



Fundamental Definitions

Random experiment

7 stocks tic

is an experiment that can result in different outcomes, even though it is repeated in the same manner

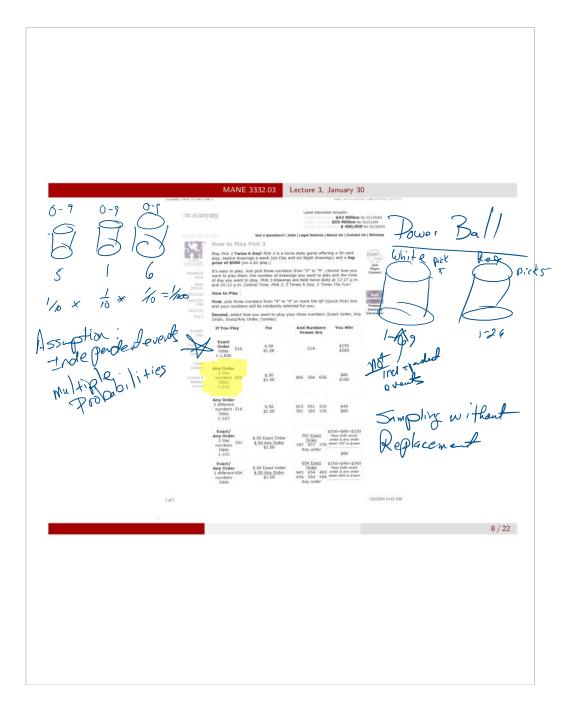
Sample Space

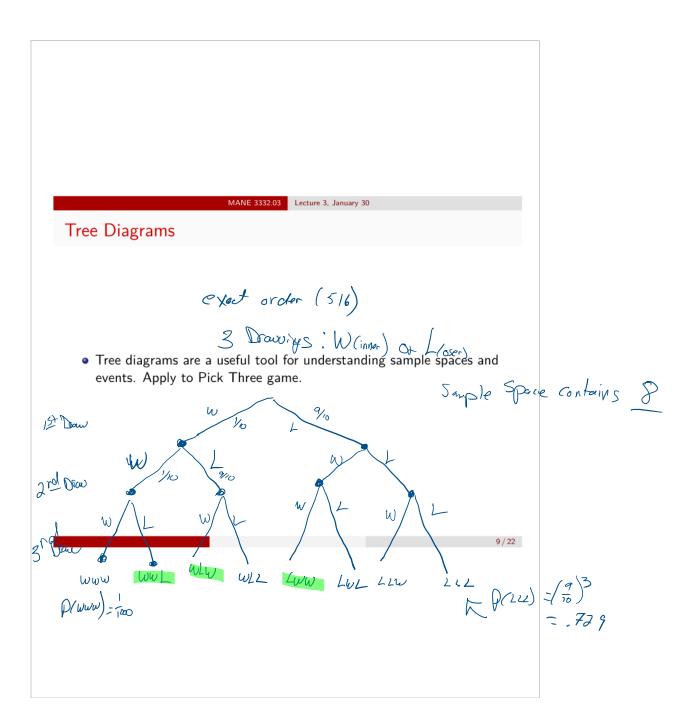
is the set of all possible outcomes of a random experiment

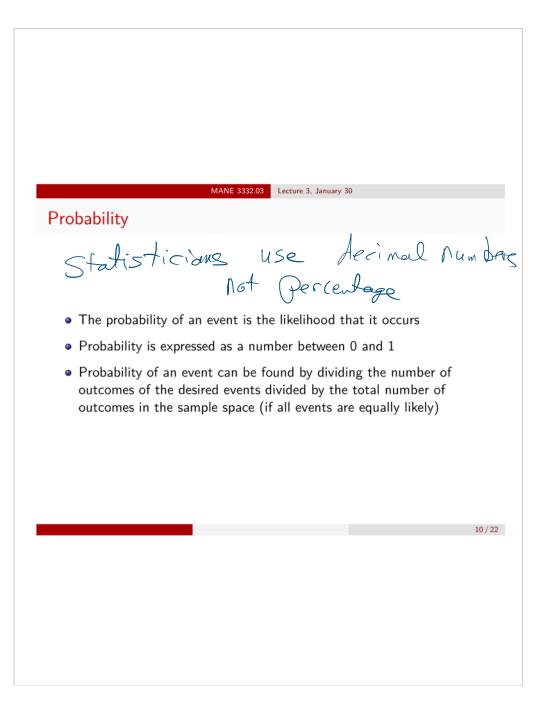
Event

is a subset of the sample space of a random experiment









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Lecture 3, January 30

Counting Techniques

• Consider ordered versus unordered subsets

• Ordered subsets (Permutations)

