

Overview of Statistical Hypotheses

- Many engineering problems require a decision to be made regarding some statement about a parameter
 - The statement is called a **hypothesis**
 - The decision-making process about the hypothesis is call hypothesis testing
- Statistical hypothesis testing is usually the data analysis stage of a comparative experiment
- A procedure leading to a decision about a particular hypothesis is called a test of hypothesis
- Testing the hypothesis involves taking a random sample, computing a test statistic from the sample data and then using the to make a decision

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Statistical Hypothesis

- A statistical hypothesis is a statement about the parameters of one or more populations
- A statistical hypothesis has two parts a null hypothesis (denoted H₀) and an alternative hypothesis (denoted H₁)
 - The null hypothesis contains an equality statement about the value of parameter. For example H₀: μ = 12 ounces.
 - parameter. For example $H_0: \mu=12$ ounces. • There are three possible alternative hypotheses: $H_1: \mu \neq 12$, $H_1: \mu < 12$, or $H_1: \mu > 12$
 - The goal of the research will determine the appropriate alternative hypothesis

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Mull hypothosis

Ho; parameter = value

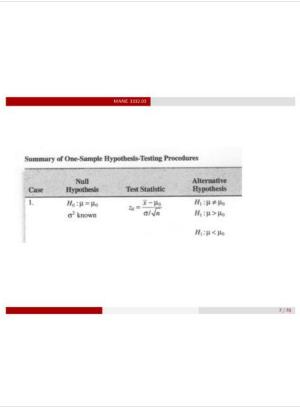
Atternative Hypothesis

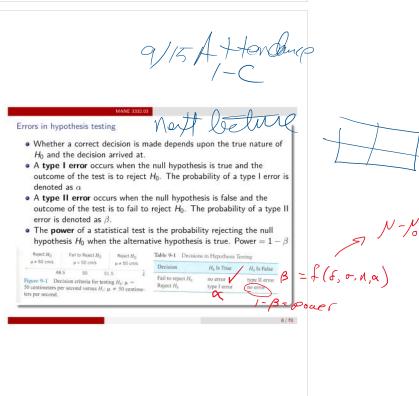
H, or Ha

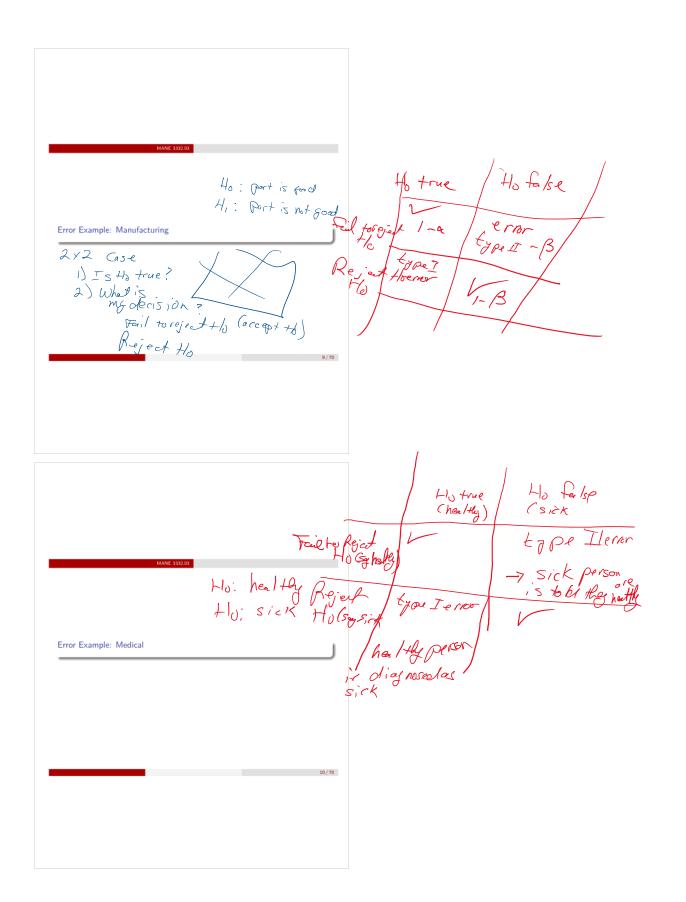
L); N>12 (upper one-sided)

A; N<12 (lower one-sided)

H; N≠12 (two-sided or two-tailed)







with fixed rejusion region

General Procedure for Hypothesis Testing

The following sequence of steps is recommended

- From the problem context, identify the parameter of interest,

 State the null hypothesis, H_0 , $h_0 v_0 e = s_0 f_0$,

 Specify an appropriate alternative hypothesis, $H_1, g_1 g_2$, $g_0 g_2$, g

- State the rejection region for the (test) statistic,
- O Compute any necessary sample quantities, substitute these into the equation for the test statistics, and compute that value,
- O Decide whether or not H₀ should be rejected and report in the problem context

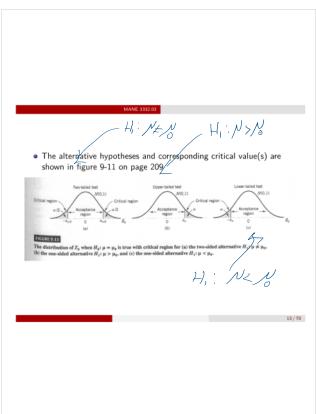
Chapter 9, Case 1

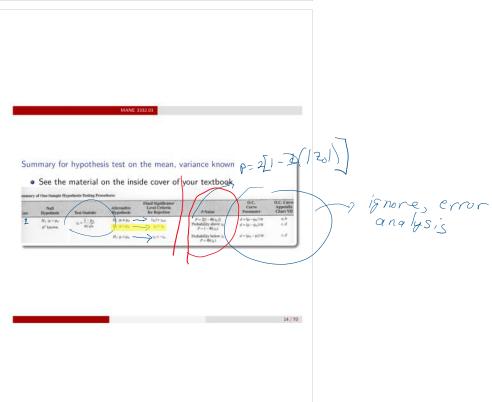
Inference on the Mean of a population, variance known

