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Wednesday, April 16, 2025 8:01 AM





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 Chapter 9 slides Chapter 9 slides marked 	
Chapter 9 slides marked	
3/70	

troc	duction to Hypot	thesis Testing	
• In	onclusions about a po	nsists of methods used	d to make decisions or drav ation contained in a sampl
• In	ference is divided int Parameter estimatio Hypothesis testing	on (both point and inte	erval)
			4

verview of Statistical Hypotheses

- Many engineering problems require a decision to be made regarding some statement about a parameter
 - The statement is called a hypothesis
 - The decision-making process about the hypothesis is call hypothesis testing
- Statistical hypothesis testing is usually the data analysis stage of a comparative experiment
- A procedure leading to a decision about a particular hypothesis is called a test of hypothesis
- Testing the hypothesis involves taking a random sample, computing a test statistic from the sample data and then using the to make a

Hoi. N= value Hoi. is innomed

Hoi. N= value Hoi. is innomed

Hi: SV = value

Hoi. N= value

Hoi. is innomed

Hoi. is innomed

Hoi. is innomed

N = value

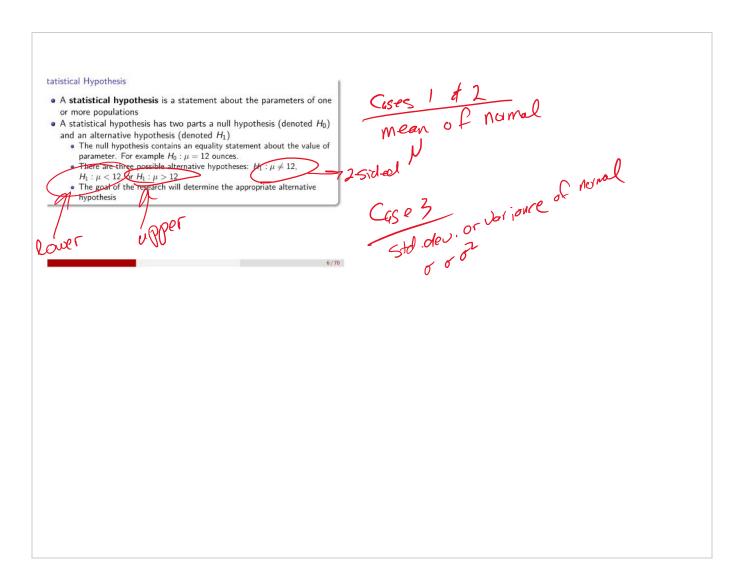
Not

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Note

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skip this for a while



Chapter 8, Case 1 X-2-12 Tr & N < X+Zax Fr

Summary of One-Sample Hypothesis-Testing Procedures

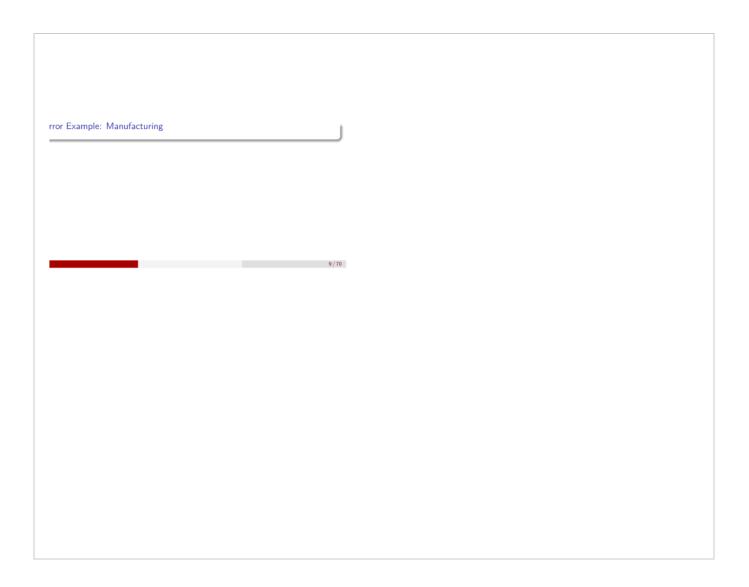
Case	Null Hypothesis	Test Statistic	Alternative Hypothesis
1.	$H_0: \mu = \mu_0$	$\bar{x} - \mu_0$	$H_1: \mu \neq \mu_0$
	σ^2 known	$z_0 = \frac{1}{\sigma / \sqrt{n}}$	$H_1: \mu > \mu_0$
			$H_1: \mu < \mu_0$

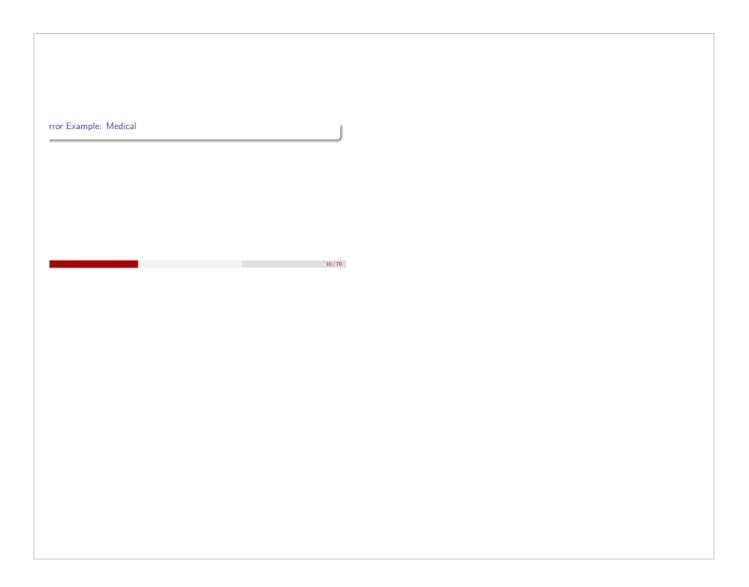
W 7 WA

rrors in hypothesis testing

- ullet Whether a correct decision is made depends upon the true nature of H_0 and the decision arrived at.
- A type I error occurs when the null hypothesis is true and the outcome of the test is to reject H_0 . The probability of a type I error is denoted as α
- A type II error occurs when the null hypothesis is false and the outcome of the test is to fail to reject H₀. The probability of a type II error is denoted as β.
- The power of a statistical test is the probability rejecting the null hypothesis H_0 when the alternative hypothesis is true. Power = $1-\beta$







neral Procedure for Hypothesis Testing he following sequence of steps is recommended • From the problem context, identify the parameter of interest, • State the null hypothesis, H₀, • Specify an appropriate alternative hypothesis, H₁, • Choose a significance level α • State an appropriate test statistic, • State the rejection region for the (test) statistic, • Compute any necessary sample quantities, substitute these into the equation for the test statistics, and compute that value, • Decide whether or not H₀ should be rejected and report in the problem context

