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Wednesday, April 16, 2025 8:01 AM





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 Chapter 9 slides Chapter 9 slides marked 	
Chapter 9 slides marked	
3/70	

troc	duction to Hypot	thesis Testing	
• In	onclusions about a po	nsists of methods used	d to make decisions or drav ation contained in a sampl
• In	ference is divided int Parameter estimatio Hypothesis testing	on (both point and inte	erval)
			4

verview of Statistical Hypotheses

- Many engineering problems require a decision to be made regarding some statement about a parameter
 - The statement is called a hypothesis
 - The decision-making process about the hypothesis is call hypothesis testing
- Statistical hypothesis testing is usually the data analysis stage of a comparative experiment
- A procedure leading to a decision about a particular hypothesis is called a test of hypothesis
- Testing the hypothesis involves taking a random sample, computing a test statistic from the sample data and then using the to make a

Hoi. N= value Hoi. is innomed

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Hi: SV = value

Hoi. N= value

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N = value

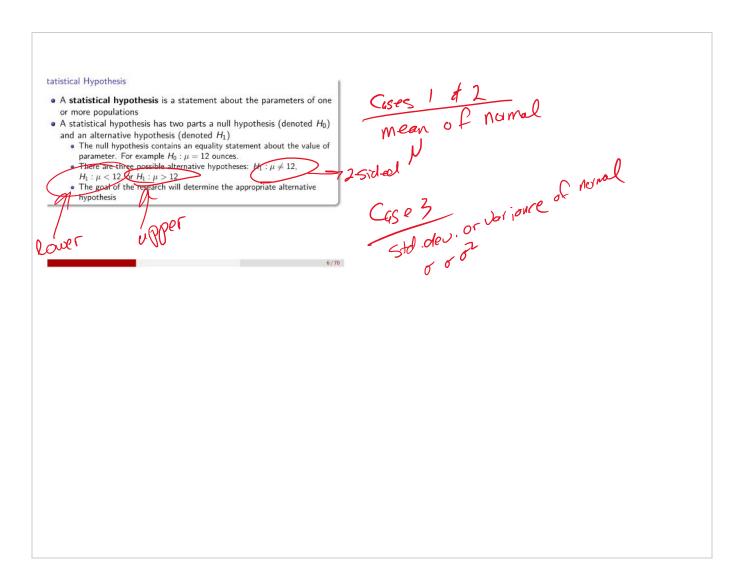
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Note

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skip this for a while

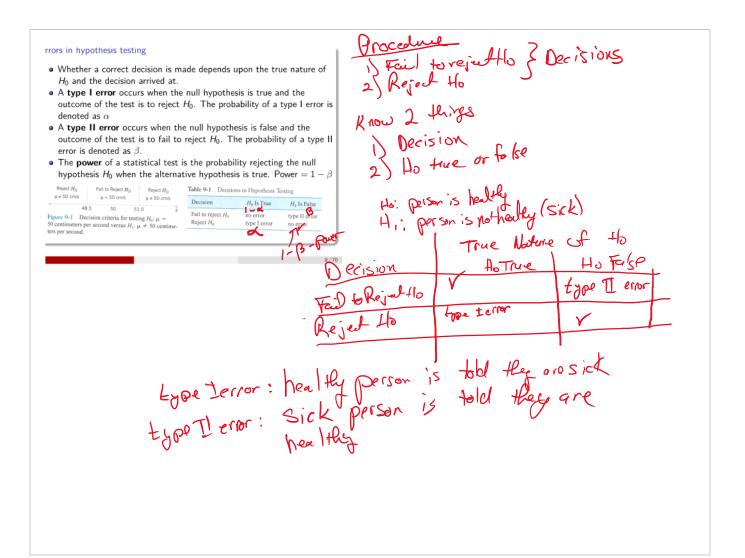


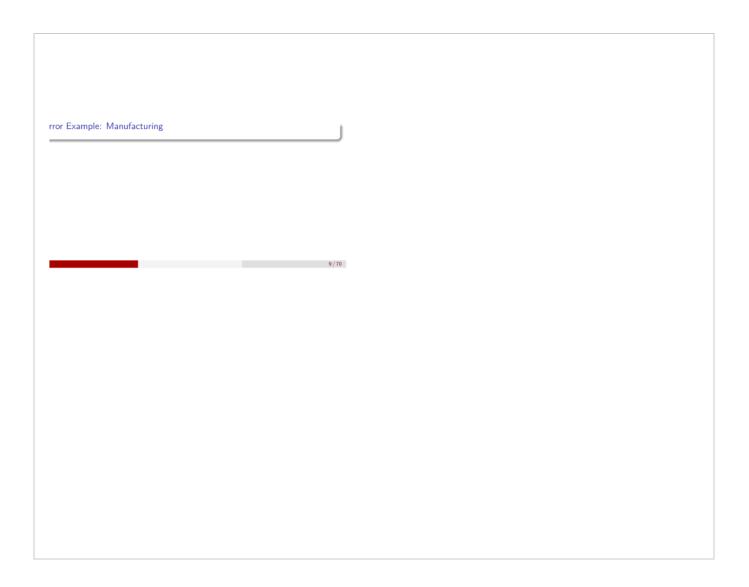
Chapter 8, Case 1 X-2-12 Tr & N < X+Zax Fr

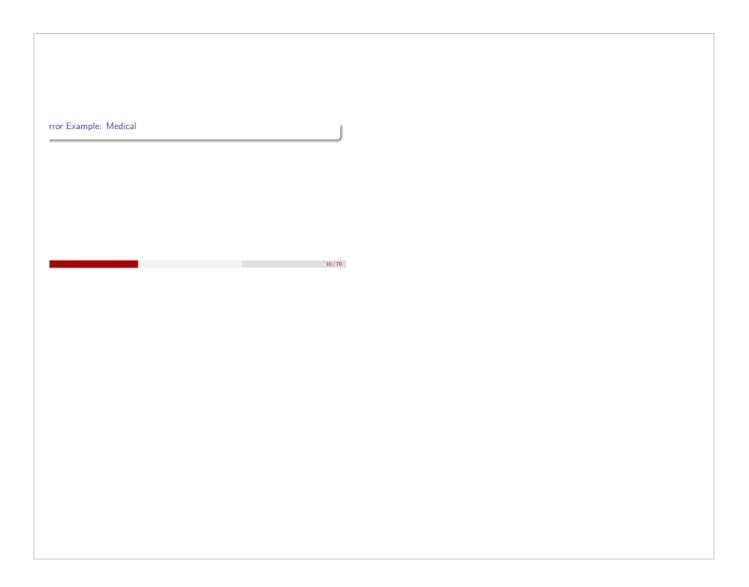
Summary of One-Sample Hypothesis-Testing Procedures

Case	Null Hypothesis	Test Statistic	Alternative Hypothesis
1.	$H_0: \mu = \mu_0$	$\bar{x} - \mu_0$	$H_1: \mu \neq \mu_0$
	σ^2 known	$z_0 = \frac{1}{\sigma / \sqrt{n}}$	$H_1: \mu > \mu_0$
			$H_1: \mu < \mu_0$

W 7 WA







neral Procedure for Hypothesis Testing he following sequence of steps is recommended • From the problem context, identify the parameter of interest, • State the null hypothesis, H₀, • Specify an appropriate alternative hypothesis, H₁, • Choose a significance level α • State an appropriate test statistic, • State the rejection region for the (test) statistic, • Compute any necessary sample quantities, substitute these into the equation for the test statistics, and compute that value, • Decide whether or not H₀ should be rejected and report in the problem context