- Assumptions:
 - X_1, X_2, \dots, X_n is a random sample of size n from a population
 - The population is normal, or if it is not normal, the conditions of the central limit theorem apply (a s < Somple n > 30)
- The parameter of interest is μ The null hypothesis is $H_0: \mu = \mu_0$ $\sqrt{a}/\mu e$ or run her
- The test statistic is

and has a standard normal distribution

Recall Chapter 8, Gse 1 x-200 m < No x+2 m





Problem 1

Example 11-1

The burning rate of a rocket propellant is being studied. Specifications require that the mean burning rate must be 40 cm/s. Furthermore, suppose that we know that the standard deviation of the burning rate is approximately 2 cm/s. The experimenter decides to specify a type Γ error probability $\alpha = 0.05$, and he will base the test on a random sample of size n = 25. The hypotheses we wish to test are

 H_0 : $\mu = 40$ cm/s, H_1 : $\mu \neq 40$ cm/s.

Twenty-five specimens are tested, and the sample mean burning rate obtained is $\bar{x} = 41.25$ cm/s.

Source: Himes. Mortgomery, Goodsman, Bornor (2003). Prebability and Statistics in Engineering, 4th ad.

Rejection Region

Hi: N+ 40 (two-to, ked tast)

Know X = .05, 0 -2, 1-25,

@ Test Statistic $Z_0 = \frac{\overline{X} - I_0}{0 / v_R} = \frac{41.25 - 40}{2 / v_{\overline{2}5}}$

= 3.125 3) Reject Riegion (H,) Reject Ho if

1201> Zaz = Z.05/2

= 1.96 a) Conclusion: Since 13.125/2 1.96, we rejed to 7 we found

evidence tool the man burn rate is not 40cm/s

45'. N=2.5 H.: 12 2.5

9.2.10 The bacterial strain Acinetobacter has been tested for its adhesion properties. A sample of five measurements gave readings of 2.69, 5.76, 2.67, 1.62 and 4.12 dyne-cm². Assume that the standard deviation is known to be 0.66 dyne-cm² and that the scientists are interested in high adhesion (at least 2.5 dyne-cm²).

a. Should the alternative hypothesis be one-sided or

two-sided?

b. Test the hypothesis that the mean adhesion is 2.5 dyne-cm².

c. What is the *P*-value of the test statistic?

Summary Statistics
x<-c(2.69,5.76,2.67,1.26,4.12)
library(psych)
vars n mean
X1 1 5 3.3,1/71 2.69 3.3 2.12 1.26 5.76 4.5 0.26 -1.71 0.76

① Tost Statistic $\overline{X} = 3.3$ $\overline{X} = \frac{\overline{X} - 1/6}{000}$ N = 5= 33-25 = 2.7/04 BRejection Region Right Ho if Zo>Zx Set x = .05 Reject Ho If ZoA Zog-Zog = 1645

A) Gre bision: Reject Ho

Connection between Hypothesis Tests and CI

- There is a close connection between confidence intervals and hypothesis tests
- stest confidence interval/hourd

 is the acceptance
 Region

 if you are not in

 the confidence interval/

 bound, you are interval

 Rejection Repion ullet Consider a 100(1 - lpha)% confidence interval on μ and a hypothesis test of size α shown below

$$H_0 : \mu = \mu_0$$

 $H_1 : \mu \neq \mu_0$

- ullet The conclusion to reject H_0 will be reached if μ_0 is not contained within the confidence interval
- If μ₀ is within the confidence interval, we fail to reject H₀
- \bullet The 100(1 $\alpha)\%$ confidence interval on μ is the acceptance region

P-values

- . Is a widely used alternative to the traditional hypothesis test
- Definition: The p-value is the smallest level of significance that would lead to reject of the null hypothesis H_0 with the given data
- Formulas are given below

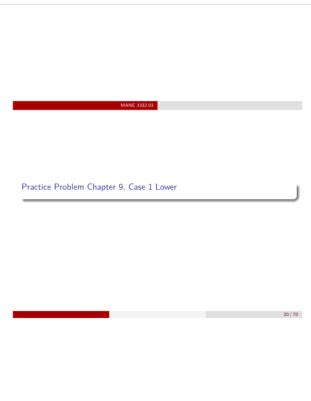
$$P = \left\{ \begin{array}{ll} 2[1-\Phi(|z_0|)] & \text{for a two-tailed test} \\ 1-\Phi(z_0) & \text{for a upper-tailed test} \\ \Phi(z_0) & \text{for a lower-tailed test} \end{array} \right.$$

ullet Usage: if p-value<lpha then the conclusion is reject H0, otherwise fail to reject H0

Tot I Zo= 1.65, Gorbsion Reject Ho Tota Zo=1.64, Grelson: fail to reject)

Man P- value





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Practice Problem Chapter 9, Case 1 Upper

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Type II error and sample size for a two-tailed test

• Probability of type II error for the two-tailed test

$$\beta = \Phi \left(z_{\alpha/2} - \frac{\delta \sqrt{n}}{\sigma} \right) - \Phi \left(-z_{\alpha/2} - \frac{\delta \sqrt{n}}{\sigma} \right)$$

where $\mu=\mu_0+\delta$

• The sample to detect a difference between the true and hypothesized mean of δ with power at least $1-\beta$ is

$$n \approx \frac{(z_{\alpha/2} + z_{\beta})^2 \sigma^2}{\delta^2}$$

where $\delta = \mu - \mu_0$

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is rore; don't add to Note Carcle