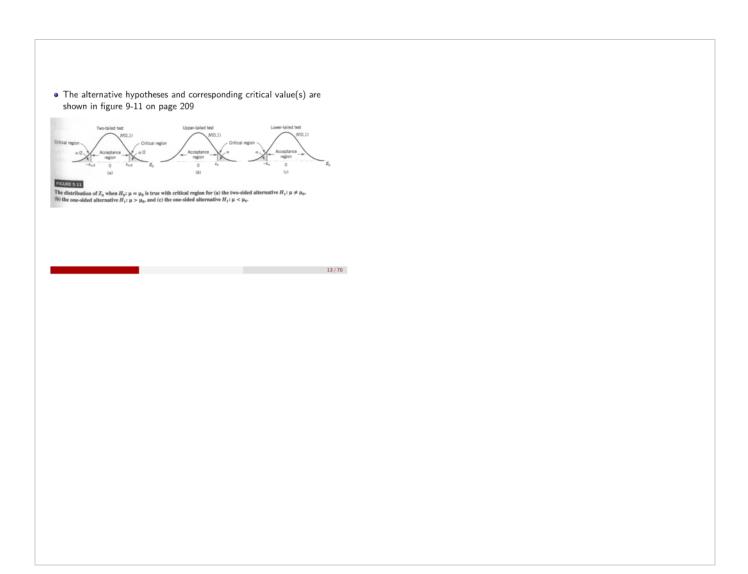
hapter 9, Case 1

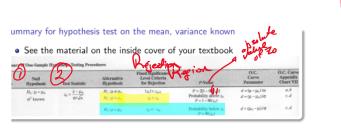
iference on the Mean of a population, variance known

- Assumptions:
 X₁, X₂,..., X_n is a random sample of size n from a population
 The population is normal, or if it is not normal, the conditions of the central limit theorem apply
- The parameter of interest is μ The null hypothesis is $H_0: \mu = \mu_0$
- The test statistic is

$$Z_0 = \frac{\overline{X} - \mu_0}{\sigma / \sqrt{n}}$$

nd has a standard normal distribution





Reject Ho if

p-value <

Else (if p-value > x)

fail to reject Ho

Chapter 9 Page 14



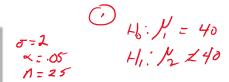
Example 11-1

The burning rate of a rocket propellant is being studied. Specifications require that the mean burning ate must be 40 cm/s. Furthermore, suppose that we know that the standard deviation of the burning ate is approximately 2 cm/s. The experimenter decides to specify a type I error probability α = 0.05, and he will base the test on a random sample of size n = 25. The hypotheses we wish to test are

 H_0 : $\mu = 40$ cm/s. H_1 : $\mu \neq 40$ cm/s.

Twenty-five specimens are tested, and the sample mean burning rate obtained is $\bar{x} = 41.25$ cm/s.

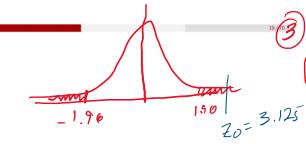
Source: Himes. Mortgonery, Goldsman, Borron (2003). Probability and Statistics in Enghamming, 4th ed.



Tot Statistic

Zo= X-1/0 = 41.25-40

2/025
3.125



Rejection Region (tied to 41)

Reject to if |Zo| > Za/2

lasical dist

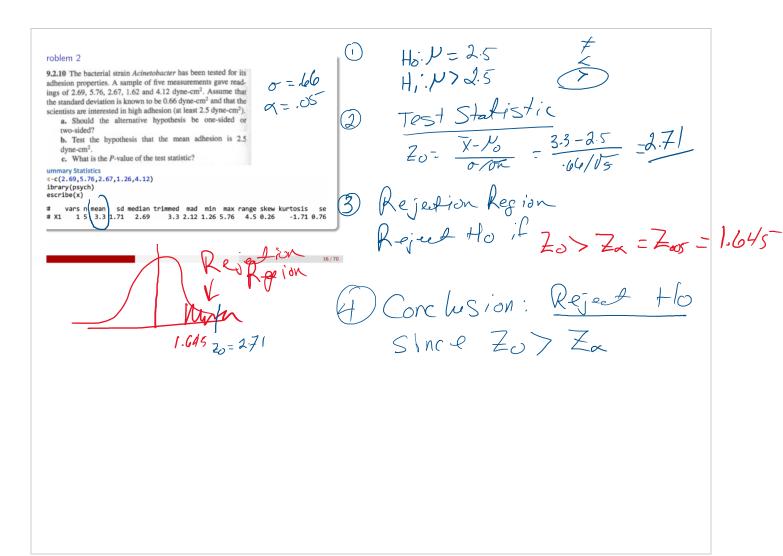
Gonclusion: =1.96

Since Zo > Zerz, we reject

the null hypothesis.

The mean burn is different from

HO CM/S at an .05 significance level



onnection between Hypothesis Tests and CI

- There is a close connection between confidence intervals and hypothesis tests
- Consider a 100(1 - $\alpha)\%$ confidence interval on μ and a hypothesis test of size α shown below

 $H_0: \mu = \mu_0$ $H_1: \mu \neq \mu_0$

- \bullet The conclusion to reject H_0 will be reached if μ_0 is not contained within the confidence interval
- If μ_0 is within the confidence interval, we fail to reject H_0
- The 100(1-lpha)% confidence interval on μ is the acceptance region

Confidence interval is the Same as the acceptance rgion in a Statistical hypothesis test

-values

• Is a widely used alternative to the traditional hypothesis test

ullet Definition: The p-value is the smallest level of significance that would lead to reject of the null hypothesis H_0 with the given data

