





MANE 2222 /

# Introduction to Hypothesis Testing

Make decision (inference)

### Decision Making for a Single Sample

- Inferential statistics consists of methods used to make decisions or draw conclusions about a population using information contained in a sample
- Inference is divided into two major areas:
  - Parameter estimation (both point and interval)
  - Hypothesis testing

### Overview of Statistical Hypotheses

- Many engineering problems require a decision to be made regarding some statement about a parameter
  - The statement is called a hypothesis
  - The decision-making process about the hypothesis is call **hypothesis** testing
- Statistical hypothesis testing is usually the data analysis stage of a comparative experiment
- A procedure leading to a decision about a particular hypothesis is called a test of hypothesis
- Testing the hypothesis involves taking a random sample, computing a test statistic from the sample data and then using the to make a decision

#### Statistical Hypothesis

- A **statistical hypothesis** is a statement about the parameters of one or more populations
- A statistical hypothesis has two parts a null hypothesis (denoted H<sub>0</sub>) and an alternative hypothesis (denoted H<sub>1</sub>)
  - The null hypothesis contains an equality statement about the value of parameter. For example  $H_0: \mu=12$  ounces.
  - There are three possible alternative hypotheses:  $H_1: \mu \neq 12$ ,  $H_1: \mu < 12$ , or  $H_1: \mu > 12$
  - The goal of the research will determine the appropriate alternative hypothesis

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Mull hypothosis

Ho; parameter = value

It ternative Hypothesis

H, or Ha

H;: N>12 (upper one-sided)

A;: N<12 (lower one-sided)

H;: N≠12 (two-sided or two-tailed)

### Summary of One-Sample Hypothesis-Testing Procedures

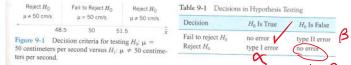
Case	Null Hypothesis	Test Statistic	Alternative Hypothesis
1.	$H_0: \mu = \mu_0$	$\overline{x} - \mu_0$	$H_1: \mu \neq \mu_0$
	$\sigma^2 \; known$	$z_0 = \frac{1}{\sigma / \sqrt{n}}$	$H_1: \mu > \mu$
			$H_1: \mu < \mu_0$

9/15 A Hordano

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#### Errors in hypothesis testing

- Whether a correct decision is made depends upon the true nature of  $H_0$  and the decision arrived at.
- A **type I error** occurs when the null hypothesis is true and the outcome of the test is to reject  $H_0$ . The probability of a type I error is denoted as  $\alpha$
- A type II error occurs when the null hypothesis is false and the outcome of the test is to fail to reject H<sub>0</sub>. The probability of a type II error is denoted as β.
- The power of a statistical test is the probability rejecting the null hypothesis  $H_0$  when the alternative hypothesis is true. Power =  $1-\beta$



f (6, 0, 11, a)

Ho: Part is food

Hi: Part is not good for oreh Error Example: Manufacturing 2×2 Case 1) Is to true? 2) What is my decision? Preject Ho Hotrue Ho falsp (healthy) (sick

Ho felsp (sick to be the feet to be

- State an appropriate test statistic, & Cakalete
- State the rejection region for the (test) statistic,
- O Compute any necessary sample quantities, substitute these into the equation for the test statistics, and compute that value,
- Decide whether or not H<sub>0</sub> should be rejected and report in the problem context

## Chapter 9, Case 1

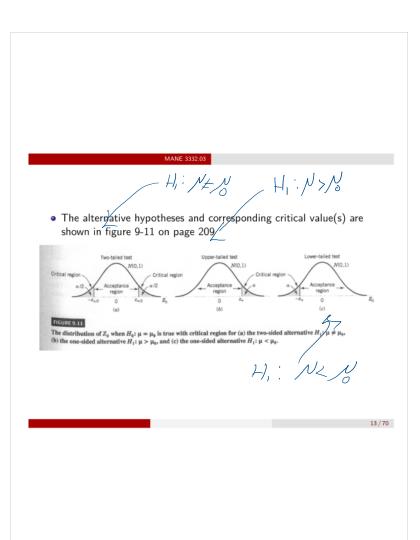
Inference on the Mean of a population, variance known

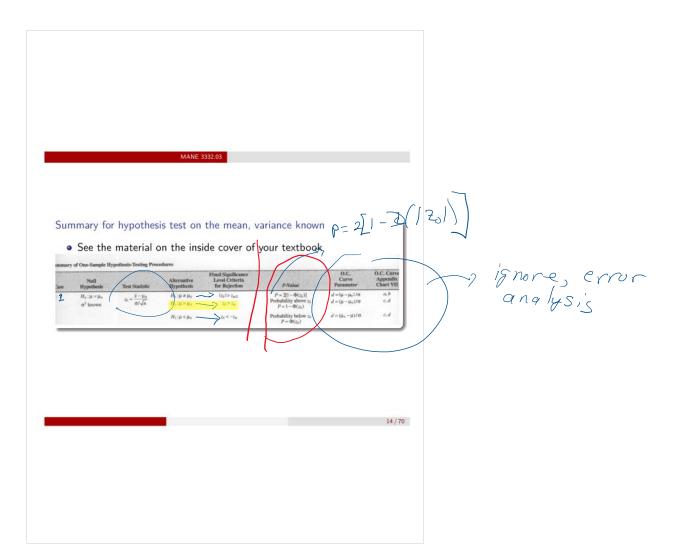
- Assumptions:
  - $lackbox{1}{}$   $X_1, X_2, \ldots, X_n$  is a random sample of size n from a population
  - The population is normal, or if it is not normal, the conditions of the central limit theorem apply ( lag < Somple n > 30)
- $\bullet$  The parameter of interest is  $\mu$
- The null hypothesis is  $H_0: \mu = \mu_0$  \ \sqrt{a}/\mu \end{a} \ \text{ve} \ \text{or rum} \ \lambda \ \end{a} \ \end{a}

$$Z_0 = \frac{\overline{X} - \mu_0}{\sigma / \sqrt{n}}$$

and has a standard normal distribution

Recall Chapter 8, Gse 1 X-Zas m < Na X + Zaz m





Problem 1

#### Example 11-1

The burning rate of a rocket propellant is being studied. Specifications require that the mean burning rate must be 40 cm/s. Furthermore, suppose that we know that the standard deviation of the burning rate is approximately 2 cm/s. The experimenter decides to specify a type I error probability  $\alpha = 0.05$ , and he will base the test on a random sample of size n = 25. The hypotheses we wish to test are

$$H_0$$
:  $\mu = 40$  cm/s,

 $H_1$ :  $\mu \neq 40$  cm/s.