Type II error and sample size for the one-tailed tests

For an upper-tailed test

$$\beta = \Phi\left(z_{\alpha} - \frac{\delta\sqrt{n}}{\sigma}\right)$$

• For a lower-tailed test

$$\beta = 1 - \Phi\left(-z_{\alpha} - \frac{\delta\sqrt{n}}{\sigma}\right)$$

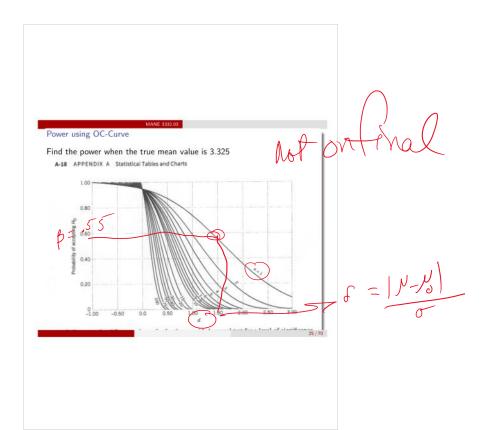
 \bullet The sample size required to detect a difference between the true mean and hypothesized mean of δ with power at least $1-\beta$ is

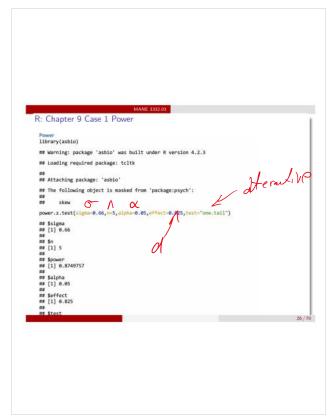
$$n = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{\delta^2}$$

If n is not an integer, round up to the nearest integer

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R: Chapter 9 Case 1 Hypothesis Testing Z-test library(BSDA) ## Loading required package: lattice ## ## Attaching package: 'BSDA' ## The following object is masked from 'package:datasets': ## ## Orange z.test(x,alternative='greater',mu=2.5,sigma.x=0.66,conf.level=0.95) ## ## One-sample z-Test ## ## z = 2.7164, p-value = 0.00336 ## ## z = 2.7164, p-value = 0.00336 ## ## ps percent confidence interval: ## 95 percent confidence interval: ## 5.314563 NA ## sample estimates: ## mean of x ## 3.3





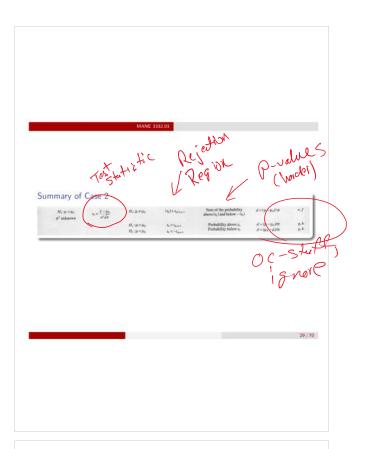
Type II Error Rate and Sample Size You will not be required to calculate or use OC-curves
 You must understand the concept and be able to correctly identity type I and type II error

Chapter 9, Case 2

Hypothesis Test on the Mean, Variance Unknown

- Much more common case than variance known
- Substitute S for σ
 The test statistics is now a t random variable

$$T = \frac{\overline{X} - \mu_0}{S/\sqrt{n}}$$



Problem 9.3.6

9.3.6 An article in the ASCE Journal of Energy Engineering (1999, Vol. 125, pp. 59–75) describes a study of the thermal inertia properties of autoclaved aerated concrete used as a building material. Five samples of the material were tested in a structure, and the average interior temperatures (*C) reported were as follows: 23.01, 22.22, 22.04, 22.62, and 22.59.

- a. Test the hypotheses H_0 : $\mu=22.5$ versus H_1 : $\mu\neq22.5$, using $\alpha=0.05$. Find the P-value. b. Check the assumption that interior temperature is nor-
- mally distributed.
- mally distributed.

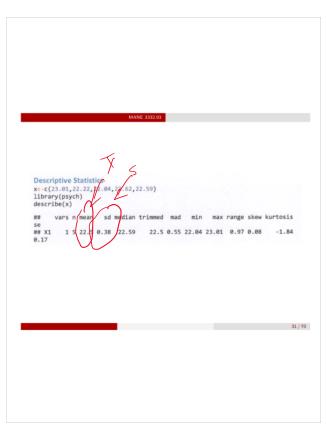
 c. Compute the power of the test if the true mean interior temperature is as high as 22.75.

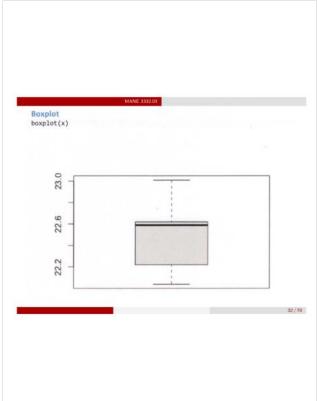
 d. What sample size would be required to detect a true mean intesior temperature as high as 22.75 if you wanted the power of the test to be at least 0.9?
- e. Explain how the question in part (a) could be answered by constructing a two-sided confidence interval on the mean interior temperature.