· Formulas are given below

$$P = \left\{ \begin{array}{ll} 2[1-\Phi(|z_0|)] & \text{for a two-tailed test} \\ 1-\Phi(z_0) & \text{for a upper-tailed test} \\ \Phi(z_0) & \text{for a lower-tailed test} \end{array} \right.$$

ullet Usage: if $p ext{-value}<lpha$ then the conclusion is reject H0, otherwise fail to reject H0

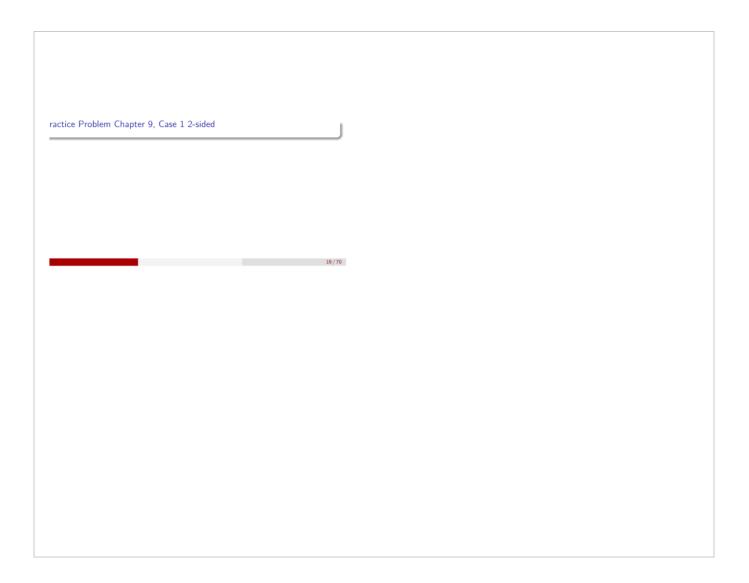
Test 1 - Continuation (1772.5)

Test2

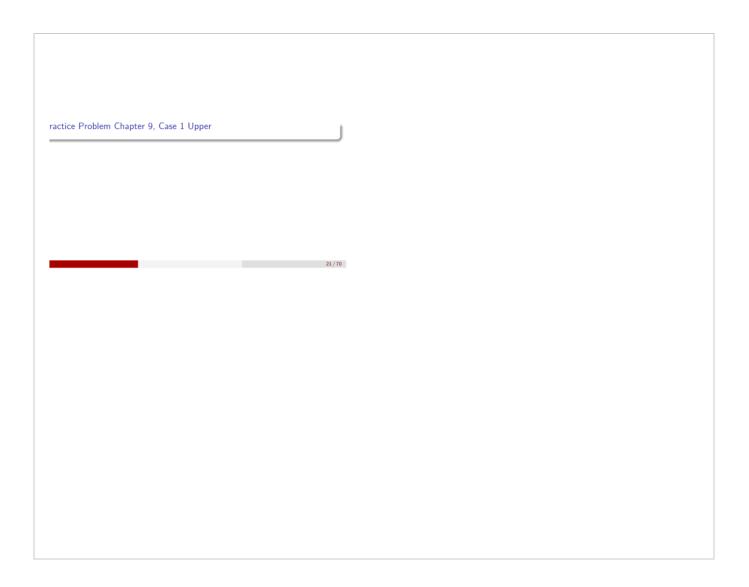
Zo=1.64

Zo=1.65

Conclusion: fail Conclusion: reject
to reject to the







ype II error and sample size for a two-tailed test

• Probability of type II error for the two-tailed test

$$\beta = \Phi \left(\mathbf{z}_{\alpha/2} - \frac{\delta \sqrt{n}}{\sigma} \right) - \Phi \left(-\mathbf{z}_{\alpha/2} - \frac{\delta \sqrt{n}}{\sigma} \right)$$

here $\mu=\mu_0+\delta$ • The sample to detect a difference between the true and hypothesized mean of δ with power at least $1-\beta$ is

$$n \approx \frac{(z_{\alpha/2} + z_{\beta})^2 \sigma^2}{\delta^2}$$

here $\delta = \mu - \mu_{\rm 0}$

ype II error and sample size for the one-tailed tests

• For an upper-tailed test

$$\beta = \Phi\left(z_{\alpha} - \frac{\delta\sqrt{n}}{\sigma}\right)$$

• For a lower-tailed test

$$\beta = 1 - \Phi\left(-z_{\alpha} - \frac{\delta\sqrt{n}}{\sigma}\right)$$

• The sample size required to detect a difference between the true mean and hypothesized mean of δ with power at least $1-\beta$ is

$$n = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{\delta^2}$$

n is not an integer, round up to the nearest integer

```
Cécsi
Library(SSGA)

BB Loading required package: lattice

BB Attaching package: 'BSGA'

BB The following object is masked from 'package:datasets':

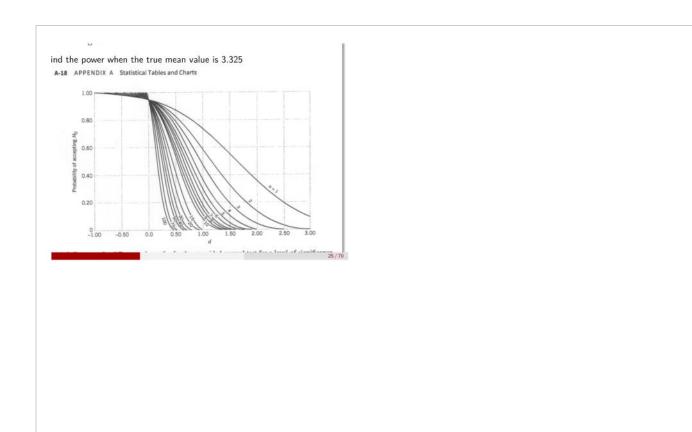
BB Corange
Lest(vg.laternative='greater',mu-2.5,sigma.u-00.66,conf.level-00.95)

BB One-:ample z-Test

BB Cec-:ample z-Test

BB data: x

BB data:
```



```
Nomer
(itery/(statio))

**H saming: package 'sobis' was built under % version 4.2.3

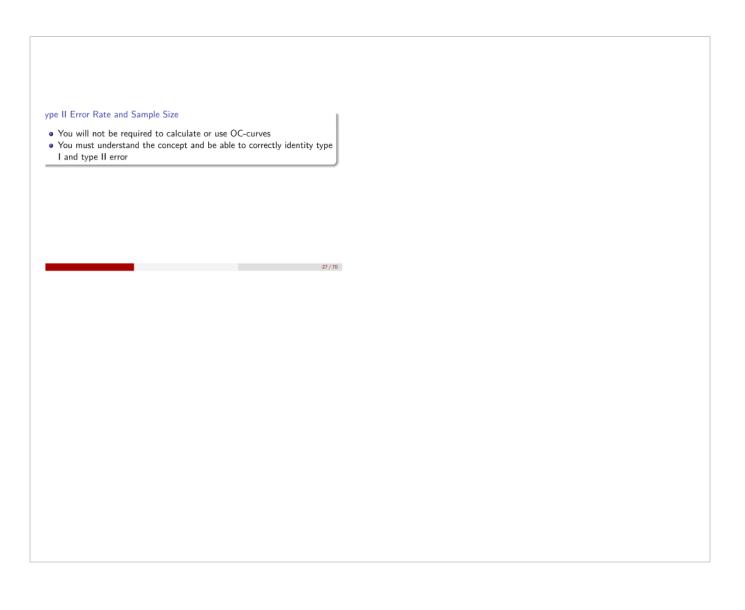
**H contain remained package: "sobis'

**H Attaching aspage: "sobis'

**H the following object is masked from 'package(spych'):

**H sam

**Nomer **C. NOTE((spuc + 0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5, -0.5
```