Twenty-five specimens are tested, and the sample mean burning rate obtained is  $\bar{x} = 41.25$  cm/s.

Source: Himes. Mortgomeny, Goodsman, Bornor (2003). Probability and Statistics in Engineering, 4th ad.

Rejection Region

Hi: N£ 40 (two-to, led tax)

Know d = -05 0 -2, 1=25

@ Test Statistic  $20 = \frac{\overline{x} - 10}{0 / vn} = \frac{41.25 - 40}{2 / \sqrt{25}}$ 

= 3.125 (3) Reject Riegion (H,) Reject Ho if

(Zo/) Zaz = Z.05% =1.96

(2) Conclusion:

Since 13.105/> 1.96, we rojed to 7 we found evidence tool the main

burn rate is not 40cm/

### Problem 2

9.2.10 The bacterial strain Acinetobacter has been tested for its adhesion properties. A sample of five measurements gave readings of 2.69, 5.76, 2.67, 1.62 and 4.12 dyne-cm2. Assume that the standard deviation is known to be 0.66 dyne-cm<sup>2</sup> and that the scientists are interested in high adhesion (at least 2.5 dyne-cm2).

- a. Should the alternative hypothesis be one-sided or two-sided?
- b. Test the hypothesis that the mean adhesion is 2.5 dyne-cm2.
- c. What is the P-value of the test statistic?

**Summary Statistics** 

x<-c(2.69,5.76,2.67,1.26,4.12) library(psych)

describe(x)

## vars n mean | median trimmed mad min max range skew kurtosis se ## X1 15 3.3 1/71 2.69 3.3 2.12 1.26 5.76 4.5 0.26 -1 71 4 74

45' N=2.5 H,: N> 2.5

= 33-25 -2.7104

BREjection Region

Rged Ho if Zo>Za Set x = .05 Reject Huif Zot Z.os-

2.0= 1.645

A) Grebsion: Reject Ho

**8** OS 16 / 70 A) Corclusion: Reject Ho

#### Connection between Hypothesis Tests and CI

- · There is a close connection between confidence intervals and hypothesis tests
- ullet Consider a 100(1-lpha)% confidence interval on  $\mu$  and a hypothesis test of size  $\alpha$  shown below

 $H_0: \mu = \mu_0$  $H_1: \mu \neq \mu_0$ 

- ullet The conclusion to reject  $H_0$  will be reached if  $\mu_0$  is not contained within the confidence interval
- If  $\mu_0$  is within the confidence interval, we fail to reject  $H_0$
- The  $100(1-\alpha)\%$  confidence interval on  $\mu$  is the acceptance region

confidence interval/bound
is the acceptance
Resion
if you are not in
the confidence interval/
bound, you are interval
Rejection Repion

#### P-values

- Is a widely used alternative to the traditional hypothesis test
- ullet Definition: The p-value is the smallest level of significance that would lead to reject of the null hypothesis  $H_0$  with the given data
- Formulas are given below

$$P = \left\{ egin{array}{ll} 2[1-\Phi(|z_0|)] & \mbox{for a two-tailed test} \ 1-\Phi(z_0) & \mbox{for a upper-tailed test} \ \Phi(z_0) & \mbox{for a lower-tailed test} \end{array} 
ight.$$

 $\bullet$  Usage: if  $p\text{-value}{<}\alpha$  then the conclusion is reject H0, otherwise fail to reject H0

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H,: N>2.5

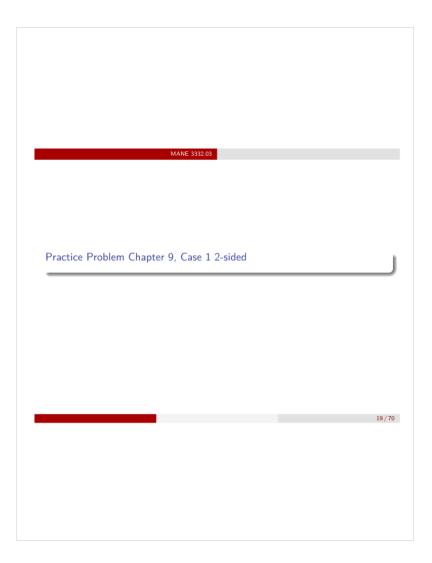
accortance \( \pi = 0.05 \)

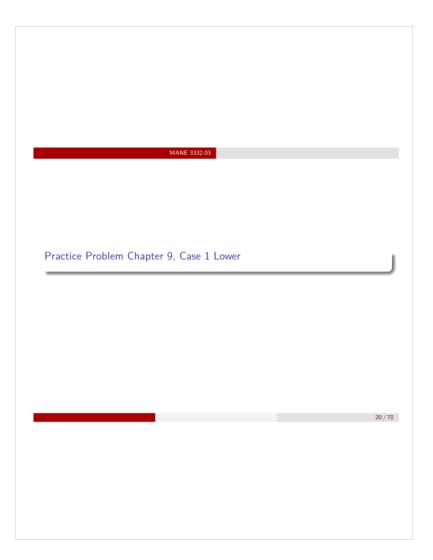
Region \( \pi = 0.05 \)

Region

Tet 20= 1.65, Grahion Reject Ho Tet 2 20=1,64, Grahiston: fail to reject)