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 $=\frac{22.5-22.5}{38/1=}=0$

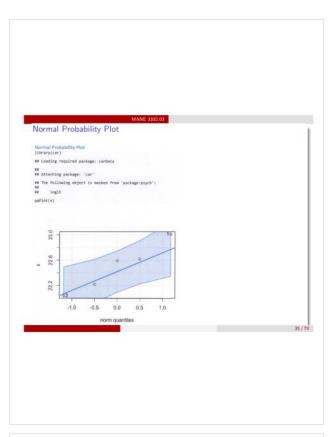
Reject Ho if Use a = .05, need £.025,4 = 2.776 Conclusion: fail to reject the





```
Classical Approach
```







```
P-values from R

t-test
t.test(x,alternative="two.sided",mu=22.5,conf.level=0.95)

##
## One Sample t-test
## data: x
## t = -0.023642, df = 4, p-value = 0.9823
## alternative hypothesis: true mean is not equal to 22.5
## 92.02625 22.96575
## sample estimates:
## mean of x
## 22.496
```

Power Calculations

• Are much more complicated

• The true distribution is now a non-central t

• Use tables to solve (Chart VII in appendix) or software

```
Power Calculation using R

Power

power.t.test(n=5,delta=0.25,sd=0.38,sig_level=0.05,type="two.sample")

##

##

Two-sample t test power calculation

##

##

delta = 0.25

##

sig_level = 0.05

##

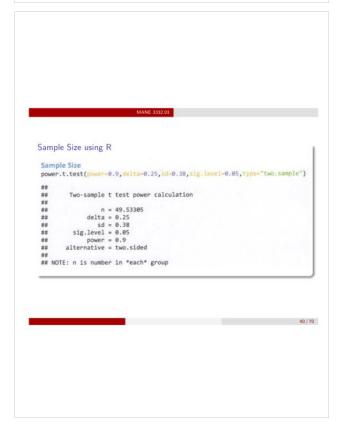
power = 0.1491624

##

## alternative = two.sided

##

## NOTE: n is number in *each* group
```







Chapter 9, Case 2 Upper Practice Problems

Chapter 9, Cases 1\$2

test statistic = 0.0 > 43ero options

Case 3. Hypothesis Test on Variance of Normal Population

ullet The test statistics is a χ^2 random variable

$$\chi_0^2 = \frac{(n-1)S^2}{\sigma_0^2}$$

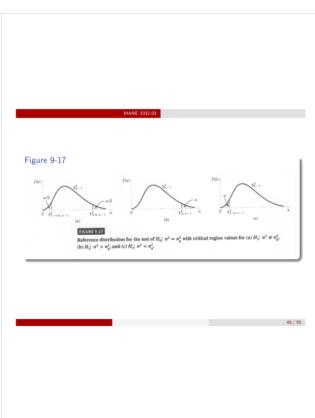
- The table below summarizes the three possible hypothesis tests. The rejection regions are clearly shown in Figure 9-17 on page 222 $\,$

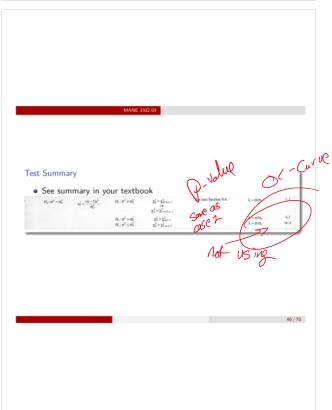
-7 what if I wanted a test
on Starchardcheviation

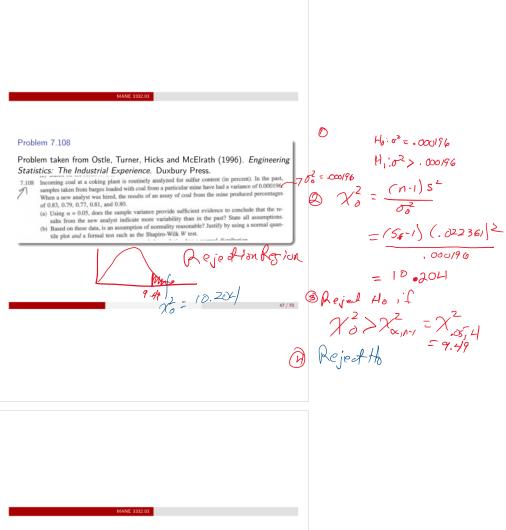
Ho: o = 50

H, i o ≠ 50

Yuse Xo from variance test







Statistics for Problem 7.108

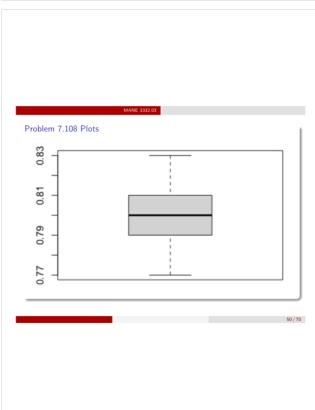
x<-c(0.83,0.79,0.77,0.81,0.80)
library(psych)
describe(x)

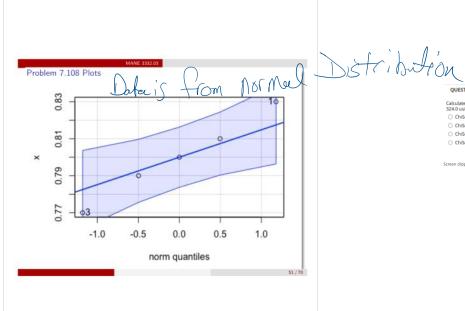
vars n mean sd median trimmed mad min max range skew kurtosis se
x1 15 0.8 0.02 0.8 0.8 0.01 0.77 0.83 0.06 0 -1.69 0.01

print(var(x))

[1] 5e-04







Problem 7.108 Shapiro-Wilks Test ## [1] 3 1 shapiro.test(x) ## ## Shapiro-Wilk normality test ## ## data: x ## W = 0.99929, p-value = 0.9998 52 / 70

QUESTION 1

Calculate the test statistic for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma*2=324.0 versus sigma*2 not equal to 324.0 using alpha+0.2. The sample statistics are n=28, xbar=126.28, 5=50.933.