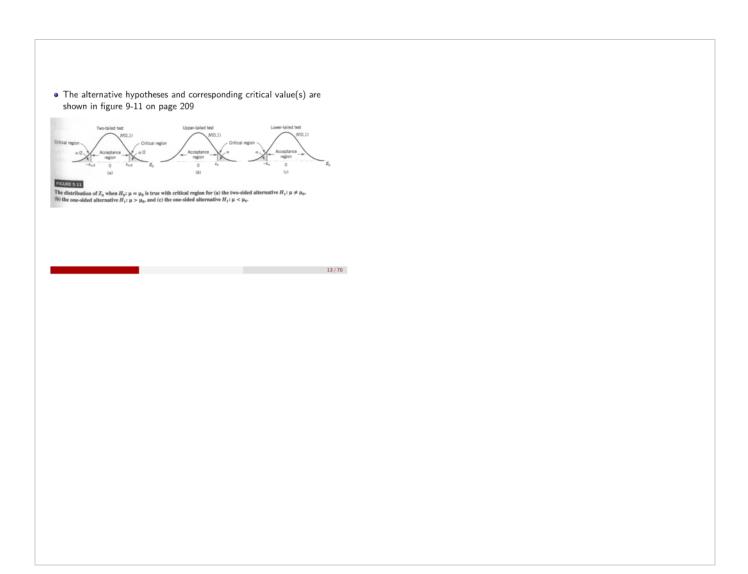
hapter 9, Case 1

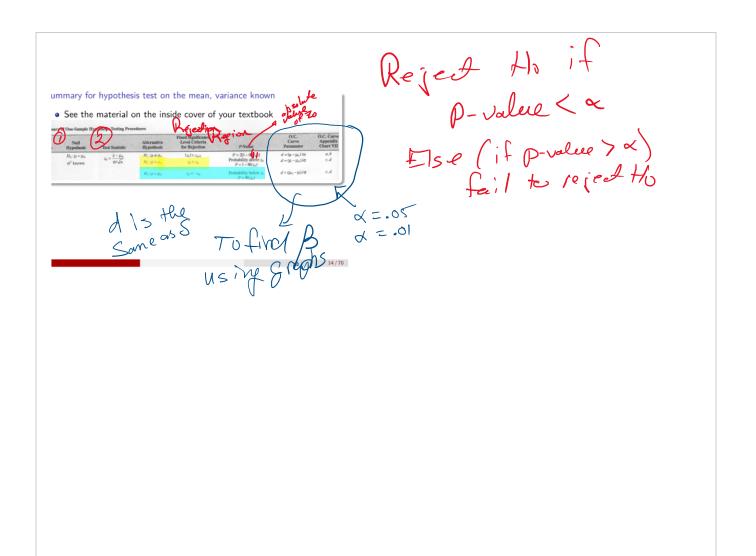
iference on the Mean of a population, variance known

- Assumptions:
 X₁, X₂,..., X_n is a random sample of size n from a population
 The population is normal, or if it is not normal, the conditions of the central limit theorem apply
- The parameter of interest is μ The null hypothesis is $H_0: \mu = \mu_0$
- The test statistic is

$$Z_0 = \frac{\overline{X} - \mu_0}{\sigma / \sqrt{n}}$$

nd has a standard normal distribution







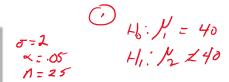
Example 11-1

The burning rate of a rocket propellant is being studied. Specifications require that the mean burning ate must be 40 cm/s. Furthermore, suppose that we know that the standard deviation of the burning ate is approximately 2 cm/s. The experimenter decides to specify a type I error probability α = 0.05, and he will base the test on a random sample of size n = 25. The hypotheses we wish to test are

 H_0 : $\mu = 40$ cm/s. H_1 : $\mu \neq 40$ cm/s.

Twenty-five specimens are tested, and the sample mean burning rate obtained is $\bar{x} = 41.25$ cm/s.

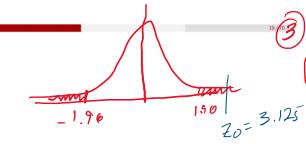
Source: Himes. Mortgonery, Goldsman, Borron (2003). Probability and Statistics in Enghamming, 4th ed.



Tot Statistic

Zo= X-1/0 = 41.25-40

2/025
3.125



Rejection Region (tied to 41)

Reject to if |Zo| > Za/2

lasical dist

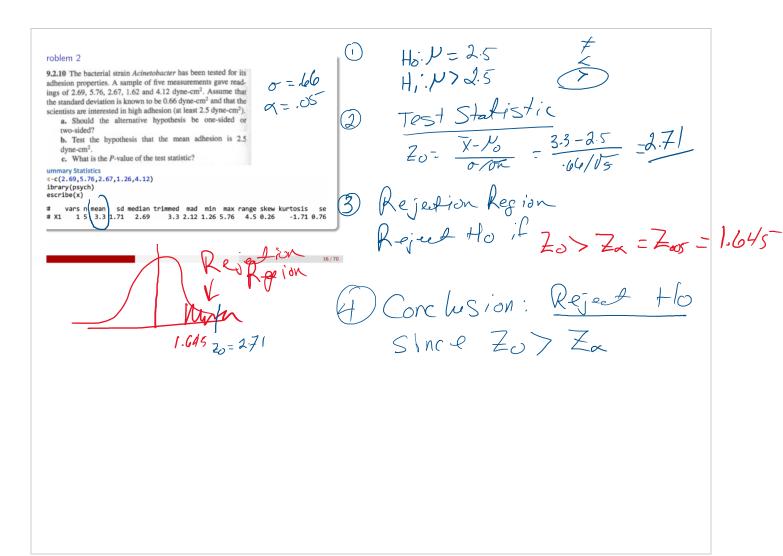
Gonclusion: =1.96

Since Zo > Zerz, we reject

the null hypothesis.

The mean burn is different from

HO CM/S at an .05 significance level



onnection between Hypothesis Tests and CI

- There is a close connection between confidence intervals and hypothesis tests
- Consider a 100(1 - $\alpha)\%$ confidence interval on μ and a hypothesis test of size α shown below

 $H_0: \mu = \mu_0$ $H_1: \mu \neq \mu_0$

- \bullet The conclusion to reject H_0 will be reached if μ_0 is not contained within the confidence interval
- If μ_0 is within the confidence interval, we fail to reject H_0
- The 100(1-lpha)% confidence interval on μ is the acceptance region

Confidence interval is the Same as the acceptance rgion in a Statistical hypothesis test

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-values

• Is a widely used alternative to the traditional hypothesis test

ullet Definition: The p-value is the smallest level of significance that would lead to reject of the null hypothesis H_0 with the given data

· Formulas are given below

$$P = \left\{ \begin{array}{ll} 2[1-\Phi(|z_0|)] & \text{for a two-tailed test} \\ 1-\Phi(z_0) & \text{for a upper-tailed test} \\ \Phi(z_0) & \text{for a lower-tailed test} \end{array} \right.$$

ullet Usage: if $p ext{-value}<lpha$ then the conclusion is reject H0, otherwise fail to reject H0

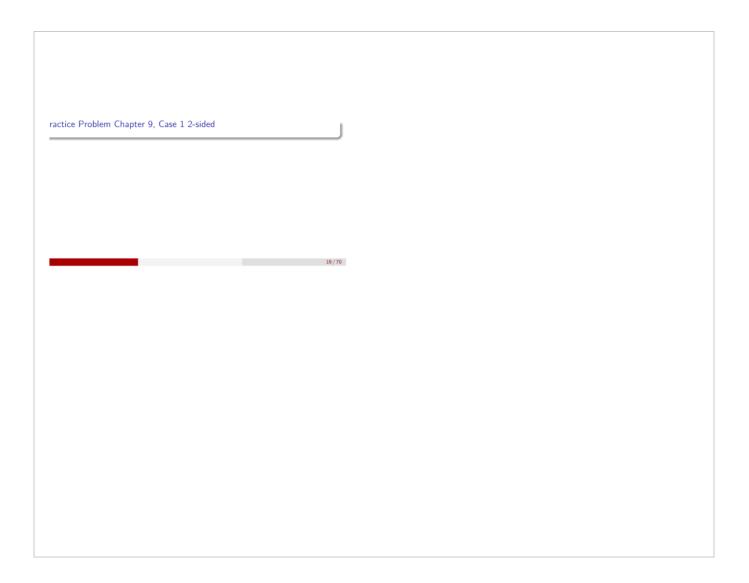
Test 1 - Continuation (1772.5)