Mm P- value







MANE 2222.02

Type II error and sample size for a two-tailed test

• Probability of type II error for the two-tailed test

$$\beta = \Phi \left( \mathbf{z}_{\alpha/2} - \frac{\delta \sqrt{n}}{\sigma} \right) - \Phi \left( -\mathbf{z}_{\alpha/2} - \frac{\delta \sqrt{n}}{\sigma} \right)$$

where  $\mu=\mu_0+\delta$ 

 $\bullet$  The sample to detect a difference between the true and hypothesized mean of  $\delta$  with power at least  $1-\beta$  is

$$n pprox rac{(z_{lpha/2} + z_{eta})^2 \sigma^2}{\delta^2}$$

where  $\delta = \mu - \mu_{\rm 0}$ 

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is nove; don't add to Note Carole

#### MANE 2222.0

Type II error and sample size for the one-tailed tests

• For an upper-tailed test

$$\beta = \Phi\left(z_{\alpha} - \frac{\delta\sqrt{n}}{\sigma}\right)$$

• For a lower-tailed test

$$\beta = 1 - \Phi\left(-z_{\alpha} - \frac{\delta\sqrt{n}}{\sigma}\right)$$

 $\bullet$  The sample size required to detect a difference between the true mean and hypothesized mean of  $\delta$  with power at least  $1-\beta$  is

$$n = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{\delta^2}$$

If n is not an integer, round up to the nearest integer

```
R: Chapter 9 Case 1 Hypothesis Testing

Z-test
library(BSDA)

## Loading required package: lattice

##

## Attaching package: 'BSDA'

## The following object is masked from 'package:datasets':

##

## Orange

z.test(x,alternative='greater',mu=2.5,sigma.x=0.66,conf.level=0.95)

##

## done-sample z-Test

##

## data: x

## z = 2.7104, p-value = 0.00336

## alternative hypothesis: true mean is greater than 2.5

## 95 percent confidence interval:

## 2.814503 NA

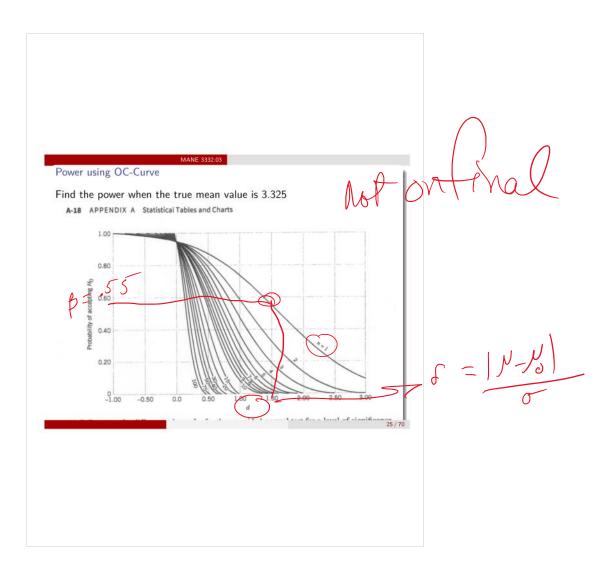
## sample estimates:

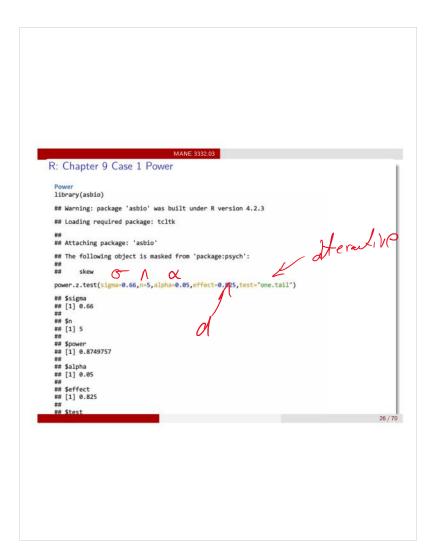
## mean of x

## mean of x

## 3.3
```

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	MANE 333	2.03	
Type II Error	Rate and Sample Siz	ze	
<ul><li>You mus</li></ul>	not be required to cont t understand the cont be II error		ity type
			27 /

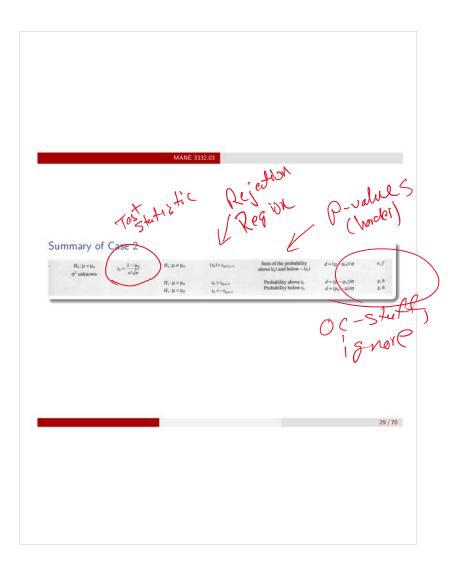
MANE 2222.01

# Chapter 9, Case 2

## Hypothesis Test on the Mean, Variance Unknown

- Much more common case than variance known
- $\bullet$  Substitute  ${\it S}$  for  $\sigma$
- ullet The test statistics is now a t random variable

$$T = \frac{\overline{X} - \mu_0}{S/\sqrt{n}}$$



#### Problem 9.3.6

- **9.3.6** An article in the ASCE Journal of Energy Engineering (1999, Vol. 125, pp. 59–75) describes a study of the thermal inertia properties of autoclaved aerated concrete used as a building material. Five samples of the material were tested in a structure, and the average interior temperatures (\*C) reported were as follows: 23.01, 22.22, 22.04, 22.62, and 22.59.
  - a. Test the hypotheses  $H_0$ :  $\mu = 22.5$  versus  $H_1$ :  $\mu \neq 22.5$ , using  $\alpha = 0.05$ . Find the *P*-value.
  - b. Check the assumption that interior temperature is normally distributed.
  - c. Compute the power of the test if the true mean interior temperature is as high as 22.75.
  - d. What sample size would be required to detect a true mean interior temperature as high as 22.75 if you wanted the power of the test to be at least 0.9?
  - e. Explain how the question in part (a) could be answered by constructing a two-sided confidence interval on the mean interior temperature.