C InSiguared0~216.1809

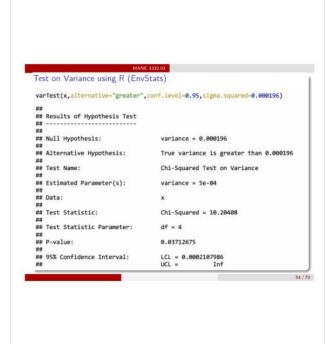
- ChiSquared0=3.3722
 ChiSquared0=9.5419

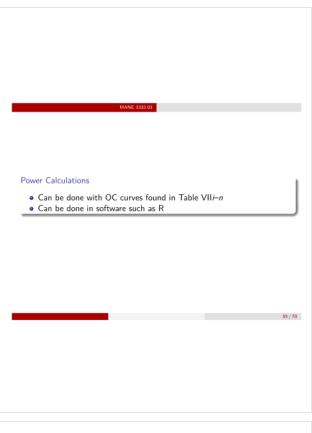
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p-values

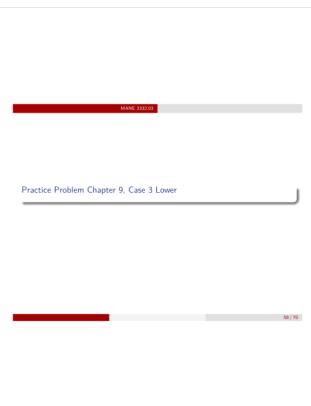
- Very similar to the case for the mean of a normal population with variance unknown
- \bullet Difficult to calculate since the $\chi^2\text{-tables}$ only contain a few quantiles
- Can use tables to generate bounds on the p-value
- Software will provide p-values











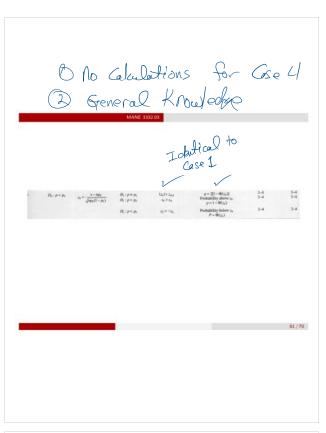


Case 4. Hypothesis Test on a Population Proportion

Prombinary

Using Mornary

• The test statistics for the hypothesis test is $Z_0 = \frac{x - np_0}{\sqrt{np_0(1-p_0)}}$





Problem 9.5.2 Classic Approach

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Power Calculations

• For the two-sided alternative hypothesis

$$\begin{split} \beta = & \quad \Phi\left(\frac{p_0-\rho+z_{\alpha/2}\sqrt{p_0(1-p_0)/n}}{\sqrt{\rho(1-\rho)/n}}\right) \\ & \quad -\Phi\left(\frac{p_0-\rho-z_{\alpha/2}\sqrt{p_0(1-p_0)/n}}{\sqrt{\rho(1-\rho)/n}}\right) \end{split}$$

• If the alternative is $H_1: p < p_0$

$$\beta = 1 - \Phi\left(\frac{p_0 - p - z_\alpha \sqrt{p_0(1-p_0)/n}}{\sqrt{p(1-p)/n}}\right)$$

ullet and finally if the alternative hypothesis is ${\cal H}_1: p>p_0$

$$\beta = \Phi\left(\frac{\rho_0 - \rho + z_\alpha \sqrt{\rho_0(1-\rho_0)/n}}{\sqrt{\rho(1-\rho)/n}}\right)$$



Sample Size

 \bullet Sample size requirements to satisfy type $\mathrm{II}(\beta)$ error constraints for a two-tailed hypothesis test is given by

$$n = \left[\frac{z_{\alpha/2}\sqrt{\rho_0(1-\rho_0)} + z_\beta\sqrt{\rho(1-\rho)}}{\rho-\rho_0}\right]^2.$$

- For a sample size for a one-sided test substitute z_{α} for $z_{\alpha/2}$.
- Problem 9.95

Testing for Goodness of Fit

- Material is presented in section 9-7 of your textbook
- Procedure determines if the sample data is from a specified underlying distribution
 Procedure uses a χ² distribution
 Example 9-12 presents a χ² goodness of fit test for a Poisson example

- ullet Example 9-13 presents a χ^2 goodness of fit test for a normal example



Procedure

- $lackbox{ }$ Collect a random sample of size n from a population with an unknown distribution,
- $\ensuremath{\mathbf{0}}$ Arrange the n observations in a frequency distribution containing k classes
- Calculate the observed frequency in each class O_i,
- From the hypothesized distribution, calculate the expected frequency in class i, denoted E_i (if E_i is small combine classes)
- Calculate the test statistic

$$\chi_0^2 = \frac{\sum_{i=1}^k (O_i - E_i)^2}{E_i}$$

• Reject the null hypothesis if the calculated value of the test statistic $\chi_0^2 > \chi_{\alpha,k-p-1}^2$ where p is the number of parameters in the hypothesized distribution

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Example 9.12, part 1

EXAMPLE 9.12 | Printed Circuit Board Defects—

Poisson Distribution

The number of defects in printed circuit boards is typothesized to follow a Poisson distribution. A random sample of n=60 printed circuit boards has been collected, and the following number of defects observed.

Number of Defects	Observed Frequency
0	32
1	15
2	9
3	4

The mean of the assumed Poisson distribution in this example is unknown and must be estimated from the sample data. The

estimate of the mean number of defects per board is the sample average, that is, $(32 \cdot 0 + 15 \cdot 1 + 9 \cdot 2 \cdot 4 \cdot 4 \cdot 3)00) \approx 0.75$. From the Poisson distribution with parameter 0.75, we may compute p_1 , the theoretical, hypothesided probability associated with the \dot{m} 1 capstraint and \dot{m} 2 consists each class interval corresponds to a particular number of defects, we may find the p_1 as follows:

$$p_1 = P(X = 0) = \frac{e^{-0.3}(0.75)^2}{e^1} = 0.472$$

 $p_2 = P(X = 1) = \frac{e^{-0.3}(0.75)^2}{2!} = 0.354$
 $p_3 = P(X = 2) = \frac{e^{-0.3}(0.75)^2}{2!} = 0.133$
 $p_4 = P(X \ge 3) = 1 - (p_1 + p_2 + p_3) = 0.041$

Example 9.12, part 2

Number of Defects	Probability	
0	0.472	28.32
1	0.354	21.24
2	0.133	7.98
3 (or more)	0.041	2.46

Because the expected frequency in the last cell is less than 3.