Test2

Zo=1.64

Zo=1.65

Conclusion: fail Conclusion: reject
to reject to the





ractice Problem Chapter 9, Case 1 Upper

$$\beta = f(s, s, a)$$
ype II error and sample size for a two-tailed test

• Probability of type II error for the two-tailed test

$$\beta = \Phi\left(z_{\alpha/2} - \frac{\delta\sqrt{n}}{\sigma}\right) - \Phi\left(-z_{\alpha/2} - \frac{\delta\sqrt{n}}{\sigma}\right)$$

here $\mu=\mu_0+\delta$ • The sample to detect a difference between the true and hypothesized mean of δ with power at least $1-\beta$ is

$$n pprox rac{(z_{lpha/2} + z_{eta})^2 \sigma^2}{\delta^2}$$

here $\delta = \mu - \mu_{\rm 0}$

ype II error and sample size for the one-tailed tests

• For an upper-tailed test

$$\beta = \Phi \left(z_{\alpha} - \frac{\delta \sqrt{n}}{\sigma} \right)$$

• For a lower-tailed test

$$\beta = 1 - \Phi \left(-z_{\alpha} - \frac{\delta \sqrt{n}}{\sigma} \right)$$

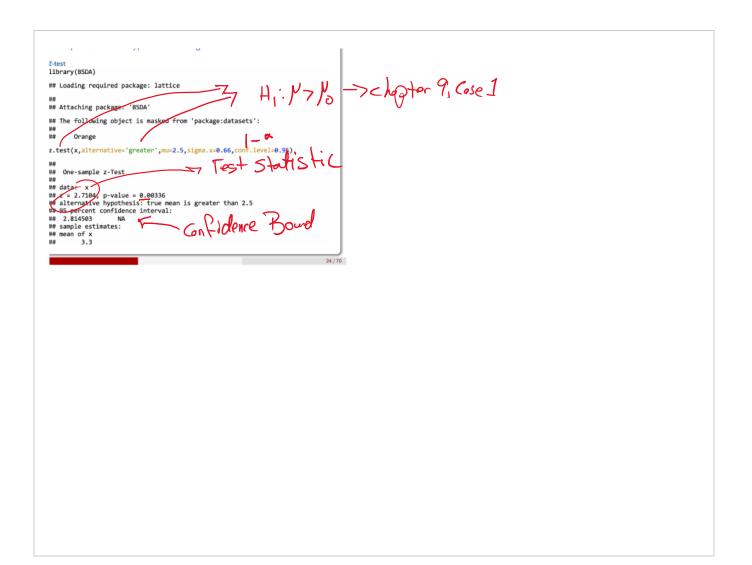
• The sample size required to detect a difference between the true mean and hypothesized mean of δ with power at least $1-\beta$ is

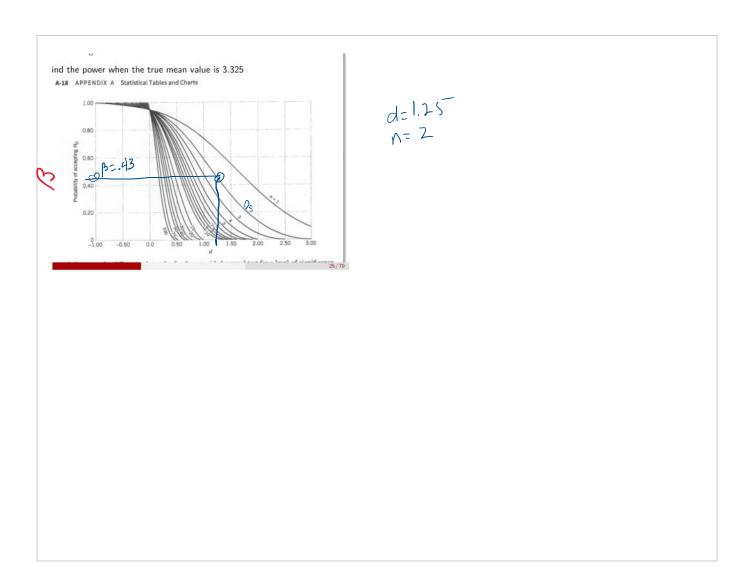
$$n = \frac{(z_{\alpha} + z_{\beta})^2 \sigma^2}{\delta^2}$$

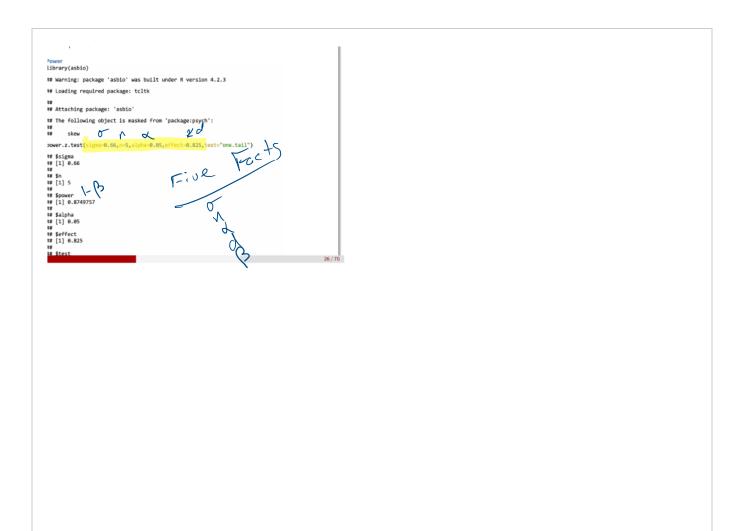
n is not an integer, round up to the nearest integer

Some thing stated

......





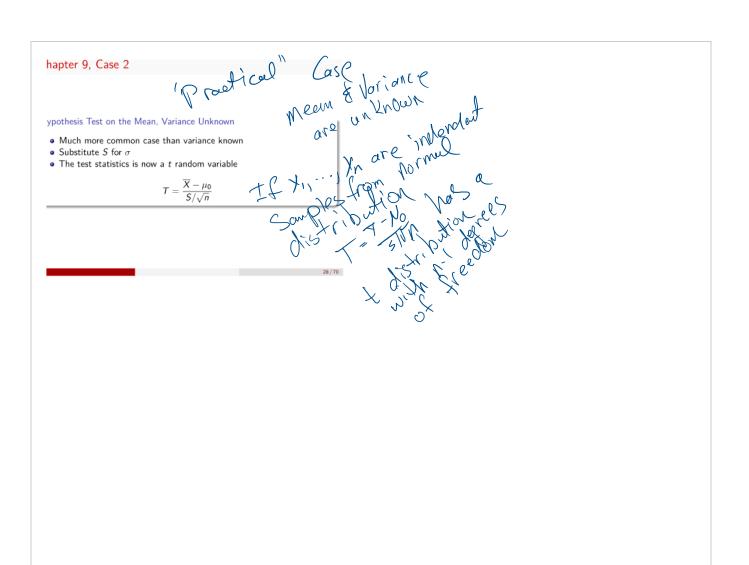


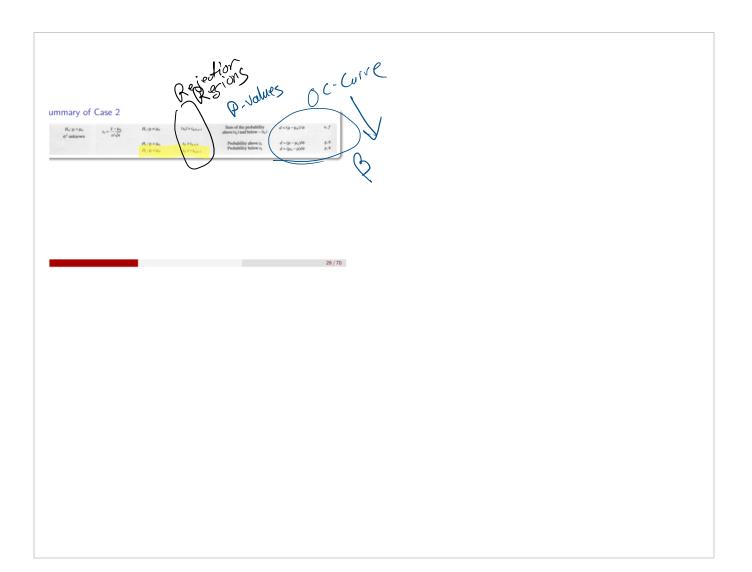
ype II Error Rate and Sample Size

- You will not be required to calculate or use OC-curves
- You must understand the concept and be able to correctly identity type table 9-1 decision Home table