9-5:4d Ho: N=22.5 HI: N7205

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Test Stolistic

$$t_0 = \frac{\overline{X} - V_0}{5/In}$$
 $= \frac{22.5 - 22.5}{.38/Is} = 0$ 

Reject Ho if

| to | > taxs,n-1

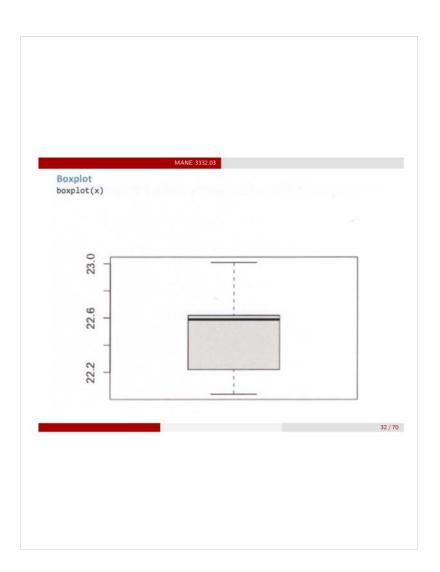
Use a = .05, need t.025,4 = 2.776

Conclusion: fail to reject to

Descriptive Statistic

x < - (23.01,22.22,12.04,27.62,22.59)
11brary(psych)
describe(x)

## vars n mean sd middian trimmed mad min max range skew kurtosis
se
## X1 1 5 22.5 0.38 22.59 22.5 0.55 22.04 23.01 0.97 0.08 -1.84
0.17

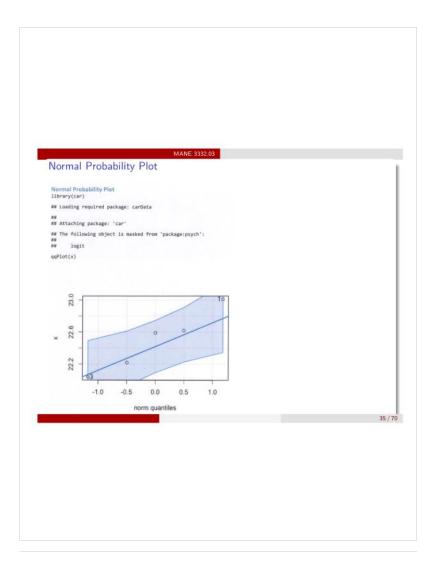




# Hypothesis Test Using R

```
t-test
t.test(x,alternative="two.sided",mu=22.5,conf.level=0.95)

##
## One Sample t-test
##
## data: x
## t = -0.023642, df = 4, p-value = 0.9823
## alternative hypothesis: true mean is not equal to 22.5
## 95 percent confidence interval:
## 22.02625 22.96575
## sample estimates:
## mean of x
## 22.496
```

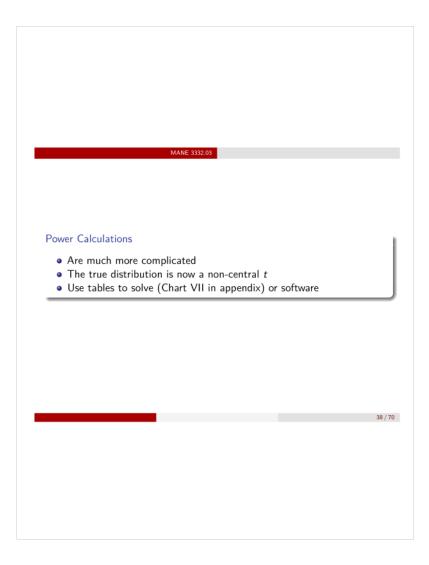


P-values

• More difficult to calculate since the t-tables only contain a few quantiles
• Can use tables to generate bounds on the p-value
• Software will provide p-values

### P-values from R

```
t-test
t.test(x,alternative="two.sided",mu=22.5,conf.level=0.95)
##
## One Sample t-test
##
## data: x
## t = -0.023642, df = 4, p-value = 0.9823
## alternative hypothesis: true mean is not equal to 22.5
## 95 percent confidence interval:
## 22.02625 22.96575
## sample estimates:
## mean of x
## 22.496
```



```
Power Calculation using R

Power
power.t.test(n=5,delta=0.25,sd=0.38,sig.level=0.05,type="two.sample")

##

##

Two-sample t test power calculation

##

##

delta = 0.25

##

sid = 0.38

##

sid.level = 0.05

##

power = 0.1491624

##

## NOTE: n is number in *each* group
```

```
Sample Size using R

Sample Size
power.t.test(power=0.9,delta=0.25,sd=0.38,sig.level=0.05,type="two.sample")

##

##

##

##

##

## 1wo-sample t test power calculation

##

##

## 0 = 49.53305

##

## sig.level = 0.05

##

## power = 0.9

##

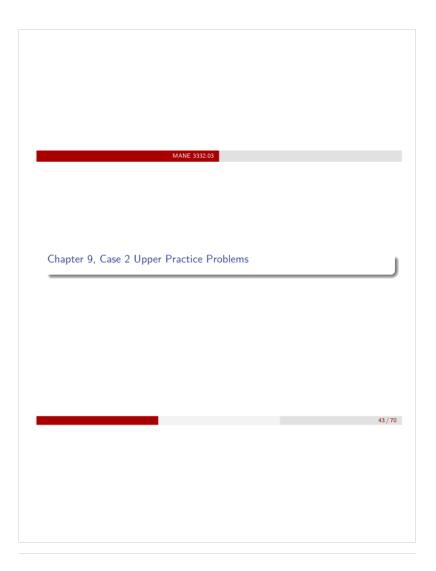
## alternative = two.sided

##

## NOTE: n is number in *each* group
```