6. Computations:

		Expected Frequency
Defects	Frequency.	
0	32	28.32
1	15	21.24
2 (or more)	13	10.44

Parameter of interest: The variable of interest is the form of the distribution of defects in printed circuit bounds.

- 4. Test statistic: The test statistic is $\chi_0^2 = \sum_{i=1}^k \frac{(O_i E_i)^2}{E_i}$ 5. Reject H_0 iff. Because the mean of the Poisson distribution was estimated, the preceding this square statistic will have k p 1 = 3 1 1 = 1 degree of freedom. Consider whether the P-value is less than 0.05.
- $\begin{aligned} \chi_0^2 &= \frac{(32 28.32)^2}{28.32} + \frac{(15 21.24)^2}{21.24} + \frac{(13 10.44)^2}{10.44} \\ &= 2.94 \end{aligned}$
- = 2.94 = 2.94 7. Conclusions: We find from Appendix Table III that $\frac{2}{\lambda_{\rm BM}} = 2.71$ and $\frac{2}{\lambda_{\rm BM}} = 3.84$. Because $\frac{2}{\lambda_{\rm BM}} = 2.94$ lies between the switches, we conclude that the $P-v_{\rm BM}$ is between 0.05 and 0.10. Therefore, because the $P-v_{\rm BM}$ is the records 0.05. we are unable to reject the full hypothesis that the distribution of defects in printed circuit boards is Poisson. The exact $P-v_{\rm BM}$ computed from software is 0.0864.

Chapter 9 Summary

- You should be prepared to work any practice problems assigned: Cases 1-3 with three different alternatives
- All other information is conceptual knowledge that can be questioned with multiple choice

 Name 3 ways to test if data is from a normal distribution

Attendance: 1-B

One-sided example

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H. . N>2.5 20-2.71

P- Julye = P(Z>Z) = 1- 1(2.71) = 1 - .996636 = .003364

If p-value < a, Reject Ho ? p-value = .008367 Else fail to reject Ho

Is p-value L x? yes - Reject

Chapter 9 case 1 lower

Thursday, April 17, 2025 11:43 AM

QUESTION 1

HO. N= 12 H: N212

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=12.0 versus mu less than 12.0 using alpha=0.1. The sample statistics are n=21, xbar=11.11, sigma=2.331.

O z0=1.7497

O z0=-8.018

z0=-1.7497

z0=-3.4397

 $\frac{20-\frac{x-y_0}{x-y_0}}{\sqrt{x}} = \frac{11.11-12}{2331/\sqrt{21}} = -1.74967 = 21$ = -1.74967 = 21 = -1.11 = -1.11

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Ch9, Case 1 Lower

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Construct the rejection region for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=32.0 versus mu less than 32.0 using alpha=0.005. The sample statistics are n=20, xbar=32.11, sigma=2.972.

O Reject Ho if Z0<-2.807

O Reject H0 if z0>2.576

O Reject Ho if |z0|>2.807

Reject H0 if z0<-2.576

Reject +0 if -2a = -2.005 = -2.576

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Ch 9, Case 1 Lower

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QUESTION 5

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=12.0 versus mu less than 12.0 using alpha=0.0025. The sample statistics are n=11, xbar=11.61, sigma=1.067. The value of 20 is -1.2123 and the rejection region is reject H0 if 20 < 2.807

○ Fail to reject H^O

○ Reject H0

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2807 20=-1213

is -1.213 in rejection Repion? No conclusion — Tail to reject to

Ch9, Case 1 Lower

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QUESTION 7

Find the p-value for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=32.0 versus mu less than 32.0 using alpha=0.001. The sample statistics are n=29, xbar=31.1, sigma=3.849 and the value of the test statistic, Z0, is -1.2592.

p value=0.207669

O p-value=0.103835

O p-value=0.896165

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Q-value = $\Phi(z_0) = \Phi(-1.2592)$ = $\Phi(-1.26)$

_ #8 .103835

Ch9, Case 1 Lower

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QUESTION 9

Using the p-value from a test of hypothesis for the mean of single sample with variance known, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.01. The sample statistics are n=21, xbar=17.21, sigma=3.418. The results of hypothesis test include z0=-1.7295 and p-value=0.04186.

Reject H0

Fail to reject H0

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Call 11.57 AM

Call 11.57 AM

p-value = .04/86 = .01

Chapter 9, Case 2 2-sided

Tuesday, April 22, 2025 11:31 AM

QUESTION 1

Ho. N=. S

Ho. N=. S

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=0.5 versus mu not equal to 0.5 using alpha=0.001. The sample statistics are n=18, xbar=0.51, S=0.051.

O t0=69.2042

O t0=3.5294 ○ t0=0.8319

 $t_0 = \frac{\bar{x} - N_0}{s/on} = \frac{s/-s}{0s/\sqrt{s}}$

O t0=-0.8319

= 0.83189

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Chapter 9, Case 2 2-sided

Tuesday, April 22, 2025 11:34 AM

QUESTION 3

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=18.5 versus mu not equal to 18.5 using alpha=0.02. The sample statistics are n=20, xbar=19.35, S=4.813.