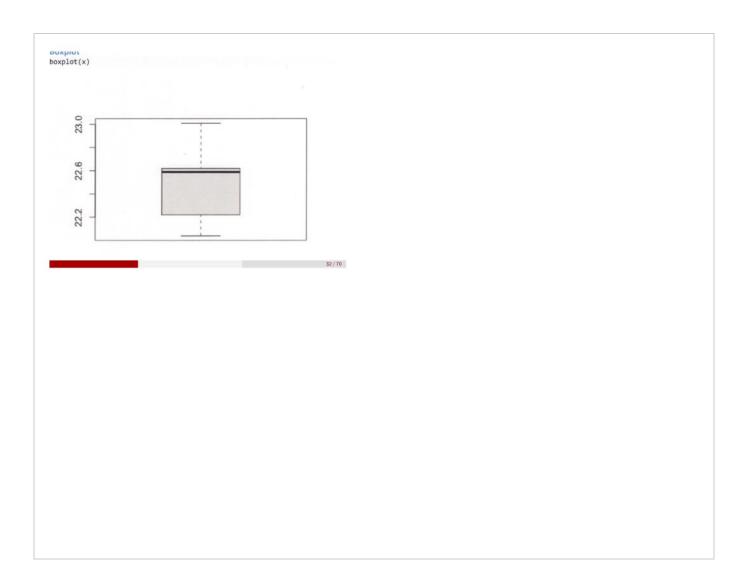
 27/70 I and type II error

Chapter 9 Page 26





Ho: N=22.5 HI: N + 22.5 Tost Stadistic Lo= X-No (No=22.5, n=5) 0 roblem 9.3.6 9.3.6 An article in the ASCE Journal of Energy Engineering (1999, Vol. 125, pp. 59-75) describes a study of the thermal inertia properties of autoclaved aerated concrete used as a building material. Five samples of the material were tested in a structure, and the average interior temperatures (°C) reported were as follows: 23.01, 22.22, 22.04, 22.62, and 22.59. a. Test the hypotheses H_0 : $\mu=22.5$ versus H_1 : $\mu\neq22.5$, using $\alpha=0.05$. Find the P-value. b. Check the assumption that interior temperature is normally distributed. -22.5-225 _E0.0 c. Compute the power of the test if the true mean interior temperature is as high as 22.75. d. What sample size would be required to detect a true mean Rejection Region interior temperature as high as 22.75 if you wanted the power of the test to be at least 0.9? e. Explain how the question in part (a) could be answered by constructing a two-sided confidence interval on the mean Reject to if Ital> tax2n-1=t-025,4 A Econchesion
Fail to reject to -2.776 L502.776





```
ypothesis Test Using R

Lesst
Litest(x,a)servative="two.sided",mu-22.5, conf. lines|-0.95)

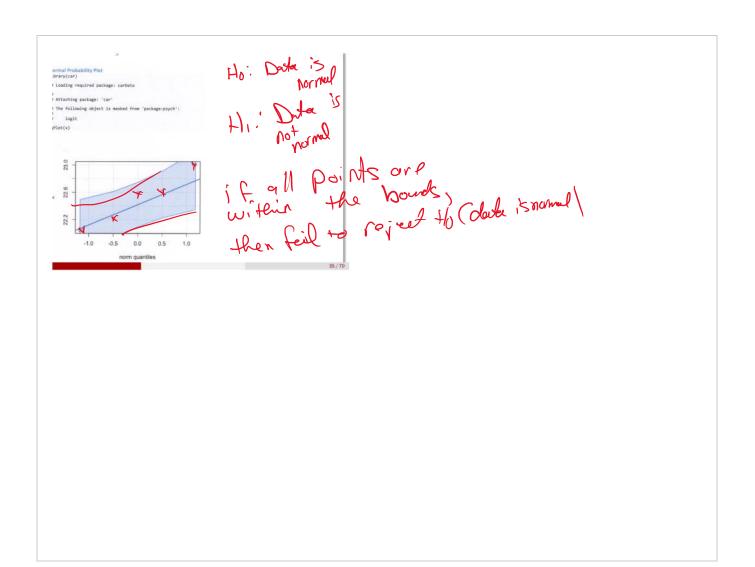
##

## Grows Sample t-test
## data: x

## = 0.023642, of = 4, p-value = 0.9021

## alternative hypothesis: true mean is not equal to 22.5

## 35 percent confidence introduce confidence confiden
```



-values	
More difficult to calculate since the t-tables only contain a few	
The state of the s	
quantiles	
ullet Can use tables to generate bounds on the p -value	
C C C C C C C C C C C C C C C C C C C	
Software will provide p-values	
36/70	

```
-values from R

Lest

t.test(x,s)servative="two.sided",mu>22.5,cod.level=0.95)

##

## One Sample t-test

## data: ,

## alternative hypothesis: true seen is not equal to 22.5

## 35 percent confidence interval:

## 22.0025 22.9675

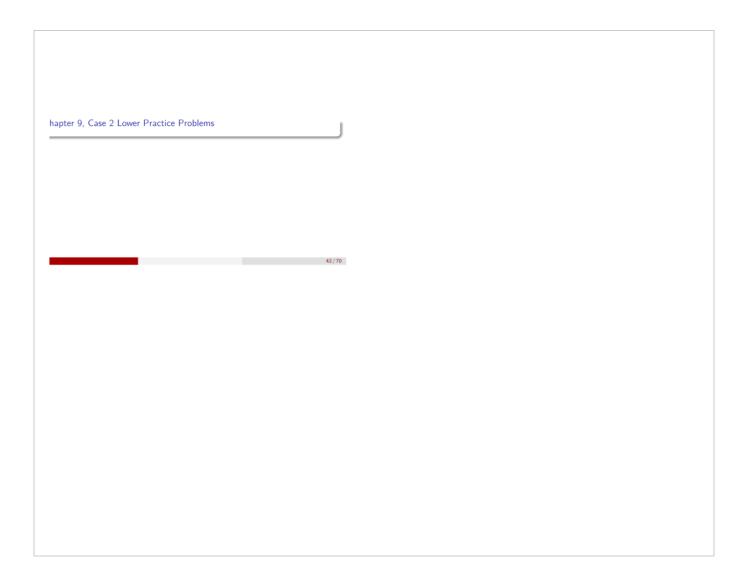
## 22.0026

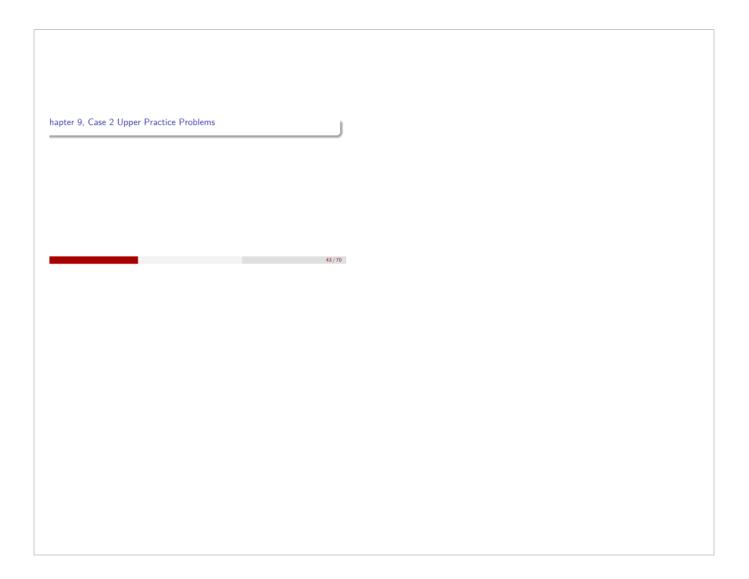
## 22.0026
```











ase 3. Hypothesis Test on Variance of Normal Population

 \bullet The test statistics is a χ^2 random variable

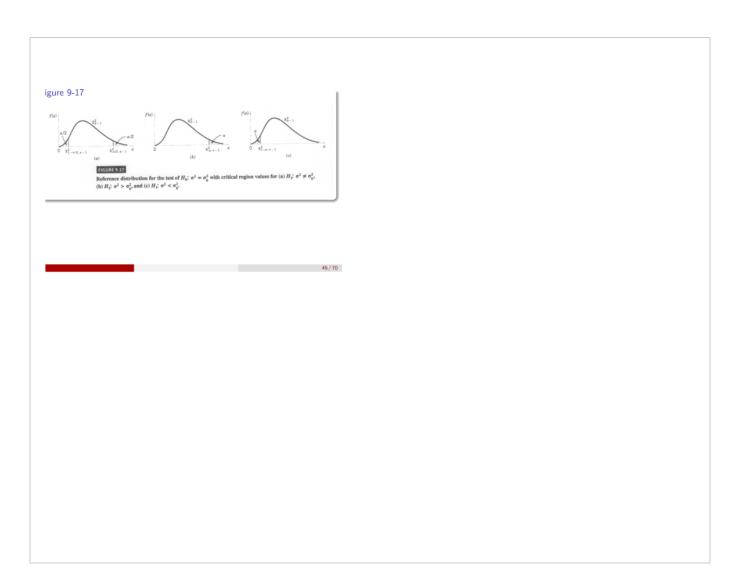
$$\chi_0^2 = \frac{(n-1)S^2}{\sigma_0^2}$$