hapter 9, Case 2

ypothesis Test on the Mean, Variance Unknown

- Much more common case than variance known Substitute S for σ
- \bullet The test statistics is now a t random variable

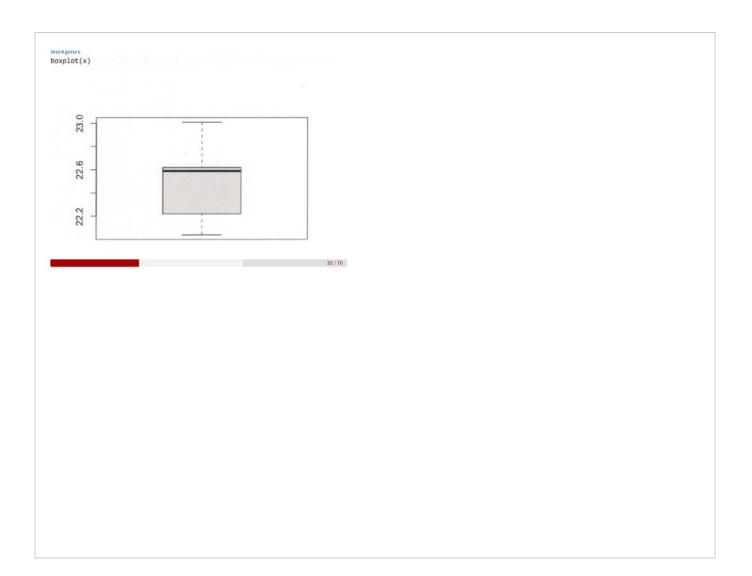
$$T = \frac{\overline{X} - \mu_0}{S/\sqrt{n}}$$



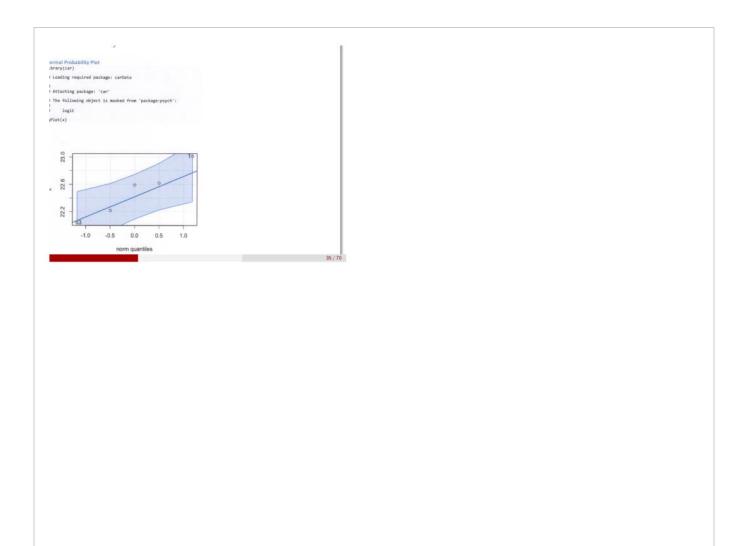
roblem 9.3.6

- 9.3.6 An article in the ASCE Journal of Energy Engineering (1999, Vol. 125, pp. 59–75) describes a study of the thermal inertia properties of autoclaved aerated concrete used as a building material. Five samples of the material were tested in a structure, and the average interior temperatures (*C) reported were as follows: 23.01, 22.22, 22.04, 22.62, and 22.59.
 - a. Test the hypotheses H_0 : $\mu=22.5$ versus H_1 : $\mu\neq22.5$, using $\alpha=0.05$. Find the P-value.
 - b. Check the assumption that interior temperature is normally distributed.
 - c. Compute the power of the test if the true mean interior temperature is as high as 22.75.
 - d. What sample size would be required to detect a true mean integor temperature as high as 22.75 if you wanted the power of the test to be at least 0.9?
 - e. Explain how the question in part (a) could be answered by constructing a two-sided confidence interval on the mean interior temperature.

```
Descriptive Statistics
c--(2].01,22.22,22.04,22.02,22.59)
Library(syxch)
SE vars n mean sd median trimmed mad min max range skew kurtosis
EM vars n mean sd median trimmed mad min max range skew kurtosis
EM vars n to var n var n
```