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• Ordered subsets (Permutations)

$$P_r^n = \frac{n!}{(n-r)!}$$

 $P_r^n = \frac{n!}{(n-r)!}$ Unordered subsets (Combinations)

We have (Jose, Leo, Miguel) $C_{n,r} \circ r \stackrel{h}{\subset} C_r^n = \frac{n!}{r!(n-r)!} = \binom{n!}{r} \quad \text{where } r$

· Good idea to do a calculator check

 $\begin{pmatrix} 3 \\ 2 \end{pmatrix} = 2 \frac{3!}{(3-2)!}$

$$3!=3.2!$$
 recursive = $\frac{3.2}{2!}$ (1!)

Stopping point $\emptyset!=1$ = 3

Calculators

Axioms (Rules) of Probability

Probability is a number that is assigned to each member of a collection of events from a random experiment that satisfies the following properties:

If S is the sample space and E is any event in a random experiment,

$$P(S) = 1$$

2
$$0 \le P(E) \le 1$$

3 For two events E_1 and E_2 with $E_1 \cap E_2 = \emptyset$



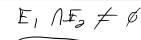
$$P(E_1 \cup E_2) = P(E_1) + P(E_2)$$

• Consider problem 2-70

Venn Diggrams

+ P(E2) (always frue) General Rulp P(E, VE) = P(E,) + P(E2)

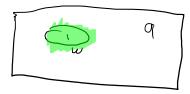






Practice Problems - Single Event

Compliment of on Event

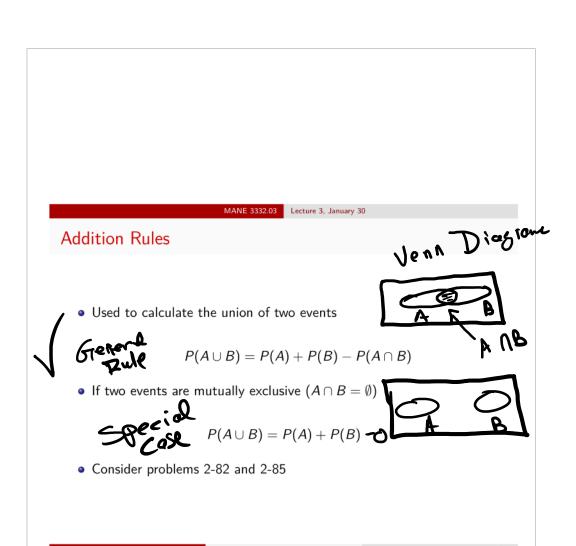


 $P(W') = 1 - P(W) = 1 - (\frac{1}{10}) - \frac{9}{10}$



MANE 3332.03 Lecture 3, January 30 Probability of Multiple Events 1- Cop Intersection: $P(A \cap B)$ is "the probability of A and B occurring U-cup Union: $P(A \cup B)$ is "the probability of A or B (or both)" Complement: P(A') is "the probability of not A" • Venn diagrams are a very useful tool for understanding multiple events and calculating probabilities trial (Block, 3) (A NB)

Size of Suple spine? (A UB)



P(AUBUCUD)

Addition Rule for 3 or More Events 21

For three events

Three events
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- For a set of events to mutually exclusive all pairs of variables must satisfy $E_1 \cap E_2 = \emptyset$
- For a collection of mutually exclusive events,

$$P(E_1 \cup E_2 \cup ... \cup E_k) = P(E_1) + P(E_2) + ... + P(E_k)$$

Conditional Probability

- Hayter (2002) states that "For experiments with two or more events of interest, attention is often directed not only at the probabilities of individual events but also at the probability of an event occurring conditional on the knowledge that another event has occurred."
- The **conditional probability** of an event B given an event A, denoted P(B|A) is BIA-Baiver A

