

# Printout

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## Section 1

MANE 6313

## Subsection 1

### Week 12, Module E

## Student Learning Outcome

- Select an appropriate experimental design with one or more factors,
- Select an appropriate model with one or more factors,
- Evaluate statistical analyses of experimental designs,
- Assess the model adequacy of any experimental design, and
- Interpret model results.

## Module Learning Outcome

*Assessing linear regression model diagnostics.*

Resources for the Week 12, Module E micro-lecture are:

- Week 12, Module E Micro-lecture
- Week 12, Module E Marked Notes

## Assessing Linear Regression Model Diagnostics

provide table of contents

$R^2$

- The coefficient of multiple determination is defined to be

$$R^2 = \frac{SS_R}{SS_T} = 1 - \frac{SS_E}{SS_T}$$

- $R^2$  is the reduction in variability (in the data) due to using the regressor variables  $x_1, x_2, \dots, x_k$  (the model).

- A larger  $R^2$  value indicates more of the total variability is explained by the model; **however it does not imply that the model is a GOOD model**
- $R^2$  always increases as the number of terms in the model is increased
- Adjusted  $R^2$  is  $\{x_1, x_2, x_3, \text{like } SOI, \text{ etc.}\}$

$$R_{\text{adj}}^2 = 1 - \frac{SS_E/(n-p)}{SS_T/(n-1)} = 1 - \left( \frac{n-1}{n-p} \right) (1 - R^2)$$

- penalty for unnecessary terms in the model
- $R^2$  &  $R_{\text{adj}}^2$  are close

## Model Assumptions and Residuals

- Least squares estimation requires that  $E(\varepsilon) = 0$  and  $V(\varepsilon) = \sigma^2$  and the  $\{\varepsilon_i\}$  are uncorrelated
- To perform statistical hypothesis tests, we further assume that  $\varepsilon \sim \text{NID}(0, \sigma^2)$
- These assumptions are validated by examining the residuals
- Perform same analyses previously used for the fixed effects model

## Minitab Demonstration

## Model Summary

S	R-sq	R-sq(adj)	R-sq(pred)
4.80885	98.37%	97.14%	93.47%

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