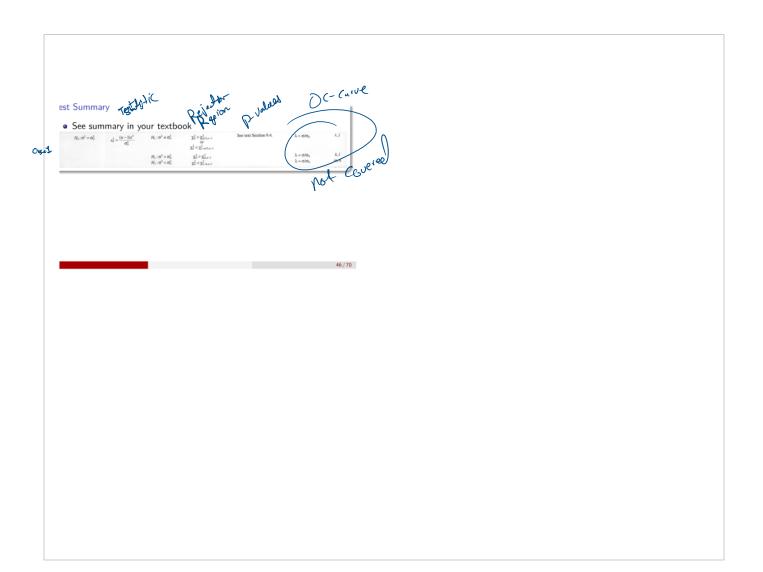
lover x/2

of a Normal Distribution	Null hypothesis: H_0 : $\sigma^2 = \sigma_0^2$ Test statistic: $\chi_0^2 = \frac{(n-1)S^2}{\sigma_0^2}$	
	Alternative Hypothesis	Rejection Criteria
Hg: 0+00	$H_1: \sigma^2 \neq \sigma_0^2$ $H_1: \sigma^2 > \sigma_0^2$	$\chi_0^2 > \chi_{\alpha/2,e-1}^2$ or $\chi_0^2 < \chi_{1-\alpha/2,e-1}^2$ $\chi_0^2 > \chi_{\alpha,e-1}^2$
4,:0-75	$H_1: \sigma^2 < \sigma_0^2$	$\chi_0^2 < \chi_{1-\alpha,n-1}^2$
41,:0200		of the second of the second

The table below summarizes the three possible hypothesis tests. The ejection regions are clearly shown in Figure 9-17 on page 222

Chapter 9 Page 43





roblem 7.108

roblem taken from Ostle, Turner, Hicks and McElrath (1996). Engineering tatistics: The Industrial Experience. Duxbury Press.

Incoming coal at a coking plant is routinely analyzed for sulfur content (in percent). In the past, samples taken from barges loaded with coal from a particular mine have had a variance of 0.000196. When a new analyst was hired, the results of an assay of coal from the mine produced percentages of 0.83, 0.79, 0.77, 0.81, and 0.80.

of 0.83, 0.79, 0.77, 0.81, and 0.80.
(a) Using α = 0.05, does the sample variance provide sufficient evidence to conclude that the results from the new analyst indicate more variability than in the past? State all assumptions.
(b) Based on these data, is an assumption of normality reasonable? Justify by using a normal quantile plot and a formal test such as the Shapiro-Wilk W test.

Ho: 02 = 0.000196 H: 02 > 0,000196 Test Stulistic

 $\chi_{0}^{L} = \frac{(n \cdot 1/s^{2})^{2}}{\sigma_{0}^{2}} = \frac{(n \cdot 1/s^{2})^{2}}{(5 \cdot 1)(.012361)^{2}} = \frac{(5 \cdot 1)(.012361)^{2}}{(0.204)}$ $= \frac{(5 \cdot 1)(.012361)^{2}}{(0.204)}$

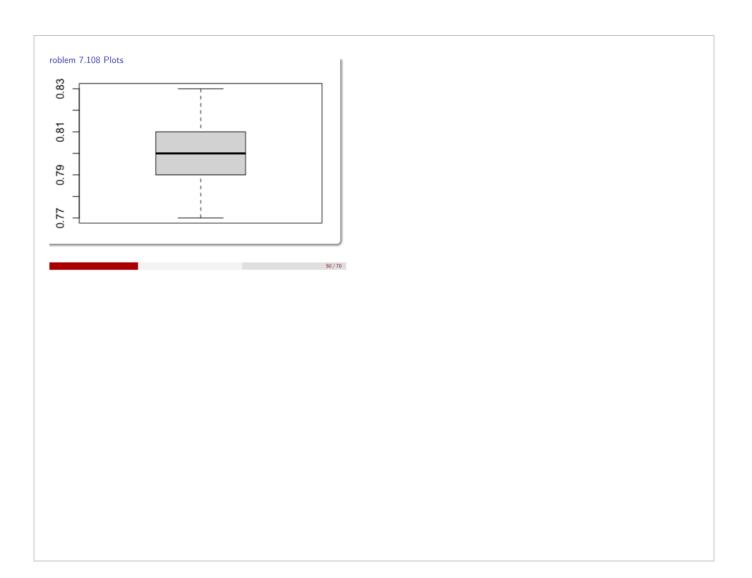
Reject Ho if XO > X2 x 1/1-1

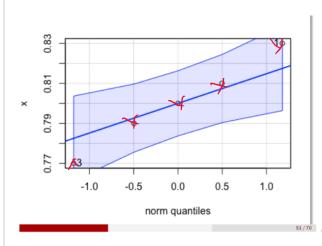
χ² > χ² = 9.49

Conclusion: Since 72 79.49, we reject Ho









Asi, deba is normal Hi. datais Not normal

Reject to if one or more points are outside the Confidence (x : 05)

51/10 Conclusion: fail to reject

Ho - I data is from normal distribution



-values
• Very similar to the case for the mean of a normal population with variance unknown • Difficult to calculate since the χ^2 -tables only contain a few quantiles • Can use tables to generate bounds on the p -value • Software will provide p -values
53/70

VarTest(x,alternative="greater",conf.level=0.95,sigma.squared=0.000196)

Results of Hypothesis Test
Null Hypothesis: variance = 0.000196

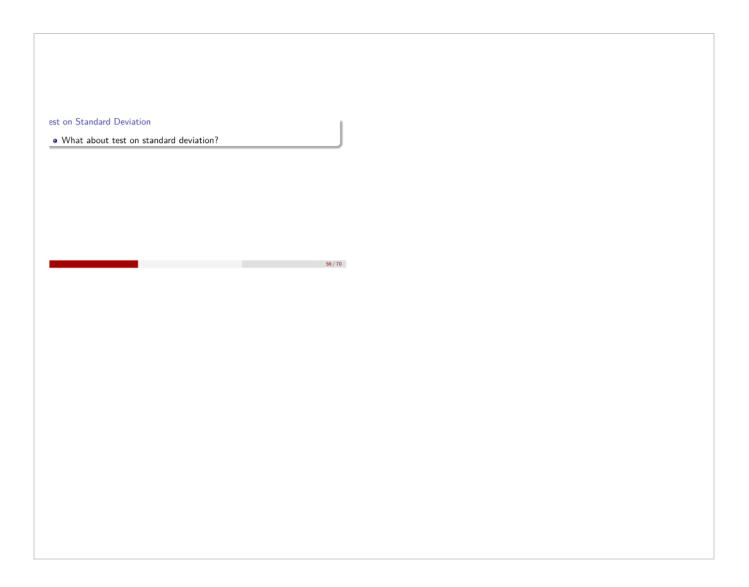
Alternative Hypothesis: True variance is greater than 0.000196