Reject Ho If t0>2.205

O Reject H0 if |t0|>2.539

Reject Ho if t0>2.539

O Reject Ho if t0<-2.539

O Reject H0 if |t0|>2.205

Reject Ho if t0<-2.205

Reject Ho ; f $1 \pm 01 > \pm \alpha/2, n-1 = \pm .01, 19 = 2.53$

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QUESTION 5

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=25.8 versus mu not equal to 25.8 using alpha=0.01. The sample statistics are n=26, x bar=30.28, x =5.3. The value of t0 is 4.3101 and the rejection region is reject HO if |t0| > 2.787

Fail to reject H0

O Reject H0

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to = 41.3101

 $RR: |t_0| > 2.787$ $TS \quad 4.3101 > 2.787$ ARRIVED AREJECT AREA AREJECT AREJE

Chapter 9, Case 2 2-sided

Tuesday, April 22, 2025 11:39 AM

QUESTION 7

Using the p-value from a test of hypothesis for the mean of single sample with variance unknown, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=0.5 versus mu not equal to 0.5 using alpha=0.1. The sample statistics are n=7, xbar=0.52, S=0.038. The results of hypothesis test include t0=1.3925 and p-value=0.213186.

O Reject H0 ○ Fail to reject H0

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D-value = . or .

d = . 1

Is . 213< . 1? No -> fail to
Reject Ho

Chapter 9, Case 2 upper

Tuesday, April 22, 2025 11:42 AM

QUESTION 1

Hb: N=132.3 H,: N>132.3

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=132.3 versus mu greater than 132.3 using alpha=0.0025. The sample statistics are n=24, xbar=139.02, S=20.204.

O t0=1.6294 O t0=-1.6294

O t0=0.3951

O t0=7.9826

 $t_{0} = \frac{X - N_{0}}{S/In} = \frac{139.02 - 132.3}{20204/\sqrt{224}}$ = 1.6294

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Chapter 9 Page 46

Chapter 9, Case 2 Upper

Tuesday, April 22, 2025 11:47 AM

Rejection Region is Hed H,

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=18.5 versus mu greater than 18.5 using alpha=0.05. The sample statistics are puts, xbar=T9.72, S=3.905.

Reject Ho if t0<-1.761

- O Reject Ho if t0<-2.145
- O Reject Ho if |t0|>2.145
- O Reject H0 if t0>1.761

QUESTION 3

O Reject H0 if |t0|>1.761

Screen clipping taken: 4/22/2025 11:47 AM

to> tainy = tos, 15-1 = 1.761

Chapter 9, Case 2 Upper

Tuesday, April 22, 2025 11:50 AM

QUESTION 5

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=12.0 versus mu greater than 12.0 using alpha=0.05. The sample statistics are n=20, xbar=12.2, S=1.928. The value of t0 is 0.4639 and the rejection region is reject HO if t0>1.729

Reject H0
Fail to reject H0
Screen clipping taken: 4/22/2025 11:50 AM

to-0.4639 Rejul Ho if to> 1.729

> is .4637 > 1.729? No -> fail to reject

Chapter 9, Case 2 Upper

Tuesday, April 22, 2025 11:51 AM

QUESTION 7

Using the p-value from a test of hypothesis for the mean of single sample with variance unknown, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=132.3 versus mu greater than 132.3 using alpha=5.0E-4. The sample statistics are n=18, xbar=139.18, S=24.068. The results of hypothesis test include t0= 1.2128 and p-value=0.241791.

O Reject H0

Fail to reject H0

Screen clipping taken: 4/22/2025 11:52 AM

.5 E -3 .05 E -2 .005 E -1

15 Prome < a 22/18 < .0005 ? No. feel to Reject Ho

Chapter 9 Page 49

Chapter 9, case 2 lower Tuesday, April 22, 2025 11:55 AM Caus	ed brog ramming	
QUESTION 1 Calculate the test statistic for a test of hypothesis for using alpha=0.001. The sample statistics are n=24, xt t0=0.0 t0=0.0	the meap of single sample with variance unknown. The null hypothesis is mu=0.5 versus mu less than 0.5 ar=0.5, \$\frac{5}{2}\text{0.061}.	i
t0=0.0 t0=0.0 Screen clipping taken: 4/22/2025 11:57 AM	$t_0 = \frac{x - 1/6}{5/10} = \frac{.55}{.061/\sqrt{247}} = 0.0$	එ

Chapter 9, Case 2 Lower

Tuesday, April 22, 2025 11:59 AM

DAMIN .

H, ; K, M

H,:NL 12

QUESTION 3

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=12.0 versus mu less than 12.0 using alpha=0.01. The sample statistics are n=6, xbar=11.79, S=2.19.

- O Reject Ho if |t0|>4.032
- O Reject Ho if t0>3.365
- O Reject H0 if t0<-3.365
 - O Reject H0 if |t0|>3.365
 - O Reject Ho if t0<-4.032

Reject Ho if tox-tainy =-t.0155 =-3.365

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Chapter 9, Case 2 Lower

Tuesday, April 22, 2025 12:01 PM

QUESTION 5

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=25.8 versus mu less than 25.8 using alpha=0.1. The sample statistics are n=5, xbar=16.98, S=6.924. The value of t0 is -2.8484 and the rejection region is reject HO if t0<-1.533

Screen clipping taking 1/2/22 pm Reject HO 1 = -2.8484Screen clipping taking 1/2/22 pm Reject HO if $t_0 < -1.533$ $1 \le -2.8484 < -1.533$ $1 \le -2.8484$ $1 \le -2.8484$

Chapter 9, Case 2 Lower

Tuesday, April 22, 2025 12:04 PM

QUESTION 7

Using the p-value from a test of hypothesis for the mean of single sample with variance unknown, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.025. The sample statistics are n=7, xbar=15.44, S=5.429. The results of hypothesis test include t0= -1.4913 and p-value=0.186478.

Fail to reject H0

O Reject H0

Screen clipping taken: 4/22/2025 12:05 PM

Q = .025 P-value = .1865

is p-value < x?