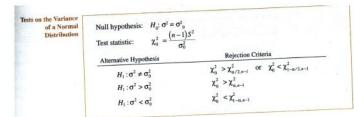




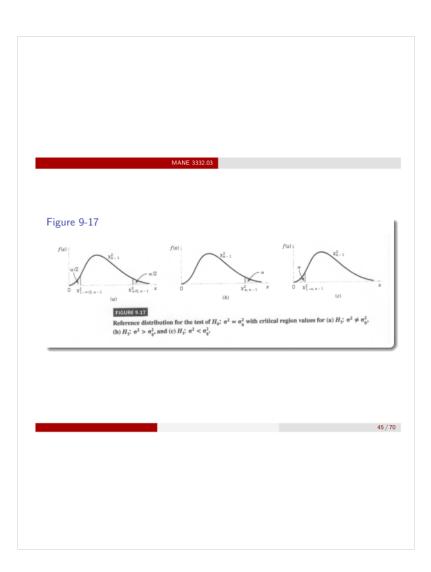
# Case 3. Hypothesis Test on Variance of Normal Population

 $\bullet$  The test statistics is a  $\chi^2$  random variable

$$\chi_0^2 = \frac{(n-1)S^2}{\sigma_0^2}$$



- The table below summarizes the three possible hypothesis tests. The rejection regions are clearly shown in Figure 9-17 on page 222





#### Problem 7.108

Problem taken from Ostle, Turner, Hicks and McElrath (1996). Engineering Statistics: The Industrial Experience. Duxbury Press.

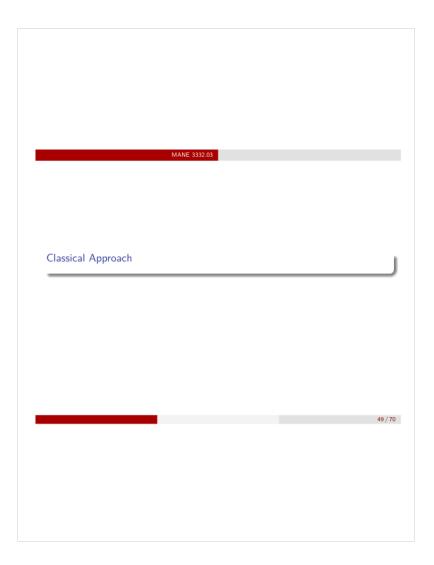
7.108 Incoming coal at a coking plant is routinely analyzed for sulfur content (in percent). In the past, samples taken from barges loaded with coal from a particular mine have had a variance of 0.000196. When a new analyst was hired, the results of an assay of coal from the mine produced percentages of 0.83, 0.79, 0.77, 0.81, and 0.80.
(a) Using α = 0.05, does the sample variance provide sufficient evidence to conclude that the results from the new analyst indicate more variability than in the past? State all assumptions.
(b) Based on these data, is an assumption of normality reasonable? Justify by using a normal quantile plot and a formal test such as the Shapiro-Wilk W test.

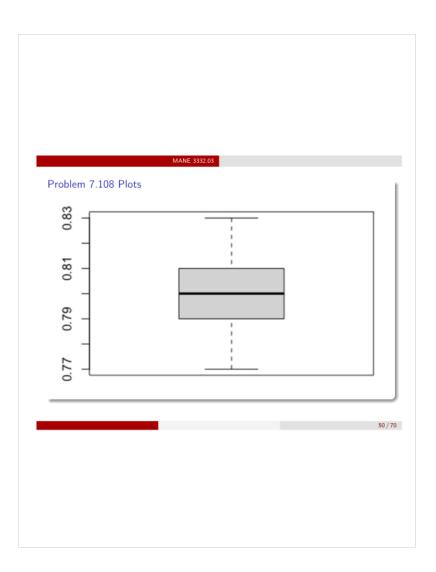
Statistics for Problem 7.108

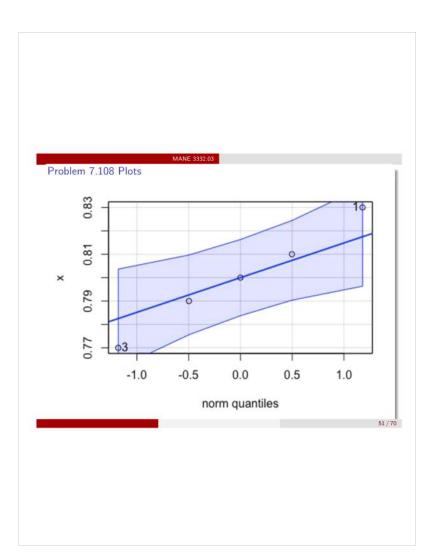
x<-c(0.83,0.79,0.77,0.81,0.80)
1lbrary(psych)
describe(x)

## vars n mean sd median trimmed mad min max range skew kurtosis se
## X1 15 0.8 0.02 0.8 0.8 0.8 0.01 0.77 0.83 0.06 0 -1.69 0.01
print(var(x))

## [1] 5e-04







```
Problem 7.108 Shapiro-Wilks Test

## [1] 3 1

shapiro.test(x)

##

## Shapiro-Wilk normality test

##

## data: x

## W = 0.99929, p-value = 0.9998
```

p-values

• Very similar to the case for the mean of a normal population with variance unknown

• Difficult to calculate since the  $\chi^2$ -tables only contain a few quantiles