Test Name: Chi-Squared Test on Variance
Estimated Parameter(s): variance = 5e-04

Data: x

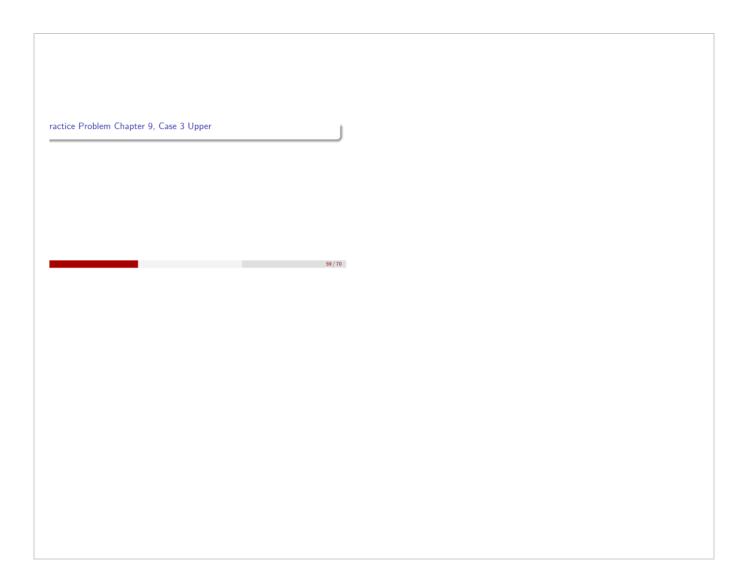
Test Statistic: Chi-Squared = 10.20408
Test Statistic Parameter: df = 4
P-value: 0.03712675
95% Confidence Interval: LCL = 0.0002107986
UCL = Inf

ower Calculations	
 Can be done with OC curves found in Table VIIi-n 	
Can be done in software such as R	
Can be done in sorthare such as it	
55/70	
35/10	

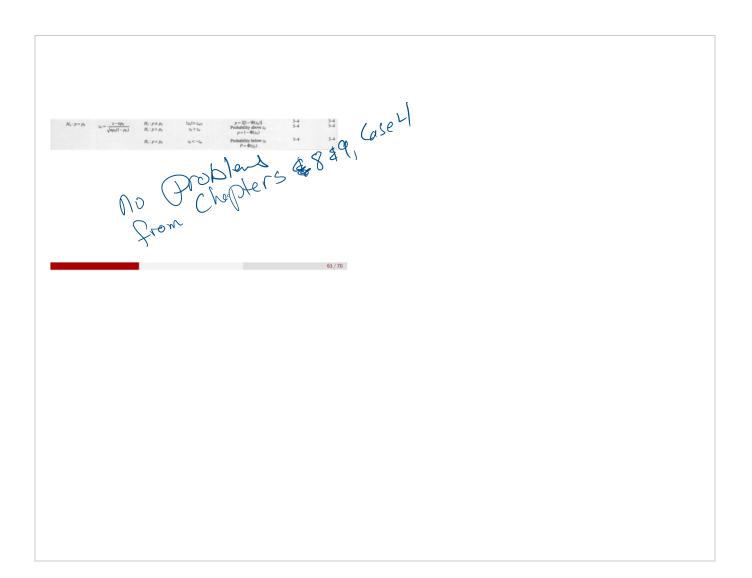




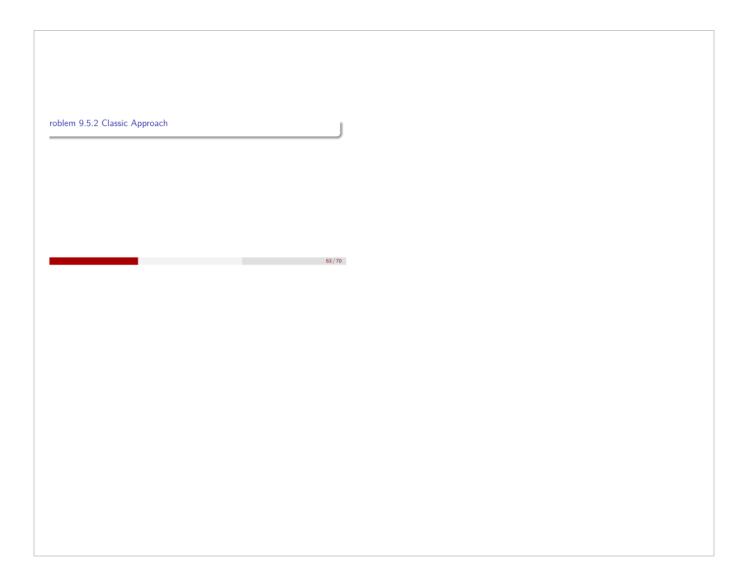




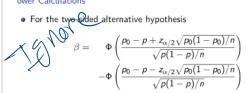
ase 4. Hypothesis Test on a Population Proportion Prom Binomial Distribution The test statistics for the hypothesis test is The test statistics for the hypothesis test is







ower Calculations



ullet If the alternative is $H_1:
ho <
ho_0$

$$\beta = 1 - \Phi\left(\frac{\rho_0 - p - z_\alpha \sqrt{\rho_0(1-\rho_0)/n}}{\sqrt{\rho(1-\rho)/n}}\right)$$

 \bullet and finally if the alternative hypothesis is ${\it H}_1: \rho > {\it p}_0$

$$\beta = \Phi\left(\frac{p_0 - p + z_\alpha \sqrt{p_0(1 - p_0)/n}}{\sqrt{p(1 - p)/n}}\right)$$

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ample Size
• Sample size requirements to satisfy type $\mathrm{II}(\beta)$ error constraints for a two-tailed hypothesis test is given by

$$n = \left[\frac{z_{\alpha/2}\sqrt{p_0(1-p_0)} + z_\beta\sqrt{p(1-p)}}{p-p_0}\right]^2.$$

- For a sample size for a one-sided test substitute z_{α} for $z_{\alpha/2}.$ Problem 9.95

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esting for Goodness of Fit • Material is presented in section 9-7 of your textbook • Procedure determines if the sample data is from a specified underlying distribution • Procedure uses a χ^2 distribution • Example 9-12 presents a χ^2 goodness of fit test for a Poisson example • Example 9-13 presents a χ^2 goodness of fit test for a normal example

rocedure

- Collect a random sample of size n from a population with an unknown distribution.
- $oldsymbol{\circ}$ Arrange the n observations in a frequency distribution containing k classes
- O Calculate the observed frequency in each class Oi,
- From the hypothesized distribution, calculate the expected frequency in class i, denoted E_i (if E_i is small combine classes)
- O Calculate the test statistic

$$\chi_0^2 = \frac{\sum_{i=1}^k (O_i - E_i)^2}{E_i}$$

• Reject the null hypothesis if the calculated value of the test statistic $\chi_0^2 > \chi_{\alpha,k-\rho-1}^2$ where ρ is the number of parameters in the hypothesized distribution

Brief Overview

Shorted vous

Coleman Shortest (SS)

From observed Supples

A Calculate with Farometer

Shortest (SS)

From observed Supples

A Calculate with Farometer

Shortest (SS)

Values with Farometer

Shortest (SS)

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xample 9.12, part 1

EXAMPLE 9.12 | Printed Circuit Board Defects-

Poisson Distribution The number of defects in printed circuit boards is hypothesized to follow a Poisson distribution. A random sample of n=60 printed circuit boards has been collected, and the following number of defects observed.