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

for P(A) > 0

• Consider problems 2-99

Multiplication Rules

• This rule provides another method for calculating $P(A \cap B)$

$$P(A \cap B) = P(A|B)P(B) = P(B|A)P(A)$$

• This leads to the total probability rule

$$P(B) = P(B \cap A) + P(B \cap A')$$

= $P(B|A)P(A) + P(B|A')P(A')$

• Consider problems from 3rd edition (next slide) and 2-129



Example Problem 2-76

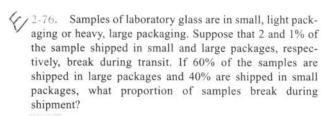


Figure 3: problem 2-76

Independent Events

• Two events are independent if any one of the following is true:

• P(A|B) = P(A)• P(B|A) = P(B)• $P(A \cap B) = P(A)P(B)$ • Consider problem 2-146

Reliability Analysis

- Reliability is the application of statistics and probability to determine the probability that a system will be working properly
- Components can be arranged in series. All components must work for the system to work.

$$P(\text{system works}) = P(A \text{ works})P(B \text{ works})$$

• Components can be arranged in parallel. As long as one component works, the system works.

$$P(\text{system works}) = 1 - (1 - P(A \text{ works})) \times 1 - P(B \text{ works}))$$

• Consider problem 2-157

Farming of Pack 3

only exact match

Dy \$1 if right win \$500 if wrong took loss doker

Winning $(500-1)(\frac{1}{100}) + -1(\frac{999}{1000}) = expected winning$

- -,50

Single event pp

Tuesday, February 4, 2025 11:07 AM

QUESTION 1

Consider a problem classified by 2 rows and 3 columns containing 200 observations. The table is described in the figure below and has the following cell counts: A=109, B=52, C=14,

	column 1	column 2	column 3	
D=12, E=8, F=5. Let event S denote an item that occurs in row 1. Find P(S).	A	B	C	109 52 14
rowa	D	E	F	12 8 5
The correct answer is not provided 0 0.605 0 0.3	A+ B+	<u> </u>	N=200	
○ 0.6904 ○ 0.4001	h		200	

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0.0950.125

QUESTION 3

Consider a problem classified by 2 rows and 3 columns containing 500 observations. The table is described in the figure below and has the following cell counts: A=306, B=47, C=92,

D=17, E=26, F=12. Let event T denote an item that occurs in column 3. Find P(T').	A I	B C	301	0 47	9. Iá
) E	F		7 26	Ιá
The correct answer is not provided					
The correct answer is not provided 0.646 0.354 0.146 0.854 $= 1 - (-7)$	$\left(\frac{C+F}{\Lambda}\right)=$		92+12 300	= .79	⁷ 2

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Single event pp

Tuesday, February 4, 2025 11:14 AM

QUESTION 5

Consider a problem classified by 2 rows and 3 columns containing 1000 observations. The table is described in the figure below and has the following cell counts: A=317, B=237, C=270,

D=11, E=46, F=119. Let event T denote an item that occurs in column 1. Find P(T).

Towal B C 317 237 270

Towal D E F 119

0.283

0.389

0.328

O The correct answer is not provided

0.672

 $\Re(7) = \frac{A+D}{n} = \frac{3/7+11}{1000} = .328$

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QUESTION 7

Consider a problem classified by 2 rows and 3 columns containing 300 observations. The table is described in the figure below and has the following cell counts: A=115, B=55, C=5,

D=16, E=12, F=97. Let event S denote an item that occurs in row 1. Find P(S'). Tow 1

A
B
C
115 55 5
16 12 97

N = 300

0.5833

0.6883

0.4167 0 0.34

O The correct answer is not provided

0.4367

0.2233

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Tuesday, February 4, 2025 11:47 AM

P(A)= .3, P(B)=.2 P(A)B)=.1

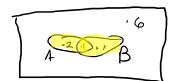
3 P/A') = 1-P/A) = 1-.3=.7





6)P(AVB) = P(A)+ P(B) -P(A)