• Can use tables to generate bounds on the p-value

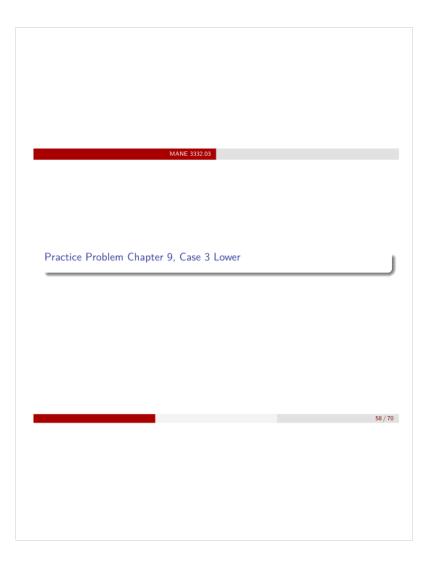
• Software will provide p-values

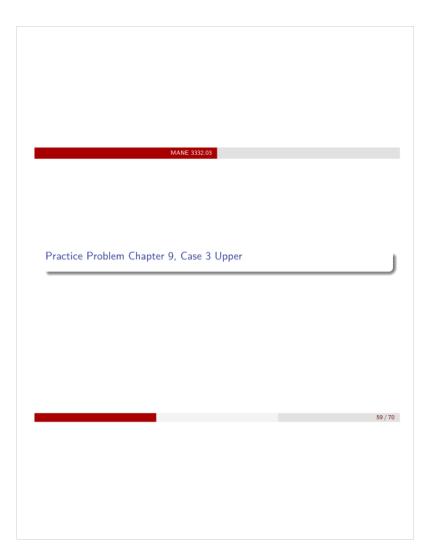
```
Test on Variance using R (EnvStats)
varTest(x,alternative="greater",conf.level=0.95,sigma.squared=0.000196)
## Results of Hypothesis Test
## ------
##
## Null Hypothesis:
##
## Alternative Hypothesis:
                                       variance = 0.000196
                                       True variance is greater than 0.000196
##
## Test Name:
##
                                          Chi-Squared Test on Variance
## Estimated Parameter(s):
##
## Data:
                                          variance = 5e-04
                                          Chi-Squared = 10.20408
## Test Statistic:
##
## Test Statistic Parameter:
                                          df = 4
                                          0.03712675
## P-value:
                                          LCL = 0.0002107986
UCL = Inf
 ## 95% Confidence Interval:
                                                                                       54/70
```







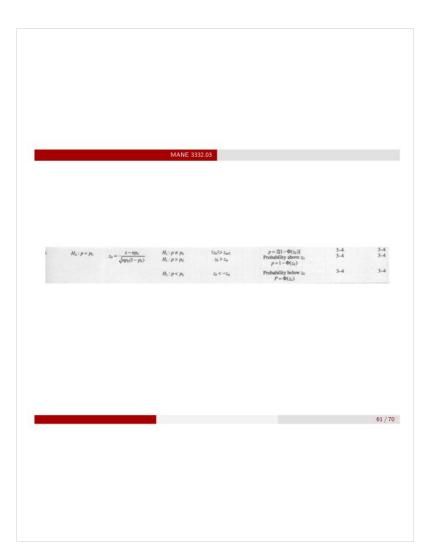




# Case 4. Hypothesis Test on a Population Proportion

• The test statistics for the hypothesis test is

$$Z_0 = \frac{x - np_0}{\sqrt{np_0(1 - p_0)}}$$



Problem 9.5.2

9.5.2 Problem 9.5.2

a. Test the hypothesis  $H_0$ : p = 0.9 against  $H_1$ :  $p \neq 0.9$  at  $\alpha = 0.05$ . Find the P-value.

b. Explain how the question in part (a) could be answered by constructing a 95% two-sided confidence interval for p.



### Power Calculations

• For the two-sided alternative hypothesis

$$\beta = \Phi\left(\frac{p_0 - p + z_{\alpha/2}\sqrt{p_0(1 - p_0)/n}}{\sqrt{p(1 - p)/n}}\right) \\ -\Phi\left(\frac{p_0 - p - z_{\alpha/2}\sqrt{p_0(1 - p_0)/n}}{\sqrt{p(1 - p)/n}}\right)$$

• If the alternative is  $H_1: p < p_0$ 

$$\beta = 1 - \Phi\left(\frac{\rho_0 - \rho - z_\alpha \sqrt{\rho_0(1-\rho_0)/n}}{\sqrt{\rho(1-\rho)/n}}\right)$$

ullet and finally if the alternative hypothesis is  $H_1: p>p_0$ 

$$\beta = \Phi\left(\frac{\rho_0 - \rho + z_\alpha \sqrt{\rho_0(1 - \rho_0)/n}}{\sqrt{\rho(1 - \rho)/n}}\right)$$

### Sample Size

 $\bullet$  Sample size requirements to satisfy type  ${\rm II}(\beta)$  error constraints for a two-tailed hypothesis test is given by

$$n = \left[\frac{z_{\alpha/2}\sqrt{p_0(1-p_0)} + z_\beta\sqrt{p(1-p)}}{p-p_0}\right]^2.$$

- $\bullet$  For a sample size for a one-sided test substitute  $\emph{z}_{\alpha}$  for  $\emph{z}_{\alpha/2}.$
- Problem 9.95

## Testing for Goodness of Fit

- $\bullet$  Material is presented in section 9-7 of your textbook
- Procedure determines if the sample data is from a specified underlying distribution
- $\bullet$  Procedure uses a  $\chi^2$  distribution
- $\bullet$  Example 9-12 presents a  $\chi^2$  goodness of fit test for a Poisson example
- $\bullet$  Example 9-13 presents a  $\chi^2$  goodness of fit test for a normal example

#### Procedure

- $lackbox{0}$  Collect a random sample of size n from a population with an unknown distribution,
- Arrange the n observations in a frequency distribution containing k classes
- $\odot$  Calculate the observed frequency in each class  $O_i$ ,
- From the hypothesized distribution, calculate the expected frequency in class i, denoted  $E_i$  (if  $E_i$  is small combine classes)
- Calculate the test statistic

$$\chi_0^2 = \frac{\sum_{i=1}^k (O_i - E_i)^2}{E_i}$$

• Reject the null hypothesis if the calculated value of the test statistic  $\chi_0^2 > \chi_{\alpha,k-\rho-1}^2$  where  $\rho$  is the number of parameters in the hypothesized distribution

### Example 9.12, part 1

### EXAMPLE 9.12 | Printed Circuit Board Defects—

Poisson Distribution
The number of defects in printed circuit boards is hypothesized to follow a Poisson distribution. A random sample of n=60 printed circuit boards has been collected, and the following number of defects observed.