Number of Defects	Observed Frequenc
0	32
1	15
2	9
¥ 72	4

The mean of the assumed Poisson distribution in this example is unknown and must be estimated from the sample data. The

estimate of the mean number of defects per board is the sample average, that is, (32 · 0 + 15 · 1 + 9 · 2 · 4 + 3)60 = 0.75. From the Poisson distribution with parameter 0.75, we may compute p₁, the theoretical, hypothesized probability associated with the th class interval. Because each class interval corresponds to a particular number of defects, we may find the p₁ as follows:

$$p_1 = P(X = 0) = \frac{e^{-0.75}(0.75)^0}{0!} = 0.472$$

$$p_2 = P(X = 1) = \frac{e^{-0.75}(0.75)^4}{1!} = 0.354$$

$$p_3 = P(X = 2) = \frac{e^{-0.25}(0.75)^2}{2!} = 0.133$$

$$p_4 = P(X \geq 3) = 1 - (p_1 + p_2 + p_3) = 0.041$$

	nes the probabi	puted by multiplying the illities p_i . That is, $E_i = np_i$.	 Null hypothesis: H₀: The form of the distribution of defects is Poisson. Alternative hypothesis: H₁: The form of the distribution of the distribution of the distribution.
Number of Defects	Probability	Expected Frequency	bution of defects is not Poisson. $\stackrel{k}{\leftarrow} (O_i - E_i)^i$
0	0.472	28.32	4. Test statistic: The test statistic is $\chi_0^2 = \sum_{i=1}^k \frac{(O_i - E_i)^i}{E_i}$
1	0.354	21.24	5. Reject Ha if: Because the mean of the Poisson distri
2	0.133	7.98	bution was estimated, the preceding chi-square statistic
3 (or more)	0.041	2.46	will have $k - p - 1 = 3 - 1 - 1 = 1$ degree of freedom Consider whether the P-value is less than 0.05.

Because the expected frequency in the last cell is less than 3,
we combine the last two cells:
6. Computations:

Number of Defects	Observed Frequency	Expected Frequency
0	32	28.32
1	15	21.24
2 (or more)	13	10.44

The seven-step hypothesis-testing procedure may now be applied, using $\alpha=0.05$, as follows:

Parameter of interest: The variable of interest is the form of the distribution of defects in printed circuit boards.

$$\chi_0^2 = \frac{(32 - 28.32)^2}{28.32} + \frac{(15 - 21.24)^2}{21.24} + \frac{(13 - 10.44)^2}{10.44}$$

= 2.94

= 2.94

7. Conclusions: We find from Appendix Table III that $\chi^2_{0.01} = 2.71$ and $\chi^2_{0.01} = 3.84$. Because $\chi^2_0 = 2.94$ lies between these values, we conclude that the P_v -value is between 0.05 and 0.10. Therefore, because the P_v -value exceeds 0.05, we are unable to reject the null hypothesis that the distribution of defects in printed circuit boards is Poisson. The exact P_v -value computed from software is 0.0864.

4-28 Atterdace: 1-C

hapter 9 Summary

- You should be prepared to work any practice problems assigned: Cases 1-3 with three different alternatives
- All other information is conceptual knowledge that can be questioned with multiple choice

with multiple choice
Name 3 ways to test if data is from a normal distribution

The probability Platting

The production of the probability probabilit

Chapter 9, case 1 2-sided

Monday, April 21, 2025 8:31 AM

QUESTION 1

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is thu=18.5 versus mu not equal to 18.5 using alpha=0.001. The sample statistics are n=28, xbar=18.94, sigma=3.595.

- O z0=0.6476
- O z0=0.9533
- O z0=3.427
- O z0=-0.6476

 $Z_0 = \frac{x - y_0}{\sigma / v n} = \frac{18.94 - 18.5}{3.595 / v a8}$ = 0-64764

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Chapter 9 Page 70

Chapter 9, Case 1 2-sided

Monday, April 21, 2025 8:33 AM

OI			

othesis for the mean of single sample with variance known. The null hypothesis is

Hi. $V \pm 18-5$ \longrightarrow Reject ± 100 if 1201 > 232 ± 2.005 ± 2.005 Construct the rejection region for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=18.5 versus mu not equal to 18.5 using alpha=0.001. The sample statistics are n=19, xbar=19.99, sigma=3.324.

O Reject H0 if |z0|>3.09

O Reject H0 if |z0|>3.291

Reject Ho if z0>3.09

O Reject Ho if z0>3.291

O Reject Ho if Z0<-3.291

O Reject Ho if Z0<-3.09

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Chapter 9, Case 1 2-sided

Monday, April 21, 2025 8:37 AM

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Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=18.5 versus mu not equal to 18.5 using alpha=0.005. The sample statistics are n=29, xbar=18.36, sigma=4.851. The value of Z0 is -0.1554 and the rejection region is reject HO if |z0| > 2.807

O Fail to reject H0

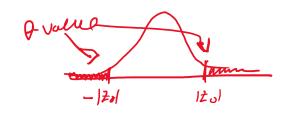
O Reject H0

Zo = -.1554 reject Ho if /20/ >2.807

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15/-.155H) > 2.807 ? No -> fail to reject Ho

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QUESTION 7

Find the p-value for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=132.3 versus mu not equal to 132.3 using alpha=0.05. The sample statistics are n=19, xbar=136.01, sigma=16.636 and the value of the lest statistic, Z0, is 0.9721.

- Op-value=0.332046
- Op-value=0.833977
- O p-value=0.166023

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for
$$H_1: N \neq 132.3$$
 $P-value = 2 \left[1-\frac{1}{20}(120)\right]$

$$= 2 \left[1-\frac{1}{20}(1.971)\right]$$

$$= 2 \left[1-\frac{1}{20}(1.971)\right]$$

$$= 2 \left[1-\frac{1}{20}(1.9771)\right]$$

$$= 2 \left[1-\frac{1}{20}(1.9771)\right]$$

$$= 33205$$

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QUESTION 9

Using the p-value from a test of hypothesis for the mean of single sample with variance known, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=25.8 versus mu not equal to 25.8 using alpha=0.005. The sample statistics are n=19, xbar=30.86, sigma=6.713. The results of hypothesis test include z0= 3.2856 and p-value=0.001018.

O Reject H0 Fail to reject HO

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X = .005

P-value = .001

if p-value < x , Reject + 6 ; s. ou/ < . ous ? yes, Reject Ho

Monday, April 21, 2025 8:47 AM

QUESTION 1

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=25.8 versus mu less than 25.8 using alpha=0.01. The sample statistics are n=17, xbar=29.37, sigma=6.853.

O z0=8.856

O z0=-2.1479

O z0=2.1479

O z0=1.2923

 $\overline{Z}_{0} = \frac{\overline{\chi} - \gamma_{0}}{\sigma / \sigma \Lambda} = \frac{29.37 - 25.8}{6.853 / \sqrt{17}} + \frac{10.1 - 25.8}{11.1 + 12.8}$

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QUESTION 3

Construct the rejection region for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=25.8 versus mu less than 25.8 using alpha=0.1. The sample statistics are n=28, xbar=23.76, sigma=6.296.

O Reject H0 if z0>1.282

O Reject H0 if z0<-1.282

O Reject Ho if |z0| >1.645

O Reject Ho if Z0<-1.645

for NK No s reject Hoil Zo <-Z=-Z.,

= -1.282

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Reject Ho if Zoc -1.282

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QUESTION 5

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=32.0 versus mu less than 32.0 using alpha=0.05. The sample statistics are n=10, xbar=31.29, sigma=2.72. The value of Z0 is -0.8254 and the rejection region is reject HO if z0<-1.645

○ Fail to reject H0

Reject H0

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20 = -8254 Reject to if 20< -1.645 is -.8254 < -1.645 ? No -> fail to Reject Ho

Monday, April 21, 2025 8:56 AM

QUESTION 7

Find the p-value for a test of hypothesis for the mean of single sample with variance known. The null hypothesis is mu=18.5 versus mu less than 18.5 using alpha=0.005. The sample statistics are n=28, xbar=17.63, sigma=4.618 and the value of the test statistic, 20, is -0.9969.

O p-value=0.158655

O p-value=0.317311

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Prulue for H,: P< Po is

Prulue = \$\overline{20}\$
= \$\overline(-1.00)\$
= \$158655

Monday, April 21, 2025 8:59 AM

QUESTION 9

Using the p-value from a test of hypothesis for the mean of single sample with variance known, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=0.5 versus mu less than 0.5 using alpha=0.1. The sample statistics are n=10, xbar=0.46, sigma=0.057. The results of hypothesis test include 20=-2.2191 and p-value=0.01324.

O Reject H0

Fail to reject HO

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need & & p-value

Rule: if p-value < x , Reject the

IS . C1324 2 . 1? Yes - Reject to

Attendance

Chapter 9 Page 79

Wednesday, April 23, 2025 8:48 AM

QUESTION 1

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=12.0 versus mu not equal to 12.0 using alpha=0.2. The sample statistics are n=18, xbar=12.51, S=2.177.

