001024344, 0.001524344).