Number of Defects	Observed Frequency
0	32
1	15
2	9
3	4

The mean of the assumed Poisson distribution in this example is unknown and must be estimated from the sample data. The

estimate of the mean number of defects per board is the sample average, that is,  $(32\cdot0+15\cdot1+9\cdot2+4\cdot3)/60=0.75$ . From the Poisson distribution with parameter 0.75, we may compute  $p_i$ , the theoretical, hypothesized probability associated with the fit class interval corresponds to a particular number of defects, we may find the  $p_i$  as follows:

$$p_1 = P(X = 0) = \frac{e^{-0.75}(0.75)^0}{0!} = 0.472$$

$$p_2 = P(X = 1) = \frac{e^{-0.75}(0.75)^1}{1!} = 0.354$$

$$p_3 = P(X = 2) = \frac{e^{-0.75}(0.75)^2}{2!} = 0.133$$

$$p_4=P(X\geq 3)=1-(p_1+p_2+p_3)=0.041$$

#### Example 9.12, part 2

The expected frequencies are computed by multiplying the sample size n=60 times the probabilities  $p_i$ . That is,  $E_i=np_i$ . The expected frequencies follow:

2. Null hypothesis:  $H_0$ : The form of the distribution of defects is Poisson.

3. Alternative hypothesis:  $H_i$ : The form of the distribution of the distribution

Number of Defects	Probability	Expected Frequency
0	0.472	28.32
1	0.354	21.24
2	0.133	7.98
3 (or more)	0.041	2.46

Because the expected frequency in the last cell is less than 3, we combine the last two cells:

6. Computations:

Number of Defects	Observed Frequency	Expected Frequency
0	32	28.32
1	15	21.24
2 (or more)	13	10.44

The seven-step hypothesis-testing procedure may now be applied, using  $\alpha=0.05,$  as follows:

Parameter of interest: The variable of interest is the form of the distribution of defects in printed circuit boards.

- Alternative hypothesis: H<sub>1</sub>: The form of the distri-bution of defects is not Poisson.
- button of defects is not Poisson.

  4. Test statistic: The test statistic is  $\chi_0^2 = \sum_{i=1}^4 \frac{(O_i E_i)^2}{E_i}$ 5. Reject  $H_0$  iff: Because the mean of the Poisson distribution was estimated, the preceding chi-square statistic will have k p 1 = 3 1 = 1 degree of freedom. Consider whether the P-value is less than 0.05.

$$\begin{matrix} \chi_0^2 = \frac{(32-28.32)^2}{28.32} + \frac{(15-21.24)^2}{21.24} + \frac{(13-10.44)^2}{10.44} \\ = 2.94 \end{matrix}$$

= 2.94
— Conclusions: We find from Appendix Table III that Z<sup>0</sup><sub>0.10.1</sub> = 2.71 and X<sup>0</sup><sub>0.05.1</sub> = 3.34. Because χ<sup>0</sup><sub>0</sub> = 2.94 lies between these values, we conclude that the P-value is between 0.05 and 0.10. Therefore, because the P-value exceeds 0.05, we are unable to reject the null hypothesis that the distribution of defects in printed circuit boards is Poisson. The exact P-value computed from software is 0.0864.

You should be prepared to work any practice problems assigned: Cases 1-3 with three different alternatives
 All other information is conceptual knowledge that can be questioned with multiple choice
 Name 3 ways to test if data is from a normal distribution

### One-sided example

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H. . N>2.5 20-2.71

P- Julye = P(Z>Z) = 1- 1(2.71) = 1 - .996636 = .003364

If p-value < a, Reject Ho ? p-value = .008367 Else fail to reject Ho

Is p-value L x? Yes -> Reject

# Chapter 9 case 1 lower

Thursday, April 17, 2025 11:43 AM

**QUESTION 1** 

HO. N= 12 H: N212

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=12.0 versus mu less than 12.0 using alpha=0.1. The sample statistics are n=21, xbar=11.11, sigma=2.331.

O z0=1.7497

O z0=-8.018

z0=-1.7497

z0=-3.4397

 $\frac{20-\frac{x-y_0}{x-y_0}}{\sqrt{x}} = \frac{11.11-12}{2331/\sqrt{21}} = -1.74967 = 21$  = -1.74967 = 21 = -1.11 = -1.11

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## Ch9, Case 1 Lower

Thursday, April 17, 2025 11:48 AM

0				

Construct the rejection region for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=32.0 versus mu less than 32.0 using alpha=0.005. The sample statistics are n=20, xbar=32.11, sigma=2.972.

O Reject Ho if Z0<-2.807

O Reject H0 if z0>2.576

O Reject Ho if |z0|>2.807

Reject H0 if z0<-2.576

Reject +0 if -2a = -2.005 = -2.576

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## Ch 9, Case 1 Lower

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#### **QUESTION 5**

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=12.0 versus mu less than 12.0 using alpha=0.0025. The sample statistics are n=11, xbar=11.61, sigma=1.067. The value of 20 is -1.2123 and the rejection region is reject H0 if 20 < 2.807

○ Fail to reject H<sup>O</sup>

○ Reject H0

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2807 20=-1213

is -1.213 in rejection Repion? No conclusion — Tail to reject to

### Ch9, Case 1 Lower

Thursday, April 17, 2025 11:54 AM

### **QUESTION 7**

Find the p-value for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=32.0 versus mu less than 32.0 using alpha=0.001. The sample statistics are n=29, xbar=31.1, sigma=3.849 and the value of the test statistic, Z0, is -1.2592.

p value=0.207669

O p-value=0.103835

O p-value=0.896165

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Q-value =  $\Phi(z_0) = \Phi(-1.2592)$ =  $\Phi(-1.26)$ 

\_ #8 .103835

### Ch9, Case 1 Lower

Thursday, April 17, 2025 11:57 AM

#### **QUESTION 9**

Using the p-value from a test of hypothesis for the mean of single sample with variance known, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test include z0=-1.7295 and p-value=0.04186.

Reject H0

Fail to reject H0

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E/See

Facill to reject H0

Control Of the hypothesis test. The null hypothesis test. The null hypothesis test include z0=-1.7295 and p-value=0.04186.

Fail to reject H0

Control Of the hypothesis for the mean of single sample with variance known, determine the correct conclusion for the hypothesis test. The null hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test. The null hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test. The null hypothesis test. The null hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test. The null hypothesis t

p-value = .04/86 = .01 is .02186<.01? No -> fail to reject Ho

# Chapter 9, Case 2 2-sided

Tuesday, April 22, 2025 11:31 AM

QUESTION 1

Ho. N=. S

Ho. N=. S

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=0.5 versus mu not equal to 0.5 using alpha=0.001. The sample statistics are n=18, xbar=0.51, S=0.051.