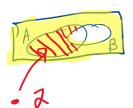
not to sale



SP(A'1B) = 1

J) P(A n B')





 $P(A' \cup B) = P(A') + P(B) - P(A' \cap B)$ (1-3) + .2 - .1 = .8

Find PIS or Ti. Power dipping taken. 2/6/2051:15 AM

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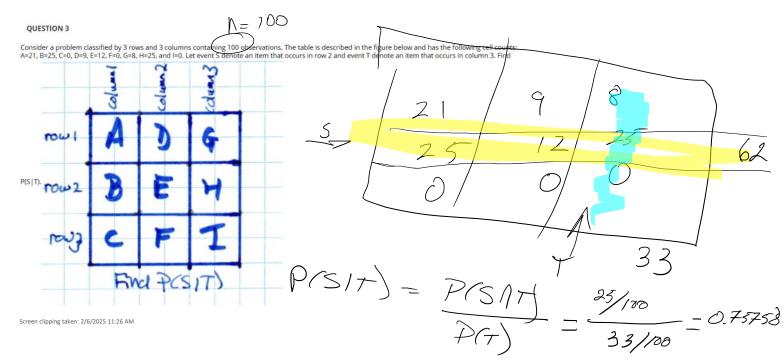
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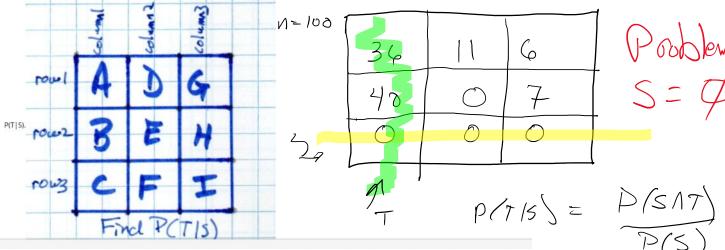
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- .3 H



QUESTION 5

Consider a problem classified by 3 rows and 3 columns containing 100 observations. The table is described in the figure below and has the following cell counts: A=36, B=40, C=0, D=11, E=0, F=0, G=6, H=7, and I=0. Let event S denote an item that occurs in row 3 and event T denote an item that occurs in column 1. Find



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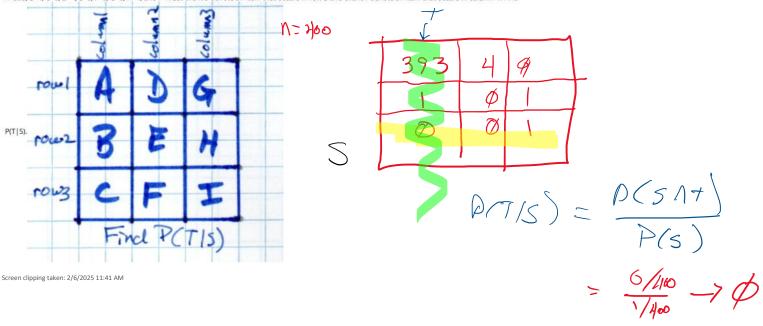
 $\frac{7}{7} \quad \frac{p(7/5)}{F(5)} = \frac{p(5)7}{P(5)}$ For P(5)70Oves not exist! Because P(5)=0

Two events pp

Thursday, February 6, 2025

11:40 AM

Consider a problem classified by 3 rows and 3 columns containing 400 observations. The table is described in the figure below and has the following cell counts: A=393, B=1, C=0, D=4, E=0, F=0, G=0, H=1, and I=1. Let event S denote an item that occurs in row 3 and event T denote an item that occurs in column 1. Find



Two events pp

Thursday, February 6, 2025 11:46 AM

Consider a problem classified by 3 rows and 3 columns containing 400 observations. The table is described in the figure below and has the following cell counts: A=231, B=2, C=0, D=165, E=0, F=0, G=2, H=0, I=0. Let event S denote an item that occurs in row 2 and event T denote an item that occurs in row 2. 2 row row 2 $P(S \Lambda 7) = \frac{2}{400} = \frac{1}{200}$ = . 005

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FIND D(SOT) Sand