-values	
More difficult to calculate since the t-tables only contain a few	
The state of the s	
quantiles	
ullet Can use tables to generate bounds on the p -value	
C C C C C C C C C C C C C C C C C C C	
Software will provide p-values	
36/70	

```
-values from R

t-test
t.test(x_alternative~two.sided',w=22.5,conf.level=0.95)

##

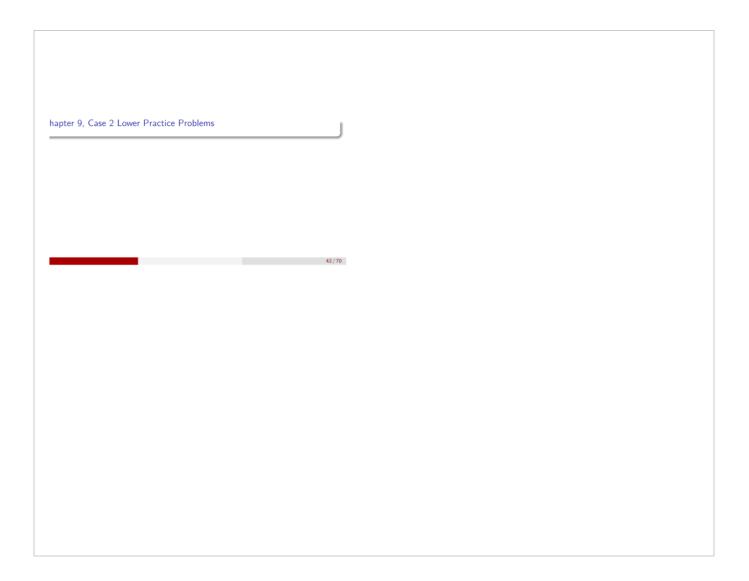
## One Sample t-test
## data: x

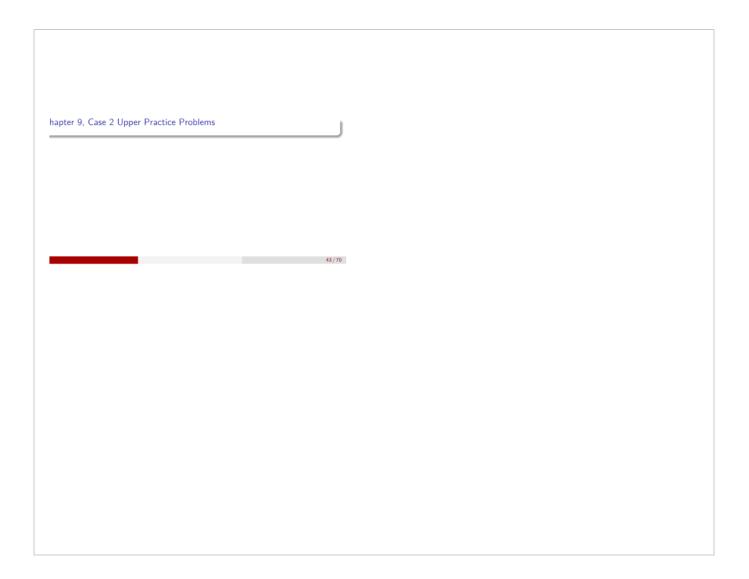
## t==0.82642.0 ff = a, p-value = 0.9823

## alternative hypothesis: true mean is not equal to 22.5
## sample extinates:
## sample extinates:
## sample extinates:
## ample extinates:
## 22.496
```





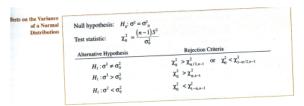




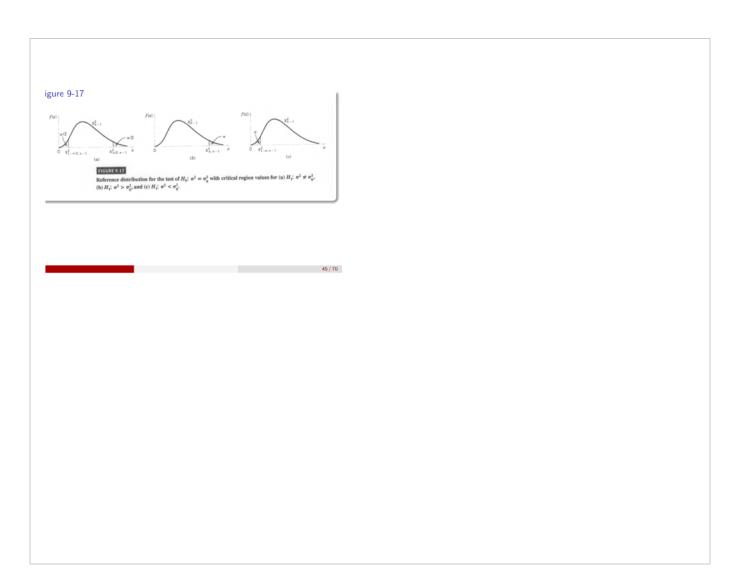
ase 3. Hypothesis Test on Variance of Normal Population

 \bullet The test statistics is a χ^2 random variable

$$\chi_0^2 = \frac{(n-1)S^2}{\sigma_0^2}$$



The table below summarizes the three possible hypothesis tests. The ejection regions are clearly shown in Figure 9-17 on page 222 $\,$