O t0=69.2042

O t0=3.5294

○ t0=0.8319 O t0=-0.8319

 $t_0 = \frac{\bar{x} - N_0}{s/on} = \frac{s/-.s}{0s/\sqrt{s}}$ 

= 0.83189

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### Chapter 9, Case 2 2-sided

Tuesday, April 22, 2025 11:34 AM

#### QUESTION 3

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknow	n. The null hypothesis is mu=18.5 versus mu not equal
to 18.5 using alpha=0.02. The sample statistics are n=20, xbar=19.35, S=4.813.	

O Reject H0 if |t0|>2.539

O Reject H0 if |t0|>2.205 Reject Ho if t0<-2.205

Reject Ho if  $1 \pm 01 > \pm 0.01, 19 = 2.53$ 

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#### **QUESTION 5**

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=25.8 versus mu not equal to 25.8 using alpha=0.01. The sample statistics are n=26, x bar=30.28, x =5.3. The value of t0 is 4.3101 and the rejection region is reject HO if |t0| > 2.787

Fail to reject H0

O Reject H0

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to = 41.3101

 $RR: |t_0| > 2.787$   $TS \quad 4.3101 > 2.787$  ARRIVED AREJECT AREA AREJECT AREJE

### Chapter 9, Case 2 2-sided

Tuesday, April 22, 2025 11:39 AM

#### **QUESTION 7**

Using the p-value from a test of hypothesis for the mean of single sample with variance unknown, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=0.5 versus mu not equal to 0.5 using alpha=0.1. The sample statistics are n=7, xbar=0.52, S=0.038. The results of hypothesis test include t0=1.3925 and p-value=0.213186.

O Reject H0 ○ Fail to reject H0

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P-value = .213

D-value = . or .

d = . 1

Is . 213< . 1? No -> fail to
Reject Ho

### Chapter 9, Case 2 upper

Tuesday, April 22, 2025 11:42 AM

**QUESTION 1** 

Hb: N=132.3 H,: N>132.3

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=132.3 versus mu greater than 132.3 using alpha=0.0025. The sample statistics are n=24, xbar=139.02, S=20.204.

O t0=1.6294 O t0=-1.6294

O t0=0.3951

O t0=7.9826

 $t_{0} = \frac{X - N_{0}}{S/In} = \frac{139.02 - 132.3}{20204/\sqrt{224}}$  = 1.6294

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## Chapter 9, Case 2 Upper

Tuesday, April 22, 2025 11:47 AM

Rejection Region is Hed H,

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=18.5 versus mu greater than 18.5 using alpha=0.05. The sample statistics are puts, xbar=T9.72, S=3.905.

Reject Ho if t0<-1.761

- O Reject Ho if t0<-2.145
- O Reject Ho if |t0|>2.145
- O Reject H0 if t0>1.761

QUESTION 3

O Reject H0 if |t0|>1.761

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## Chapter 9, Case 2 Upper

Tuesday, April 22, 2025 11:50 AM

#### **QUESTION 5**

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=12.0 versus mu greater than 12.0 using alpha=0.05. The sample statistics are n=20, xbar=12.2, S=1.928. The value of t0 is 0.4639 and the rejection region is reject HO if t0>1.729

Reject H0
Fail to reject H0
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to-0.4639 Rejul Ho if to> 1.729

> is .4637 > 1.729? No -> fail to reject

## Chapter 9, Case 2 Upper

Tuesday, April 22, 2025 11:51 AM

#### **QUESTION 7**

Using the p-value from a test of hypothesis for the mean of single sample with variance unknown, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=132.3 versus mu greater than 132.3 using alpha=5.0E-4. The sample statistics are n=18, xbar=139.18, S=24.068. The results of hypothesis test include t0= 1.2128 and p-value=0.241791.

O Reject H0

Fail to reject H0

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.5 E -3 .05 E -2 .005 E -1

15 Prome < a 22/18 < .0005 ? No. feel to Reject Ho

Chapter 9 Page 82

Chapter 9, case 2 lower Tuesday, April 22, 2025 11:55 AM	Poel trog ramming	
QUESTION 1  Calculate the test statistic for a test of hypothesi using alpha=0.001. The sample statistics are n=2 t0=0.0 t0=0.0	for the mean of single sample with variance unknown. The null hypothesis is mu=0.5 versus mu less the start of the start o	nan 0.5
t0=0.0 t0=0.0 Screen clipping taken: 4/22/2025 11:57 AM	to= X-10 = .55 = C	එ. උ

## Chapter 9, Case 2 Lower

Tuesday, April 22, 2025 11:59 AM

H, ; K, K,

H,:NL 12

### **QUESTION 3**

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=12.0 versus mu less than 12.0 using alpha=0.01. The sample statistics are n=6, xbar=11.79, S=2.19.

- O Reject Ho if |t0|>4.032
- O Reject Ho if t0>3.365
- Reject H0 if t0<-3.365
  - O Reject H0 if |t0|>3.365
  - O Reject Ho if t0<-4.032

Reject Ho if tox -tainy = -t.oiss

= - 3.365

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## Chapter 9, Case 2 Lower

Tuesday, April 22, 2025 12:01 PM

### **QUESTION 5**

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=25.8 versus mu less than 25.8 using alpha=0.1. The sample statistics are n=5, xbar=16.98, S=6.924. The value of t0 is -2.8484 and the rejection region is reject HO if t0<-1.533

Screen clipping taking 40/2025 12:02 pm Reject HO if  $t_0 < -1.533$ is -2.8484 < -1.533 /os, Reject HO +0 = -3.8484

## Chapter 9, Case 2 Lower

Tuesday, April 22, 2025 12:04 PM

#### **QUESTION 7**

Using the p-value from a test of hypothesis for the mean of single sample with variance unknown, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.025. The sample statistics are n=7, xbar=15.44, S=5.429. The results of hypothesis test include t<del>0= -1.4913 and p-</del>value=0.186478.

Fail to reject H0

O Reject H0

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Q = .025 P-value = .1865

is p-value < x?

15.1865<.025? No -> fail to Reject Ho Attendance /- C