15.1865<.025? No -> fail to Reject Ho Attendance /- C

Thursday, April 24, 2025 11:22 AM

Ho:02 =324

QUESTION 1

Hi. 02 = 324

Calculate the test statistic for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=324.0 versus sigma^2 not equal to 324.0 using alpha=0.2. The sample statistics are n=28, xbar=126.28, S=50.933. N=28

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$$\chi_{0}^{2} = \frac{(n-1)5^{2}}{\sigma_{0}^{2}} = \frac{(28-1)(50.933)}{324}$$

$$= 216.181$$

Chapter 9, Case 3 2-sided

Thursday, April 24, 2025 11:24 AM

QUESTION 3

A = 1

Construct the rejection region for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=11.56 versus sigma^2 not equal to 11.56 using alpha=0.1. The sample statistics are n=51, xhar=32.05, S=9.274.

Reject Ho If chiSquare0<37,69

Reject H0 if ChiSquare0<34.76 or ChiSquare0>67.5

- Reject Ho if chiSquare0<34.76
- O Reject Ho if chiSquare0>63.17
- O Reject Ho if ChiSquare0>67.5
- O Reject H0 if ChiSquare0<37.69 or ChiSquare0>63.17

Screen clipping taken: 4/24/2025 11:25 AM

1 Hoif

 $\chi^{2} > \chi^{2}_{\sim 10-1} = \chi^{2}_{0.05,50} = 67.50$

 $\chi_{0}^{2} < \chi_{1-\alpha/2, n-1}^{2} = \chi_{.95,50}^{2} = 34.76$ $\chi_{1-\alpha/2, so}^{2} = \chi_{1-.05,50}^{2} = \chi_{.95,50}^{2}$

Chapter 9, Case 3 2-sided

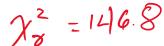
Thursday, April 24, 2025 11:30 AM

QUESTION 5

What is the correct conclusion for a test of hypothesis for the variance of a normal distribution. The null hypothesis is Sigma^2=0.0036 versus sigma^2 not equal to 0.0036 using alpha=0.1. The sample statistics are n=9, xbar=0.54, S=0.257. The value of ChiSquare0 is 146.7756 and the rejection region is reject HO if ChiSquare0<2.73 or ChiSquare0>15.51

- O Fail to reject H0
- O Reject H0

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2 = 146.8 Reject to it

is 146.8 > 15.517, yes -> Reject Ho 1468 < 2.73 ? No

Chapter 9, Case 3 2-sided

Thursday, April 24, 2025 11:34 AM

JES		
		/

Using the p-value from a test of hypothesis for the variance of a normal distribution, determine the correct conclusion for the hypothesis test. The null hypothesis is Sigma^2=11.56 versus sigma^2 not equal to 11.56 using alpha=0.02. The sample statistics are n=2, xbar=34.08, S=0.392. The results of hypothesis test include ChiSquare0= 0.0133 and p-value=0.184.

if p-value 2x, Reject Ho is 184 < .02? No -> fail to reject Ho

○ Fail to reject H0

O Reject H0

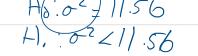
p-value = . 184 < = .02

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Chapter 9, Case 3 Lower

Thursday, April 24, 2025 11:37 AM

QUESTION 1



Calculate the test statistic for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=11.56 versus sigma^2 less than 11.56 using alpha=0.005. The sample statistics are n=6, xbar=31.81, S=1.509.

- O ChiSquared0=11.2657
- O ChiSquared0=25.3834
- O ChiSquared0=0.9849
- ChiSquared0=2 2191

 $\chi_{\mathfrak{d}}^2 =$

(n-1)52

= (6-1) (1.507)² = 11.56

=0.9849

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Chapter 9, Case 3 Lower

Thursday, April 24, 2025 11:40 AM

QUESTION 3

(bwe) h; oz < .0036

Construct the rejection region for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=0.0036 versus sigma^2 less than 0.0036 using alpha=0.1. The sample statistics are n=22, xbar=0.5, S=0.024.

- O Reject Ho if chiSquare0>29.62
- O Reject H0 if ChiSquare0>13.24 or ChiSquare0>29.62
- Reject Ho if chiSquare0<11.59

- Reject Ho if chiSquare0<13.24

 Reject Ho if ChiSquare0<11.59 or ChiSquare0>32.67
 - O Reject Ho if ChiSquare0>32.67

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Reject the it $\chi^2 < \chi^2_{1-\alpha,n-1} = \chi^2_{.9,21} =$

Chapter 9, Case 3 Upper

Thursday, April 24, 2025 11:43 AM

2=44.89

QUESTION 1

Calculate the test statistic for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=44.89 versus sigma^2 greater than 44.89 using alpha=0.005. The sample statistics are n=18, xbar=26.32, S=13.396.

- ChiSquared0=33.9899
- ChiSquared0=8.5025
- O ChiSquared0=4.2525

ChiSquared0=67.9594

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 $r_{8}^{2} = \frac{(n-1)s^{2}}{3s^{2}} = \frac{(18-1)(13.396)^{2}}{44.89}$

= 67.9594/

Chapter 9, Case 3 Upper

Thursday, April 24, 2025

11:44 AM

QUESTION 3

Z=.05

to: 02 = .0036 Hi.027,0036

Construct the rejection region for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=0.0036 versus sigma^2 greater than 0.0036 using alpha=0.05. The sample statistics are n=10, xbar=0.56, S=0.076.

- O Reject H0 if ChiSquare0<2.7 or ChiSquare0>19.02
- Reject H0 if ChiSquare0<3.33 or ChiSquare0>16.92
- O Reject Ho if chiSquare0>16.92
- O Reject Ho if chiSquare0<3.33
- O Reject Ho if chiSquare0<2.7
- O Reject Ho if ChiSquare0>19.02

Screen clipping taken: 4/24/2025 11:46 AM

Reject Ho if $\chi_0^2 > \chi_{\alpha,n-1}^2$ $\chi_0^2 > \chi_{.05,9}^2 = 16.92$