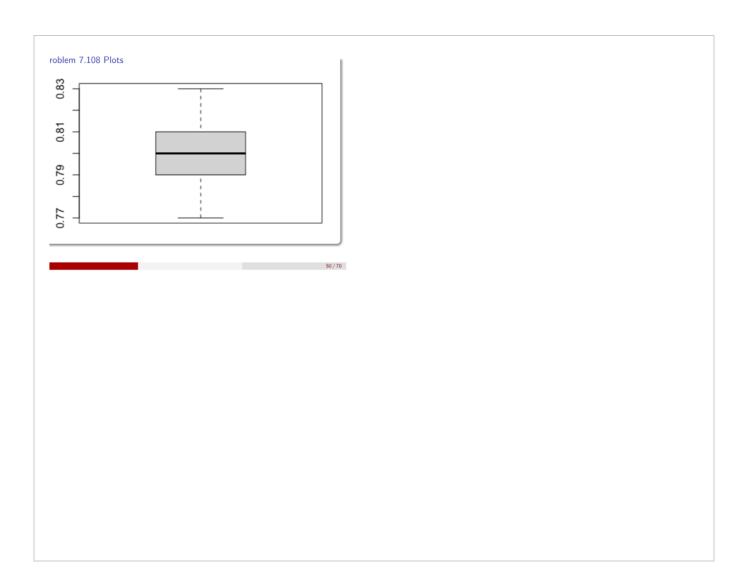


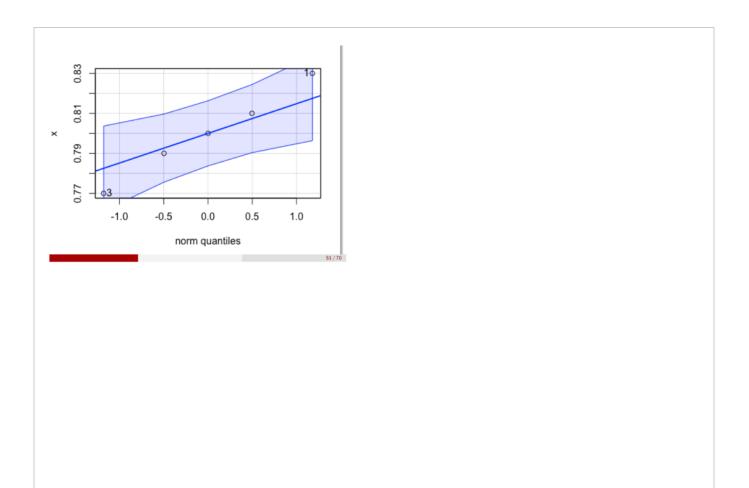


roblem T.108 roblem taken from Ostle, Turner, Hicks and McElrath (1996). Engineering tatistics: The Industrial Experience. Duxbury Press. 1.08 Incoming coal at a coking plant is routinely analyzed for sulfur content (in percent). In the past, samples taken from barges loaded with coal from a particular mine have had a variance of 0.000196. When a new analyst was hired, the results of an assay of coal from the mine produced percentages of 0.83, 0.79, 0.77, 0.81, and 0.80. (a) Using \(\alpha = 0.05, \) does the sample variance provide sufficient evidence to conclude that the results from the new analyst indicate more variability than in the past? State all assumptions. (b) Based on these data, is an assumption of normality reasonable? Justify by using a normal quantile plot and a formal test such as the Shapiro-Wilk W test.









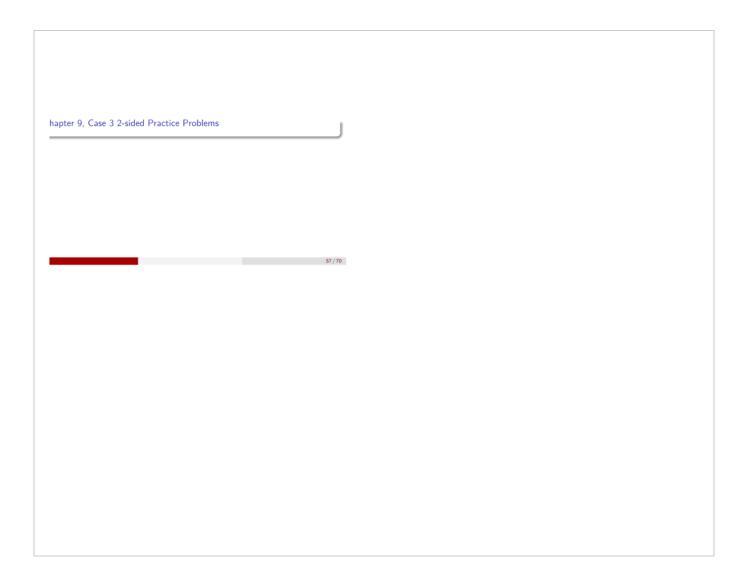


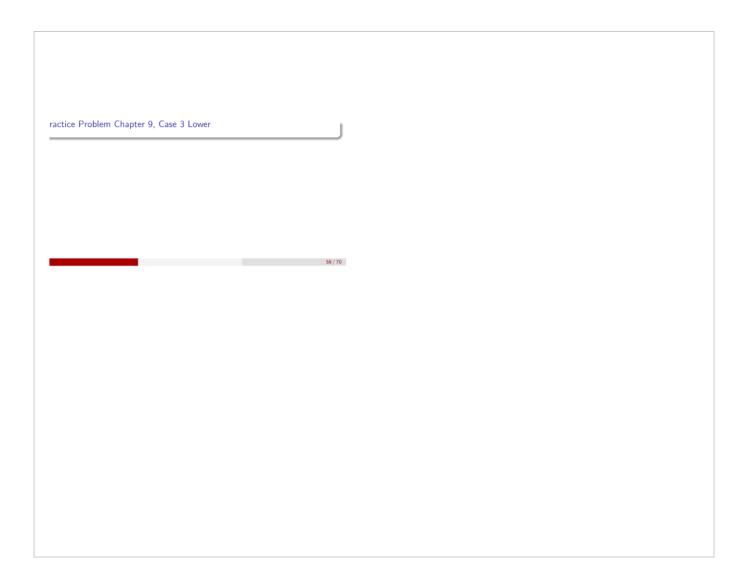
-values
A Visco similar to the core for the many of a named acceptation with
Very similar to the case for the mean of a normal population with
variance unknown
• Difficult to calculate since the χ^2 -tables only contain a few quantiles • Can use tables to generate bounds on the p -value
• Can use tables to generate bounds on the p-value
• Software will provide p-values
Software will provide p-values
53/70

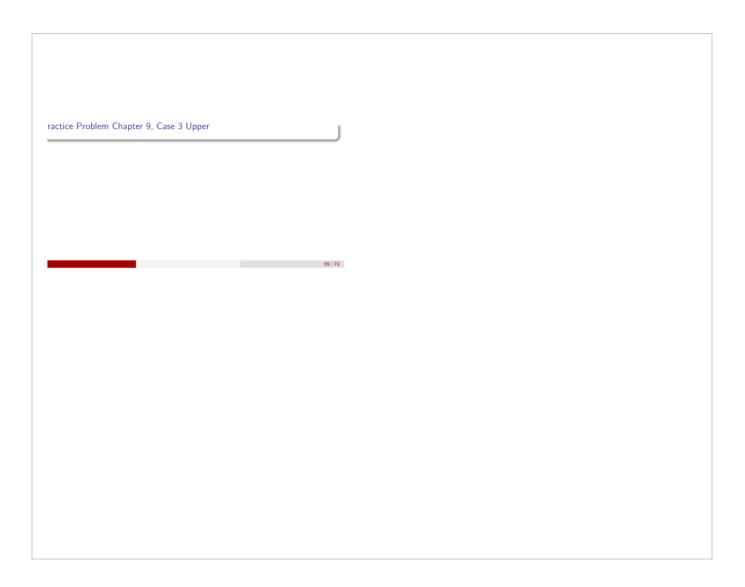
arTest(x,alternative="greater",conf.level=0.95,sigma.squared=0.000196) # Results of Hypothesis Test # # Null Hypothesis: # variance = 0.000196 # Alternative Hypothesis: True variance is greater than 0.000196 # # Test Name: Chi-Squared Test on Variance # # Estimated Parameter(s): variance = 5e-04 # Data: Chi-Squared = 10.20408 # Test Statistic: #
Test Statistic Parameter: df = 4 # P-value: 0.03712675 LCL = 0.0002107986 UCL = Inf # 95% Confidence Interval:

ower Calculations	
 Can be done with OC curves found in Table VIIi-n 	
Can be done in software such as R	
55/70	