O t0=-0.9939 Q t0=0.9939

O t0=4.2168

 $L_0 = \frac{12.51 - 12}{5/100} = \frac{12.51 - 12}{2.177/187} = 0.9939/$

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Wednesday, April 23, 2025 8:50 AM

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Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=132.3 versus mu not equal to 132.3 using alpha=0.05. The sample statistics are n=7, xbar=144.04, S=18.877.

- O Reject Ho if t0>1.943
- O Reject Ho if t0>2.447
- O Reject H0 if |t0|>1.943
- O Reject Ho if t0<-2.447
- Reject Ho if t0<-1.943
- O Reject H0 if |t0|>2.447

Reject the +1 ample statistics are n=7, xbar=144.04, S=18.8//.

Reject the +1 and +1 are +1 and +1 are +1 a

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Wednesday, April 23, 2025

QUESTION 5

Which is the correct conclusion for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis mu=132.3 versus mu not equal to 132.3 using alpha=0.02. The sample statistics are n=25, xbar=136.13, S=20.366. The value of t0 is 0.9403 and the rejection region is reject HO if

Fail to reject H0

Reject H0

) to = .9403

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The jest Hoif $|t_0| > 2.492$ is |.9403| > 2.492? No, fail to reject the

Wednesday, April 23, 2025 8:54 AM

QUESTION 7

Using the p-value from a test of hypothesis for the mean of single sample with variance unknown, determine the correct conclusion for the hypothesis test. The null hypothesis is mu=132.3 versus mu not equal to 132.3 using alpha=0.1. The sample statistics are n=5, xbar=134.52, S=11.084. The results of hypothesis test include t0= 0.4479 and p-value=0.677413.

Fail to reject H0

O Reject H0

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p-value = .6774

Rule: if P-value < x, reject to

; S. ob7742.1? no > feil to

reject to

Wednesday, April 23, 2025 8:56 AM

QUESTION 1	1	ľ	
	/	9	

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=0.5 versus mu less than 0.5 using alpha=0.0025. The sample statistics are n=19, xbar=0.51, S=0.053.

O t0=-0.8224

O t0=0.8224

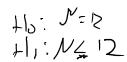
O t0=67.6397

Lo = x-10 = 151-5 = 0.82243

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Wednesday, April 23, 2025

8:58 AM





QUESTION 3

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=12.0 versus mu less than 12.0 using alpha=0.025. The sample statistics are n=18, xbar=11.57, S=2.025.

- Reject Ho if |t0|>2.458
- O Reject H0 if t0<-2.11
- Reject Ho if t0<-2.458
- O Reject Ho if t0>2.11
- O Reject H0 if |t0|>2.11

Rejert

40

, _

to<-ta,n-1

=-t.025/7 =-2.110

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Chapter 9, Case 2 Upper

Wednesday, April 23, 2025 9:03 AM

QUESTION 1

Calculate the test statistic for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=18.5 versus mu greater than 18.5 using alpha=0.005. The sample statistics are n=10, xbar=17.04, S=5.036. t0=-2.8991 t0=-0.9168 t0=-0.9168 t0=-0.5757

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Chapter 9, Case 2 Upper

Wednesday, April 23, 2025 9:05 AM

QUESTION 3

Construct the rejection region for a test of hypothesis for the mean of single sample with variance unknown. The null hypothesis is mu=12.0 versus mu greater than 12.0 using alpha=0.005. The sample statistics are n=2, xbar=13.62, S=1.953.

- Reject H0 if t0>63.657
- O Reject Ho if |t0|>127.321
- O Reject H0 if |t0|>63.657
- O Reject Ho if t0<-127.321
- O Reject Ho if t0<-63.657

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Reject to if to Hain-1 = t.005,1 = 63.657

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8:20 AM

QUESTION 1

Calculate the test statistic for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=324.0 versus sigma^2 not equal to 324.0 using alpha=0.2. The sample statistics are n=28, xbar=126.28, S=50.933.

- O ChiSquared0=76.3995
- O ChiSquared0=216.1809
 - ChiSquared0=3.3722
 - ChiSquared0=9.5419

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$$\gamma_0^2 = \frac{(n-1)5^2}{03}$$

Monday, April 28, 2025 8:25 AM

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n=29 x=.01

Construct the rejection region for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=17.64 versus sigma^2 not equal to 17.64 using alpha=0.01. The sample statistics are n=29, xbar=17.28, S=9.817.

- O Reject Ho if chiSquare0<13.56
- Reject H0 if ChiSquare0<12.46 or ChiSquare0>50.99
- O Reject Ho if chiSquare0>48.28
- O Reject Ho if ChiSquare0>50.99
- O Reject H0 if ChiSquare0<13.56 or ChiSquare0>48.28
- O Reject Ho if chiSquare0<12.46

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Rejul Ho if

72) XX/2,11 = X2,005,28 = 50.99

XOLX1-4/2,n-1=X2,995,28 = 12.46

Monday, April 28, 2025 8:29 AM

QUESTION 5

What is the correct conclusion for a test of hypothesis for the variance of a normal distribution. The null hypothesis is Sigma^2=44.89 versus sigma^2 not equal to 44.89 using alpha=0.2. The sample statistics are n=91, xbar=22.64, S=18.005. The value of ChiSquare0 is 649.9488 and the rejection region is reject HO if ChiSquare0<73.29 or ChiSquare0>107.57

Vo-649.9485 Reject Hoif

Reject 10 72, 273.29 -> 10 05 72, 57 -> 10 Reject Ho

O Fail to reject H0
O Reject H0

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QUESTION 1

Calculate the test statistic for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=4.41 versus sigma^2 less than 4.41 using alpha=0.05. The sample statistics are n=10, xbar=12.11, S=0.815.

- O ChiSquared0=23.1902
- ChiSquared0=1.3556
- O ChiSquared0=59.7538
- O ChiSquared0=3.4929

$$= \frac{(10-1)(.8/5)^2}{4.4/1}$$

$$= 1.35-556$$

Monday, April 28, 2025 8:37 AM

Lied to Hi: 02 < 324 **QUESTION 3**

Construct the rejection region for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=324.0 versus sigma^2 less than 324.0 using alpha=0.05. The sample statistics are n=5, xbar=130.0, S=14.414.

- O Reject Ho if ChiSquare0>11.14
- O Reject Ho if chiSquare0>9.49
- O Reject H0 if ChiSquare0<0.48 or ChiSquare0>11.14
- O Reject H0 if ChiSquare0>0.71 or ChiSquare0>9.49
- O Reject Ho if chiSquare0<0.48
- Reject Ho if chiSquare0<0.71

X = .05

12-05,5-1 - 72- 2.71 Reject Hoif 722.71

Reject Ho i

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Chapter 9, Case 3 Upper

Monday, April 28, 2025 8:40 AM

H; 02 = 324

QUESTION 1

Calculate the test statistic for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=324.0 versus sigma^2 greater than 324.0 using alpha=0.05. The sample statistics are n=13, xbar=136.87, S=47.249.

- O ChiSquared0=4.5715
- O ChiSquared0-1.7416
- O ChiSquared0=82.684
- O ChiSquared0=31.4993

 $\gamma_0^2 = \frac{(n-1)5^2}{63} = \frac{(13-1)(13-1)}{320}$

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Chapter 9, Case 3 Upper

Monday, April 28, 2025 8:42 AM

H1:028 >11.56

QUESTION 3

Construct the rejection region for a test of hypothesis for the variance of normal distribution. The null hypothesis is sigma^2=11.56 versus sigma^2 greater than 11.56 using alpha=0.01. The sample statistics are n=2, xbar=30.76, S=4.321.

- O Reject H0 if ChiSquare0<0.0 or ChiSquare0>7.88
- O Reject Ho if chiSquare0<0.0
- Reject Ho if chiSquare0<0.0
- Reject Ho if chiSquare0>6.63
- O Reject Ho if ChiSquare0>7.88
- O Reject H0 if ChiSquare0<0.0 or ChiSquare0>6.63

Priest Hoif $\chi^2 > \chi^2 > \chi^2 > 1 = \chi_{.01} > 1$ Reject Hoif $\chi^2 > \chi^2 > 1 = \chi_{.01} > 1$ Reject Hoif $\chi^2 > \chi^2 > 1 = \chi_{.01} > 1$

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