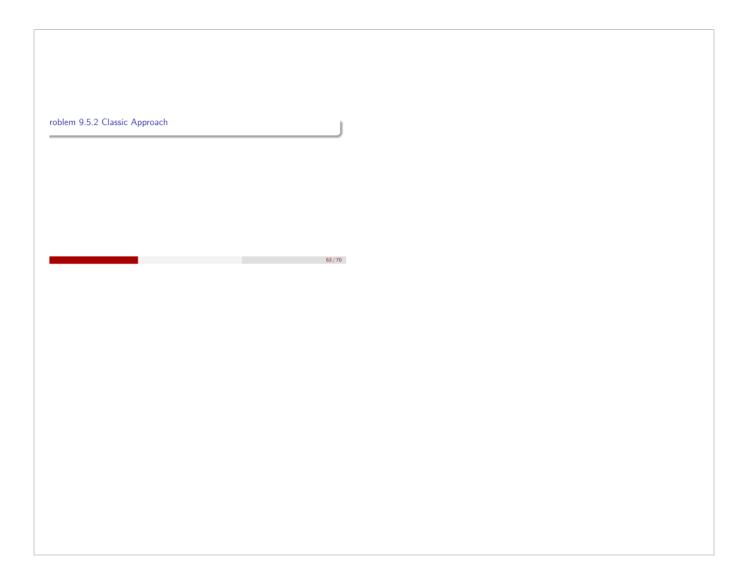
ase 4. Hypothesis Test on a Population Proportion

• The test statistics for the hypothesis test is

$$Z_0 = \frac{x - np_0}{\sqrt{np_0(1 - p_0)}}$$







ower Calculations

• For the two-sided alternative hypothesis

$$\beta = \Phi\left(\frac{p_0 - p + z_{\alpha/2}\sqrt{p_0(1-p_0)/n}}{\sqrt{p(1-p)/n}}\right)$$
$$-\Phi\left(\frac{p_0 - p - z_{\alpha/2}\sqrt{p_0(1-p_0)/n}}{\sqrt{p(1-p)/n}}\right)$$

ullet If the alternative is ${\it H}_1: {\it p} < {\it p}_0$

$$\beta = 1 - \Phi\left(\frac{\rho_0 - \rho - z_\alpha \sqrt{\rho_0(1-\rho_0)/n}}{\sqrt{\rho(1-\rho)/n}}\right)$$

 \bullet and finally if the alternative hypothesis is ${\it H}_1: p>p_0$

$$\beta = \Phi\left(\frac{p_0 - p + z_\alpha \sqrt{p_0(1 - p_0)/n}}{\sqrt{p(1 - p)/n}}\right)$$

ample Size

 \bullet Sample size requirements to satisfy type ${\rm II}(\beta)$ error constraints for a two-tailed hypothesis test is given by

$$n = \left[\frac{z_{\alpha/2}\sqrt{\rho_0(1-\rho_0)} + z_{\beta}\sqrt{\rho(1-\rho)}}{\rho - \rho_0}\right]^2.$$

- For a sample size for a one-sided test substitute z_{α} for $z_{\alpha/2}.$ Problem 9.95

esting for Goodness of Fit Material is presented in section 9-7 of your textbook Procedure determines if the sample data is from a specified underlying distribution Procedure uses a χ² distribution Example 9-12 presents a χ² goodness of fit test for a Poisson example Example 9-13 presents a χ² goodness of fit test for a normal example

rocedure

- lack O Collect a random sample of size n from a population with an unknown distribution,
- $oldsymbol{\circ}$ Arrange the n observations in a frequency distribution containing k classes
- \odot Calculate the observed frequency in each class O_i ,
- From the hypothesized distribution, calculate the expected frequency in class i, denoted E_i (if E_i is small combine classes)
- O Calculate the test statistic

$$\chi_0^2 = \frac{\sum_{i=1}^k (O_i - E_i)^2}{E_i}$$

• Reject the null hypothesis if the calculated value of the test statistic $\chi_0^2 > \chi_{\alpha,k-p-1}^2$ where p is the number of parameters in the hypothesized distribution

xample 9.12, part 1

EXAMPLE 9.12 | Printed Circuit Board Defects-

Poisson Distribution The number of defects in printed circuit boards is hypothesized to follow a Poisson distribution. A random sample of n=60 printed circuit boards has been collected, and the following number of defects observed.

Number of Defects	
0	32
1	15
2	9
3	4

The mean of the assumed Poisson distribution in this example is unknown and must be estimated from the sample data. The

estimate of the mean number of defects per board is the sample average, that is, (32 · 0 + 15 · 1 + 9 · 2 · 4 + 3)60 = 0.75. From the Poisson distribution with parameter 0.75, we may compute p₁, the theoretical, hypothesized probability associated with the th class interval. Because each class interval corresponds to a particular number of defects, we may find the p₁ as follows:

$$p_1 = P(X = 0) = \frac{e^{-0.75}(0.75)^6}{0!} = 0.472$$

 $p_2 = P(X = 1) = \frac{e^{-0.75}(0.75)^4}{1!} = 0.354$

$$p_3 = P(X = 2) = \frac{e^{-0.25}(0.75)^2}{2!} = 0.133$$

$$p_a = P(X \geq 3) = 1 - (p_1 + p_2 + p_3) = 0.041$$

The expected frequencies are computed by multiplying the sample size $n=60$ times the probabilities p_i . That is, $E_i=np_i$. The expected frequencies follow:			 Null hypothesis: H₀: The form of the distribution of defects is Poisson. Alternative hypothesis: H₁: The form of the distri- bution of defects is not Poisson.
Number of Defects		Expected Frequency	
0	0.472	28.32	4. Test statistic: The test statistic is $\chi_0^2 = \sum_{i=1}^k \frac{(O_i - E_i)^2}{E_i}$
1	0.354	21.24	5. Reject Ha if: Because the mean of the Poisson distri
2	0.133	7.98	bution was estimated, the preceding chi-square statistic
3 (or more)	0.041	2.46	will have $k - p - 1 = 3 - 1 - 1 = 1$ degree of freedom Consider whether the P-value is less than 0.05.

Because the expected frequency in the last cell is less than 3, we combine the last two cells: $v^2 = \frac{(32 - 28.32)^2}{3}$

Observed Frequency	Expected Frequency
32	28.32
15	21.24
13	10.44
	Frequency 32 15

The seven-step hypothesis-testing procedure may now be applied, using $\alpha=0.05,$ as follows:

Parameter of interest: The variable of interest is the form of the distribution of defects in printed circuit boards.

$$\chi_0^2 = \frac{(32 - 28.32)^2}{28.32} + \frac{(15 - 21.24)^2}{21.24} + \frac{(13 - 10.44)^2}{10.44}$$

= 2.94

6. Computations: $z_0^2 = \frac{(3-28.32)^2}{28.32} + \frac{(15-21.24)^2}{21.24} + \frac{(13-10.44)^2}{10.44}$ = 2.947. Conclusions: We find from Appendix Table III that z_0^2 (y_0) = 2.71 and y_0^2 (y_0) = 9.38. Because z_0^2 = 2.94 lies between these values, we conclude that the P-value is between 0.05 and 0.10. Therefore, because the P-value exceeds 0.05, we are unable to reject the null hypothesis that the distribution of defects in printed circuit boards is Poisson. The exact P-value computed from software is 0.0864.

hapter 9 Summary • You should be prepared to work any practice problems assigned: Cases 1-3 with three different alternatives • All other information is conceptual knowledge that can be questioned with multiple choice Name 3 ways to test if data is from a normal distribution 70 / 70

Chapter 9, case 1 pp

Monday, April 21, 2025 8:31 AM

QUESTION 1

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is thu=18.5 versus mu not equal to 18.5 using alpha=0.001. The sample statistics are n=28, xbar=18.94, sigma=3.595.

- O z0=0.6476
- O z0=0.9533
- O z0=3.427
- O z0=-0.6476

 $Z_0 = \frac{x - y_0}{\sigma / v n} = \frac{18.94 - 18.5}{3.595 / v a8}$ = 0-64764

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othesis for the mean of single sample with variance known. The number of the single sample with variance known at the single samp Construct the rejection region for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=18.5 versus mu not equal to 18.5 using alpha=0.001. The sample statistics are n=19, xbar=19.99, sigma=3.324.

O Reject H0 if |z0|>3.09

O Reject H0 if |z0|>3.291

Reject Ho if z0>3.09

O Reject Ho if z0>3.291 O Reject Ho if Z0<-3.291

O Reject Ho if Z0<-3.09

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Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=18.5 versus mu not equal to 18.5 using alpha=0.005. The sample statistics are n=29, xbar=18.36, sigma=4.851. The value of Z0 is -0.1554 and the rejection region is reject HO if |z0| > 2.807

- O Fail to reject H0
- O Reject H0

Zo = -.1554 reject Ho if /20/ >2.807

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15/-.155H) > 2.807 ? No -> fail to reject Ho

Q-value | mm | mm | - | zol | lt ol

QUESTION 7

Find the p-value for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=132.3 versus mu not equal to 132.3 using alpha=0.05. The sample statistics are n=19, xbar=136.01, sigma=16.636 and the value of the test statistic, Z0, is 0.9721.

- Op-value=0.332046
- Op-value=0.833977
- O p-value=0.166023

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for
$$H_1: N \neq 132.3$$

P-value = $2 \left[1 - \frac{1}{20} (1.971) \right]$

8:45 AM

QUESTION 9

Using the p-value from a test of hypothesis for the mean of single sample with variance known, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=25.8 versus mu not equal to 25.8 using alpha=0.005. The sample statistics are n=19, xbar=30.86, sigma=6.713. The results of hypothesis test include z0= 3.2856 and p-value=0.001018.

O Reject H0

Fail to reject HO

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d = .005

P-value = .001

if p-value < x , Reject + 6 ; s. ou/ < . cos ? yes, Reject Ho

Chapter 8, Case 1 lower

Monday, April 21, 2025 8:47 AM

QUESTION 1

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=25.8 versus mu less than 25.8 using alpha=0.01. The sample statistics are n=17, xbar=29.37, sigma=6.853.

O z0=8.856

O z0=-2.1479

O z0=2.1479

O z0=1.2923

 $\overline{Z}_{0} = \frac{\overline{\chi} - \gamma_{0}}{\sigma / \sigma \Lambda} = \frac{29.37 - 25.8}{6.853 / \sqrt{17}} + \frac{10.1 - 25.8}{11.1 + 12.8}$

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Construct the rejection region for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=25.8 versus mu less than 25.8 using alpha=0.1. The sample statistics are n=28, xbar=23.76, sigma=6.296.

O Reject H0 if z0>1.282

O Reject H0 if z0<-1.282

○ Reject Ho if |z0|>1.645

O Reject Ho if Z0<-1.645

for NK No , reject Hoif Zo <-Z=-Z.,
--1.28

= -1.282

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Reject Ho if Zoc -1.282

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=32.0 versus mu less than 32.0 using alpha=0.05. The sample statistics are n=10, xbar=31.29, sigma=2.72. The value of Z0 is -0.8254 and the rejection region is reject HO if z0<-1.645

O Fail to reject H0

Reject H0

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20 = -8 - 8254

2/ Réject Ho if Zo<-1.645 is -.8254</->

? No -> fail to Ho Reject Ho

Find the p-value for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.005. The sample statistics are n=28, xbar=17.63, sigma=4.618 and the value of the test statistic, 20, is -0.9969.

O p-value=0.841345

O p-value=0.158655

O p-value=0.317311

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Prulue for H,: P< Po is

Prulue = \$\overline{20}\$
= \$\overline(-1.00)\$
= \$158655

Using the p-value from a test of hypothesis for the mean of single sample with variance known, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=0.5 versus mu less than 0.5 using alpha=0.1. The sample statistics are n=10, xbar=0.46, sigma=0.057. The results of hypothesis test include z0= -2.2191 and p-value=0.01324.

O Reject H0

Fail to reject HO

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need & & p-value

< = 1) P- value = .01324

Rule: if p-value < x, Reject th

Is . C1324 2 . 1? Yes - Reject to